

# PHENIX Run 15 ZDC $A_N$ vs. $P_T$ Unfolding

CENuM Workshop II

Online

2020-07-03/(04)

4:00 – 4:15 PM (KST/JST)

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## Introduction

- Physics motivation
- Experimental procedures( detector, asymmetry measurement)

## Unfolding Overview and Motivation

- Transverse momentum smearing (1D) unfolding
- Transverse momentum and azimuthal angle smearing (2D) smearing
- Closure test

## Unfolding neutron asymmetry for inclusive pp collisions in the ZDC

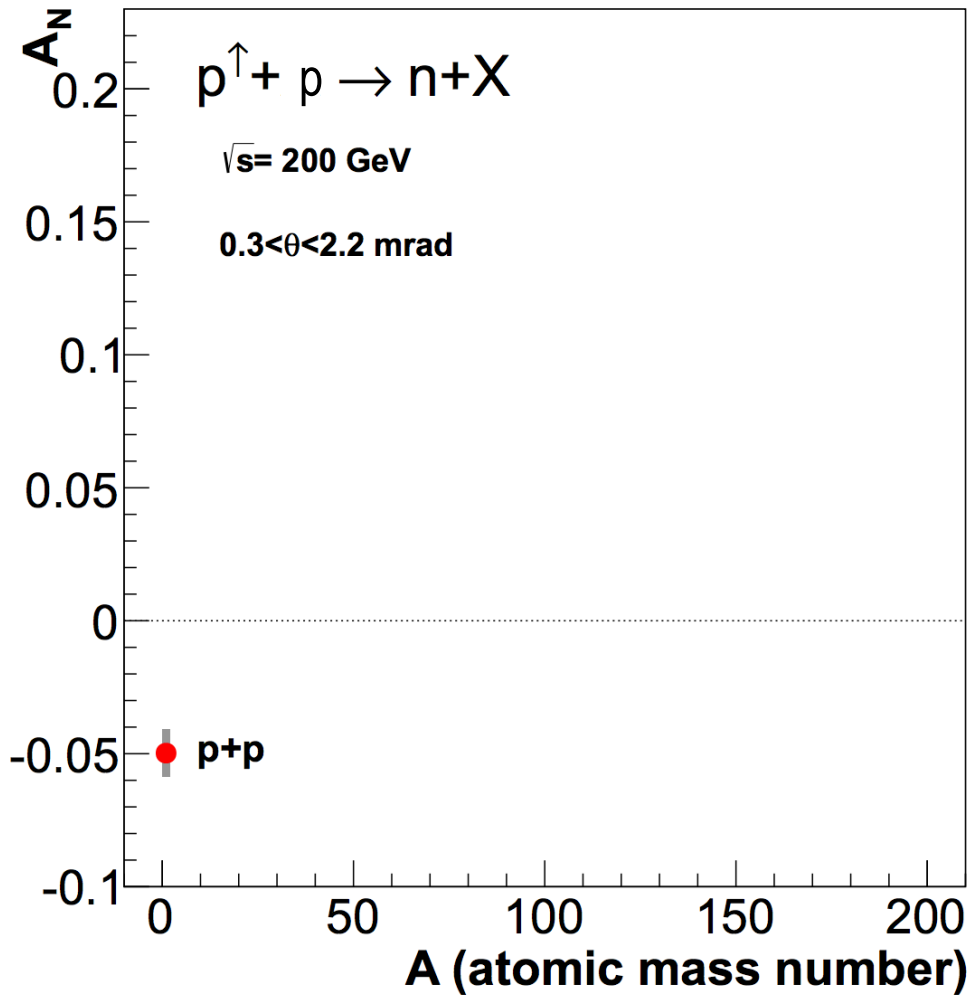
- Strategy
- Algorithm
- Asymmetry creation and reweighting

## Conclusions

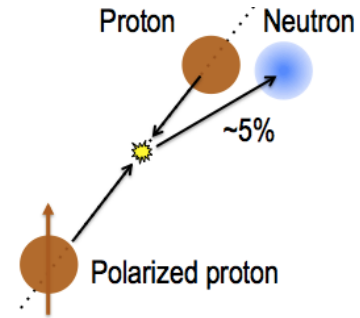
- Summary
- Short term plan

# Introduction

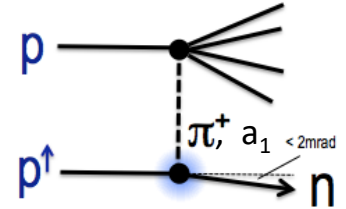
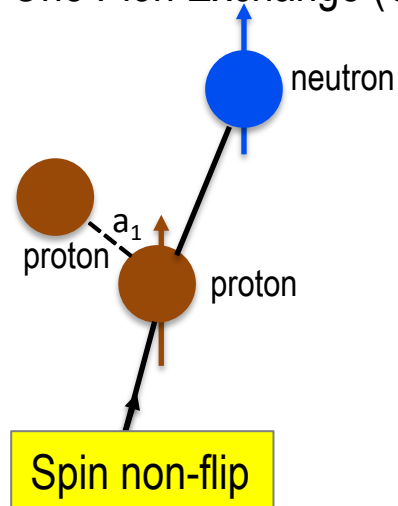
**Physics Motivation** (polarized proton – unpolarized proton collisions at 200 GeV)



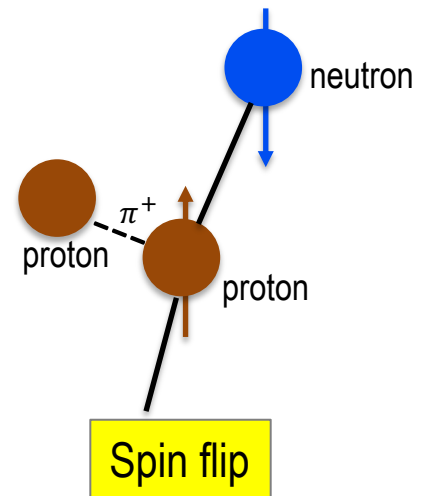
PHENIX Run15 p + p result at 200 GeV



One Pion Exchange (OPE) Model



One Pion Exchange (OPE)

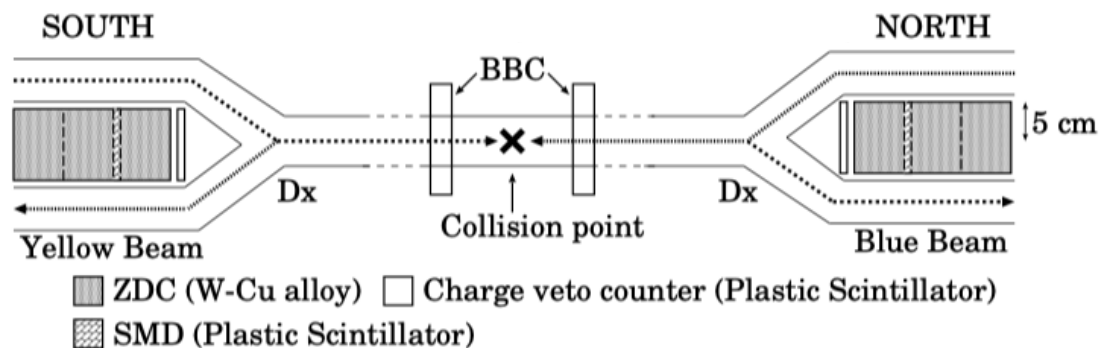
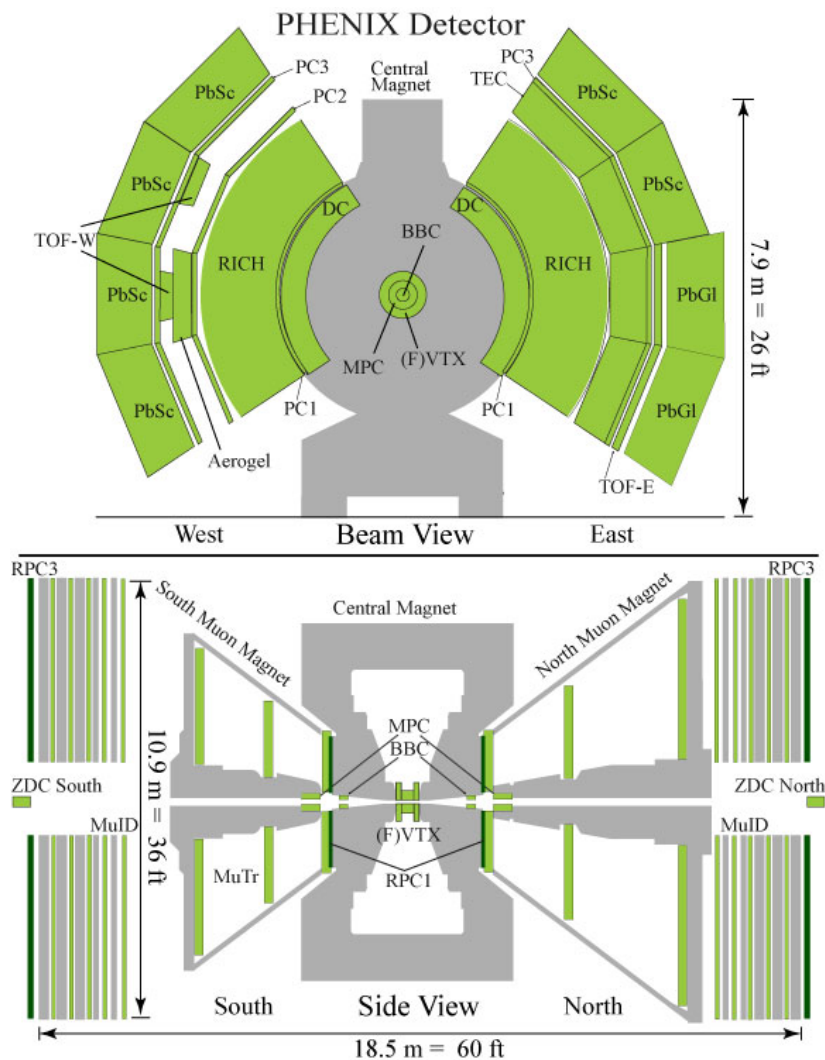


We seek to understand proton spin in terms of  $A_N$  vs. true  $P_T$ .  
This will be the first pp unfolding  $A_N$  vs true  $P_T$  result at PHENIX.

# Introduction

## Experimental Procedures ( PHENIX Detector – Layout of the PHENIX Zero Degree Calorimeter)

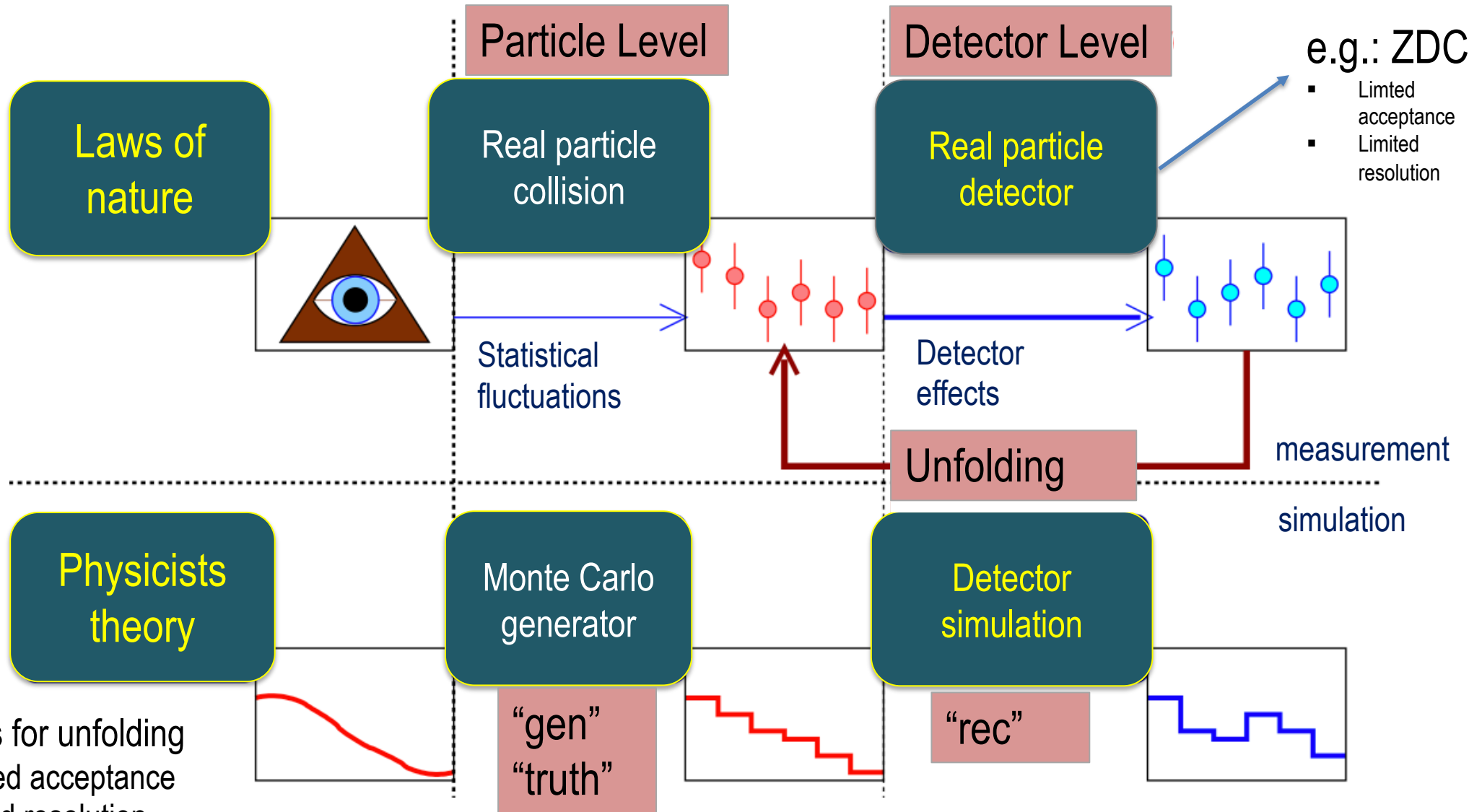
Setup for very forward neutron measurement at PHENIX



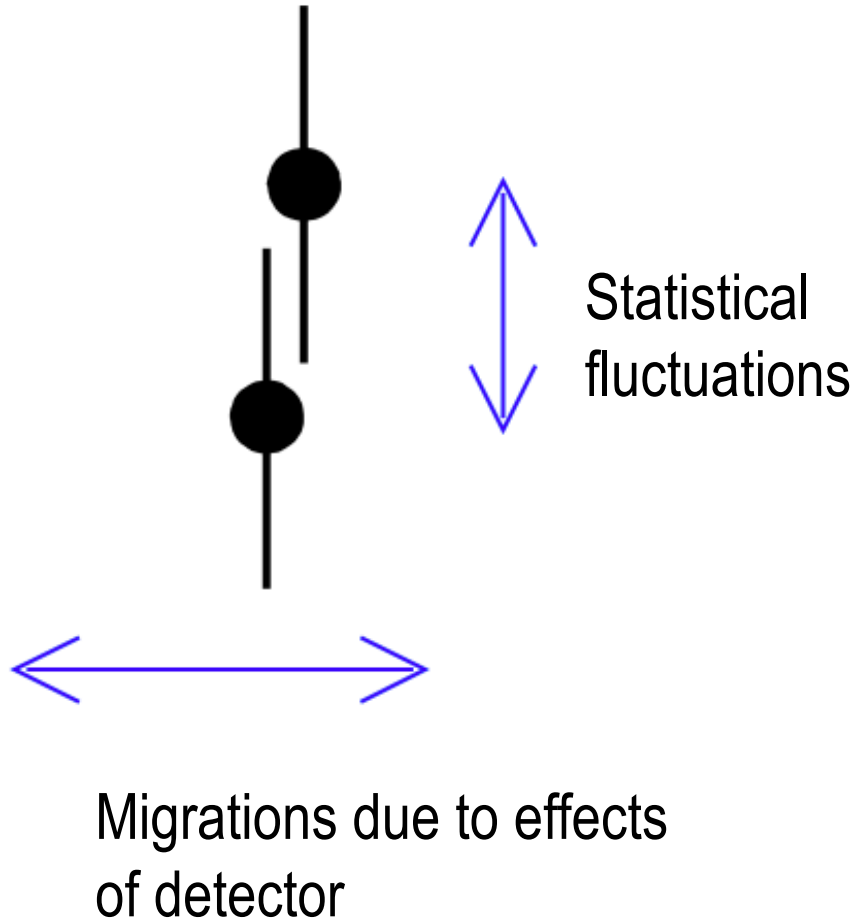
Principal components for neutron physics:

- © Zero Degree Calorimeter (neutron measurement)
- © Shower Maximum Detectors (for neutron position measurement)
- © Charge veto counter (charged particles) and BBC (timing)

# Unfolding Overview and Motivation – Limited Acceptance and Resolution



# Unfolding Overview – Statistical fluctuations and migrations due to detector effects



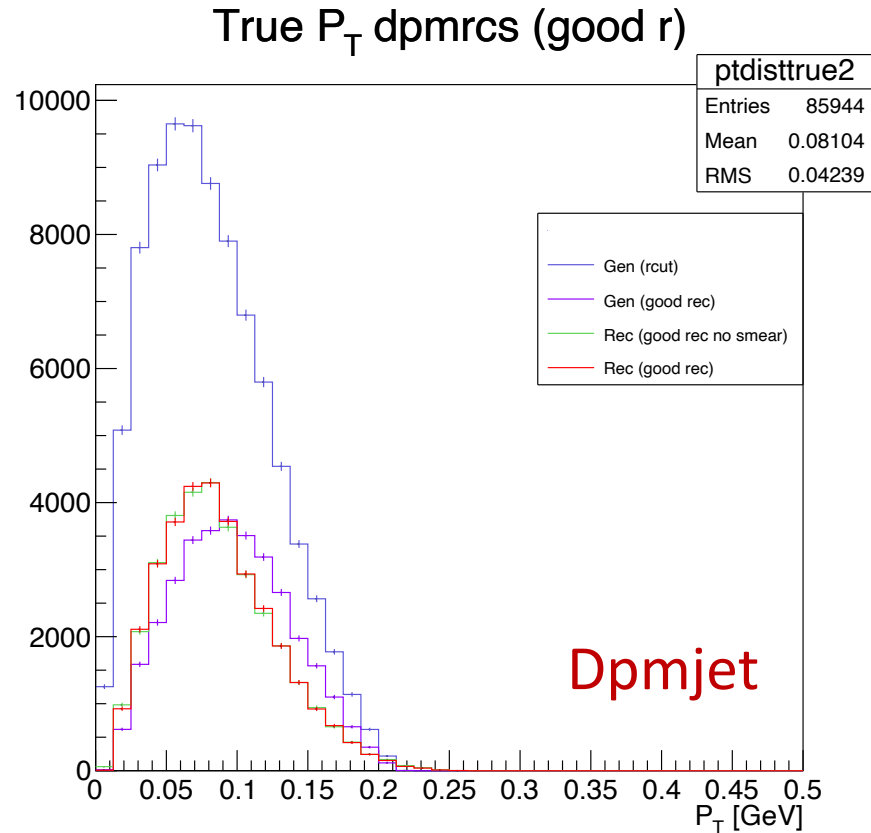
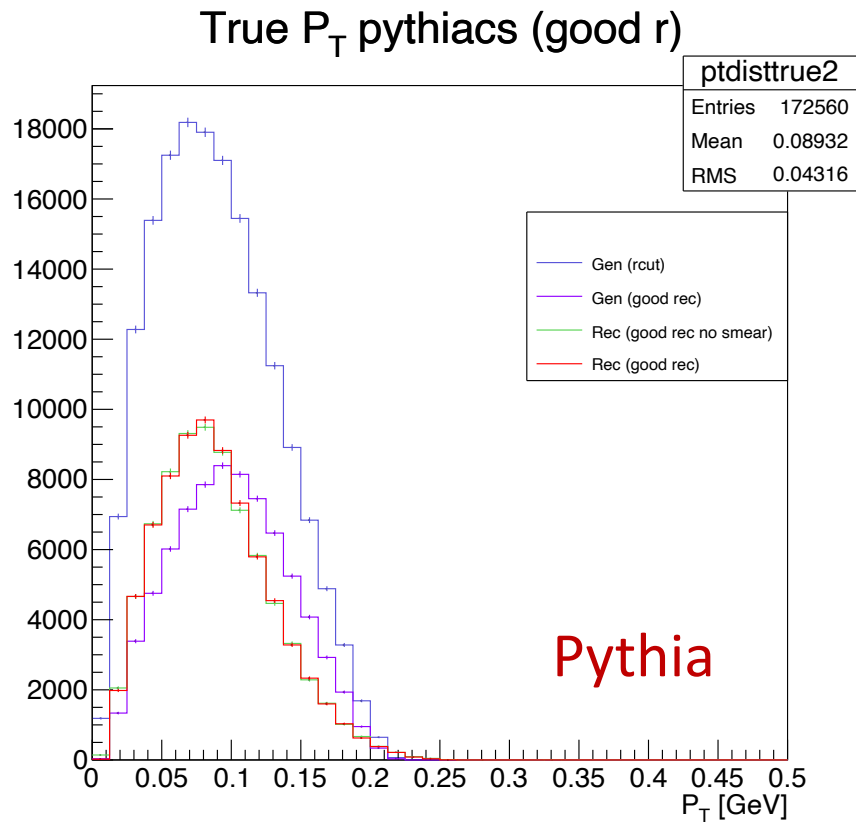
## Unfolding:

- Used to correct for migration effects in the presence of statistical fluctuations.

## Result:

- An estimator of the “truth” distribution.
- Covariance matrix (statistical uncertainties)

# Transverse Momentum SVD Unfolding Closure Test **Unfolding Input**

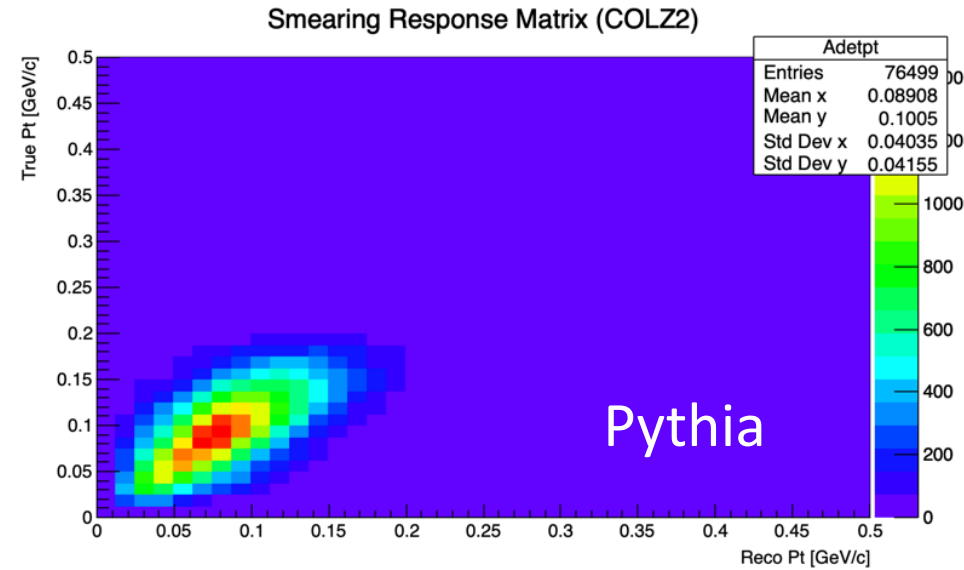


1. Gen (rcut) : **Blue line** with  $r_{min} < 0.5$  and  $r_{max} < 4.0$  cm
2. Gen (good rec): **Purple line** with cuts:  $r_{cut}$ ,  $E_{min} > 20$  GeV and  $E_{max} < 120$  GeV,  $E_{ZDC2}/E_{ZDC1} > 0.03$ ,  $N_x N_y > 1$  fired above  $E_{smdxy} = 0.003$  GeV
3. Rec (good rec no smear): **Green line** – no smearing
4. Rec (good rec): **Red line** – is reconstructed.

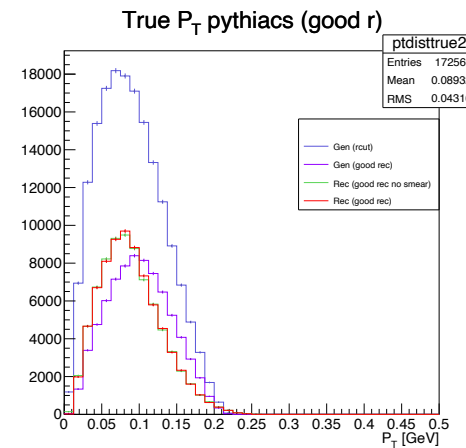
$$P_{T(True)} = \sqrt{p_x * p_x + p_y * p_y}$$

$$P_{T(Reco)} = \frac{r E_{reco}}{IP_{To\_ZDC}} \quad \text{with } r = \sqrt{x_{ev} * x_{ev} + y_{ev} * y_{ev}} \quad \text{and IP is the distance from the collision point to ZDC)}$$

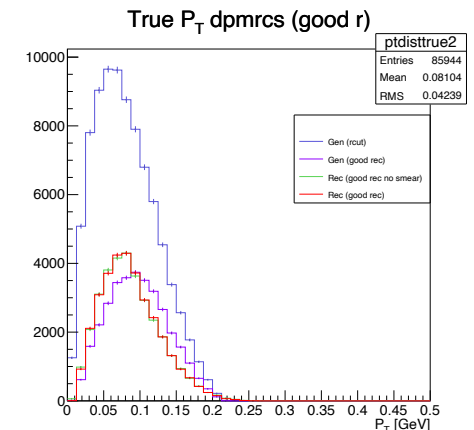
# Transverse Momentum SVD Unfolding Closure Test **Unfolding Input**



- Detector smearing matrix from pythia Monte Carlo.
- It maps the smeared (reco) pt in red line to the true pt in purple line of Pythia Monte Carlo sample.

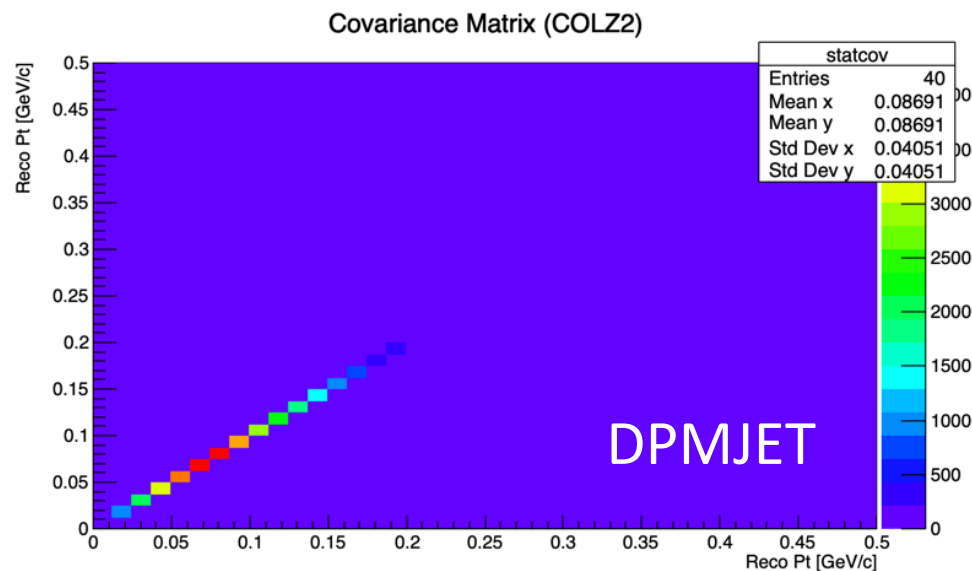


Pythia



Dpmjet

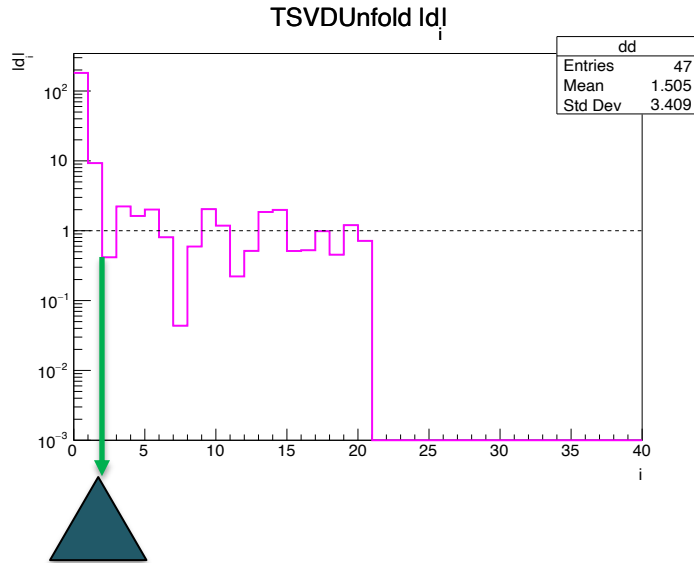
- Input covariance matrix obtained from the square of the errors of the smeared pt (red line) from dpmjet.
- Unfolding is based on the singular value decomposition(SVD) of detector response matrix.





# Transverse Momentum SVD Unfolding Closure Test **Unfolding Result**

Unfolding is performed with an optimal regularization parameter obtained from a d vector distribution for a regularized system:



$$d_i = z_i^\tau \frac{s_i^2 + \tau}{s_i}, \quad i = 1, \dots, \text{Nbin}$$

$\tau = \text{Kreg}$  (regularization parameter)

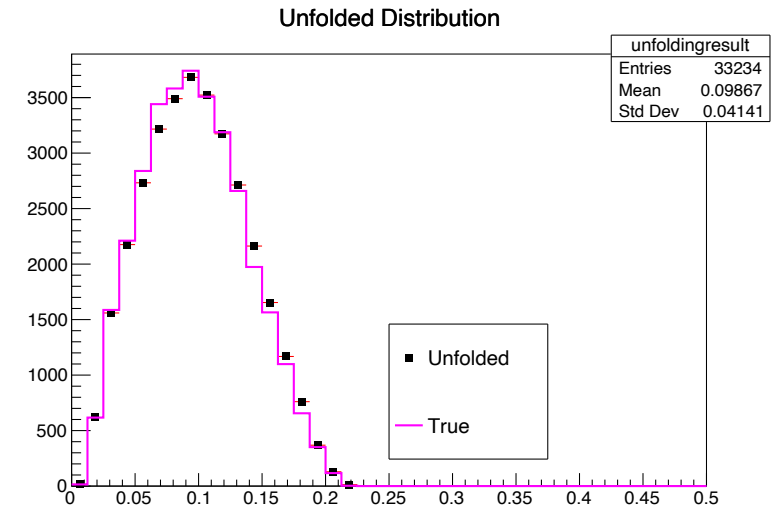
$s_i$  = positive diagonal elements (singular values of response matrix)

$\tau$  = nonzero (regularized system)

= zero (non-regularized system),  $d_i = s_i \cdot z_i^{(0)}$  (diagonal systems - not useful)

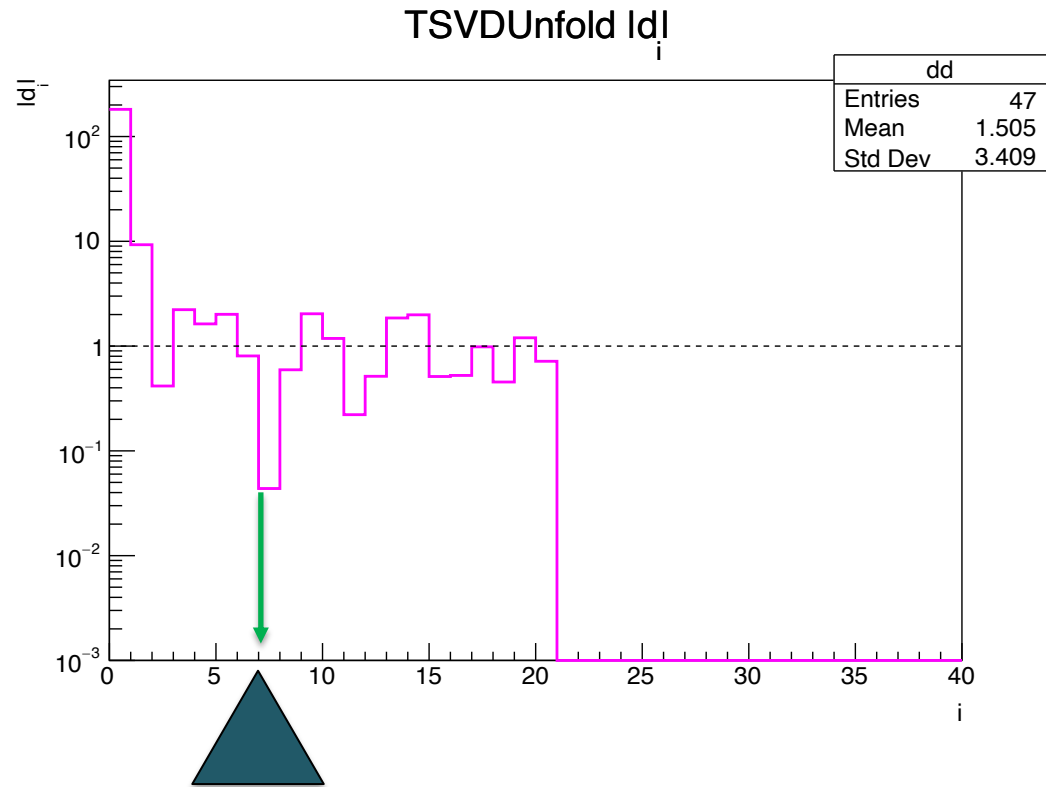
Unfolded the measured pt distribution using regularization parameter = 2

Parameter = 2 gives the best **minimum curvature = 0.000007** and is chosen as the optimum value.



Magenta line: True spectrum from dpmjet MC.

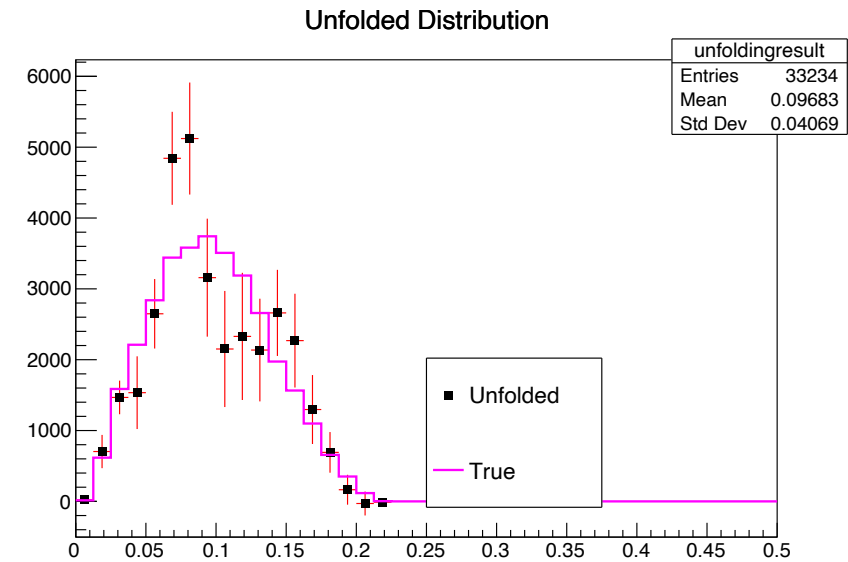
# Transverse Momentum SVD Unfolding Closure Test **Unfolding Result**



Unfolded the measured pt distribution using **regularization parameter = 7**

**Regularization parameter = 7** gives a large **minimum curvature = 0.343233**.

Best minimum curvature should be almost zero but not zero.



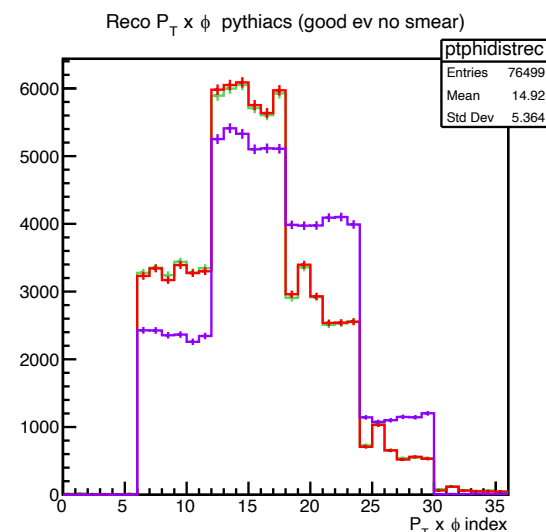
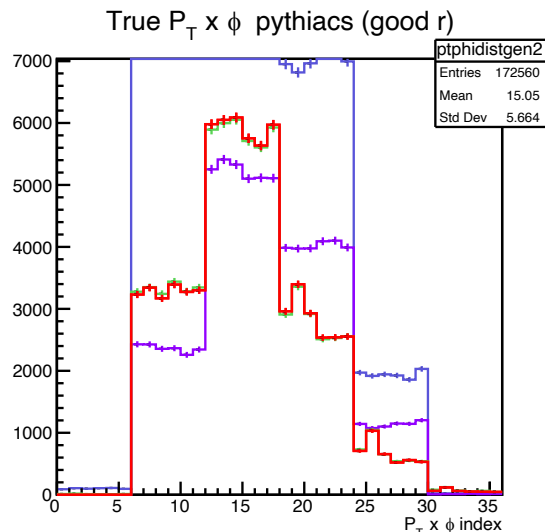
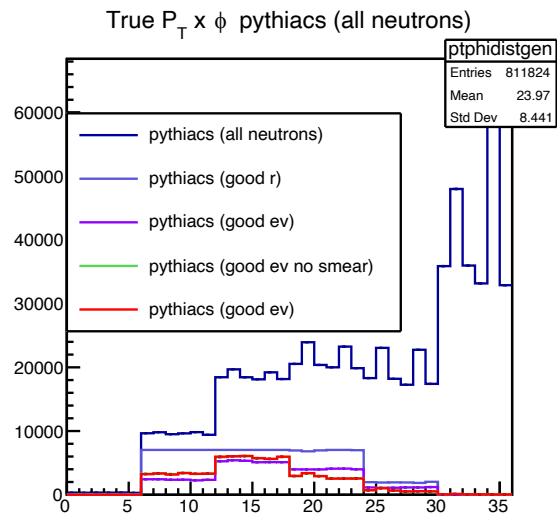
Magenta line: True distribution from dpmjet MC.

Solid black boxes: Unfolded distribution.

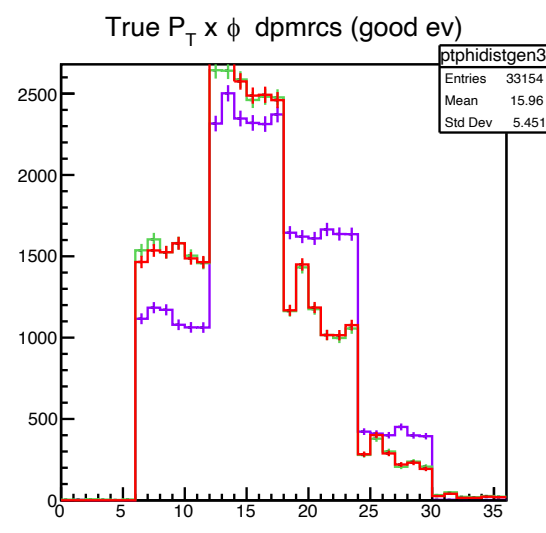
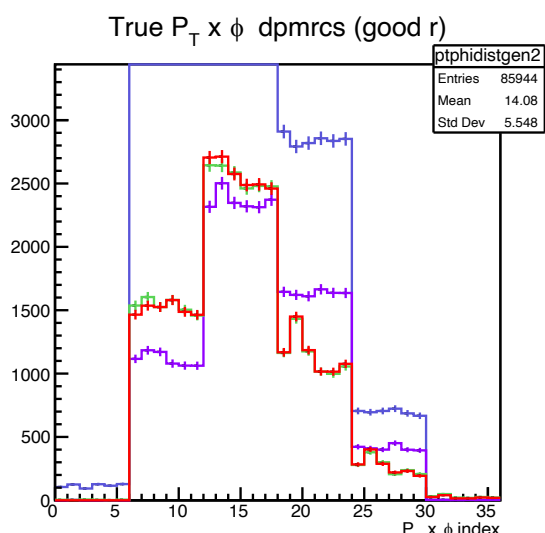
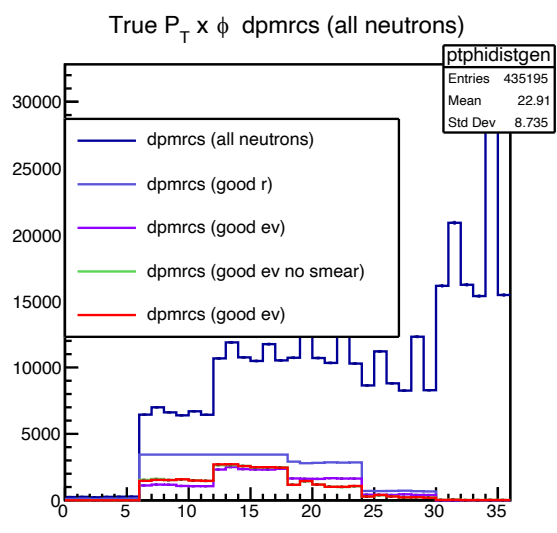
Unfolded distribution has been scaled to match the statistics between dpmjet and pythia.

# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Input



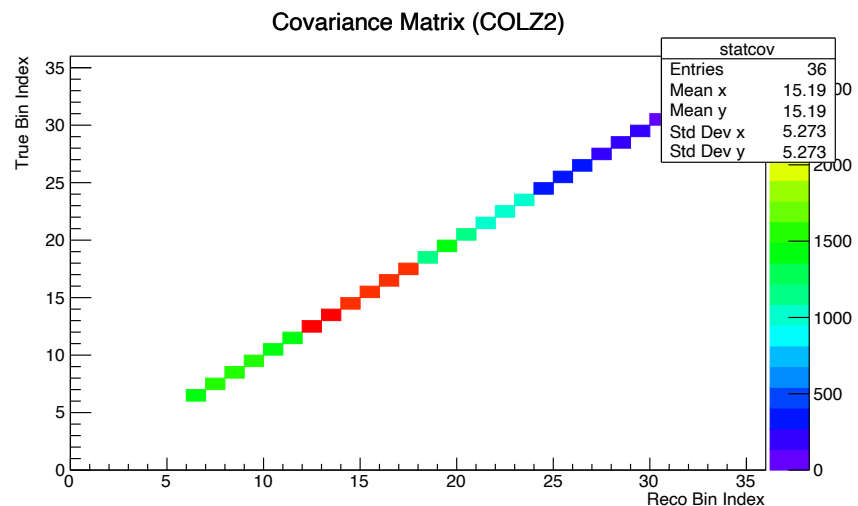
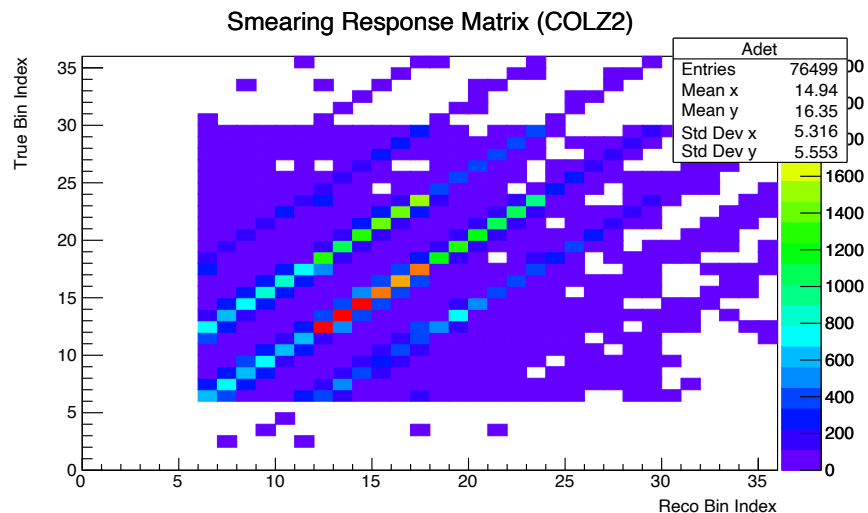
Pythia



Dpmjet

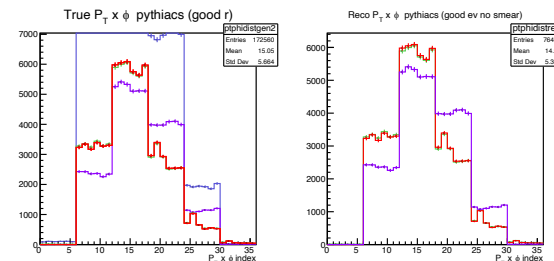
# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Input

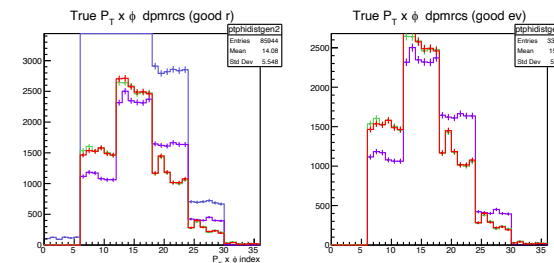


Correlation matrix between true and measured  $p_t$  in azimuth  $\phi$  distributions.  
Two variables are being used here  $p_t$  and  $\phi$ .

Pythia



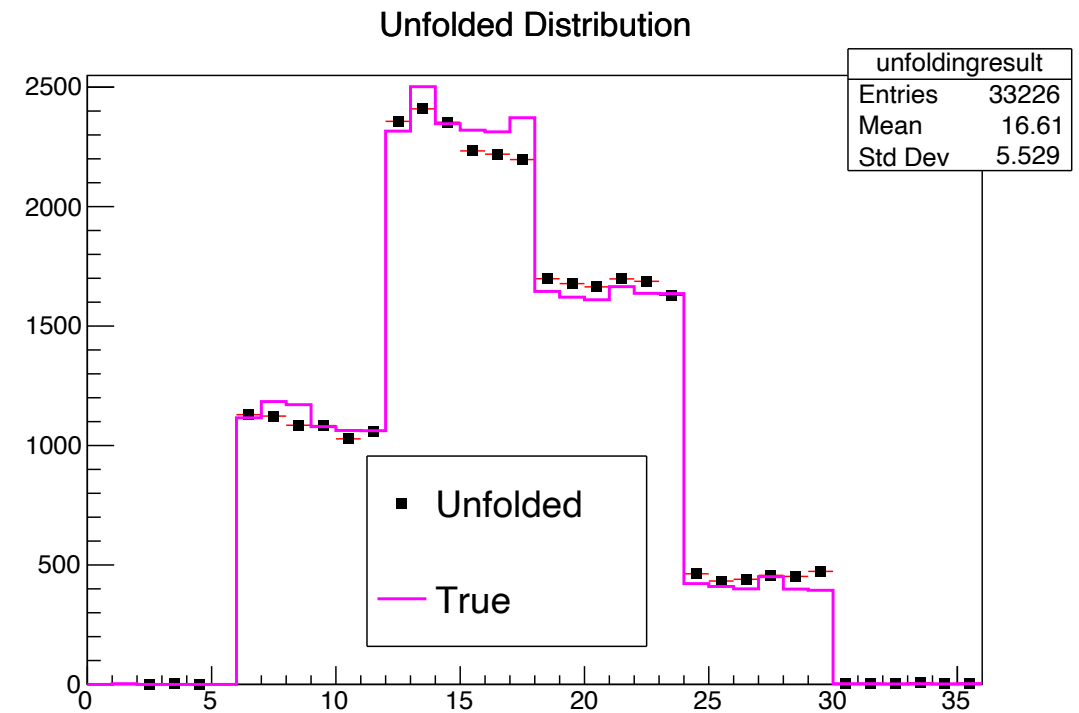
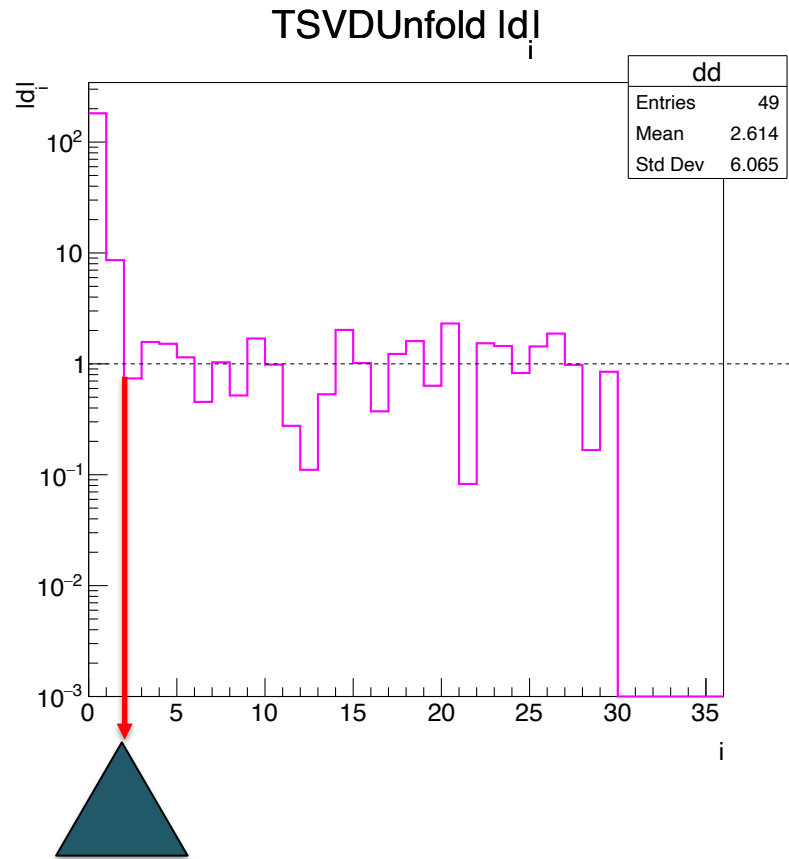
Dpmjet



Input covariance matrix obtained from the square of the errors of the reconstructed transverse momentum ( $p_t$ ) distribution (red line) from the Dpmjet Monte Carlo sample.

# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Result



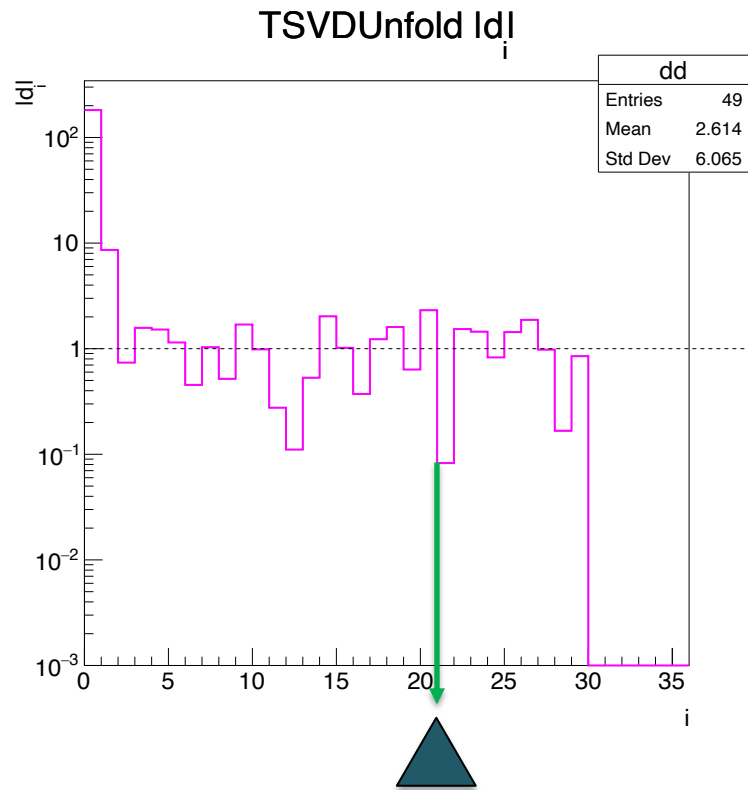
Unfolded the measured pt distribution using **regularization**  
**parameter = 2**  
Minimum curvature = **0.000002**

Magenta line: True distribution from dpmjet.

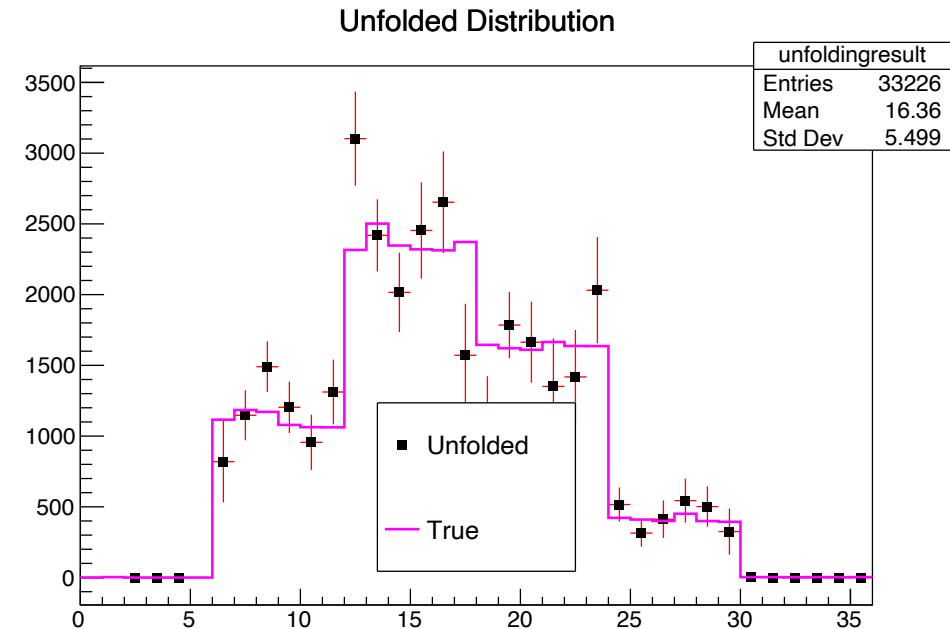
Solid black squares: the unfolded distribution.

# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Result



Unfolded the measured pt distribution using **regularization parameter = 21** with a minimum curvature equal to **0.583**

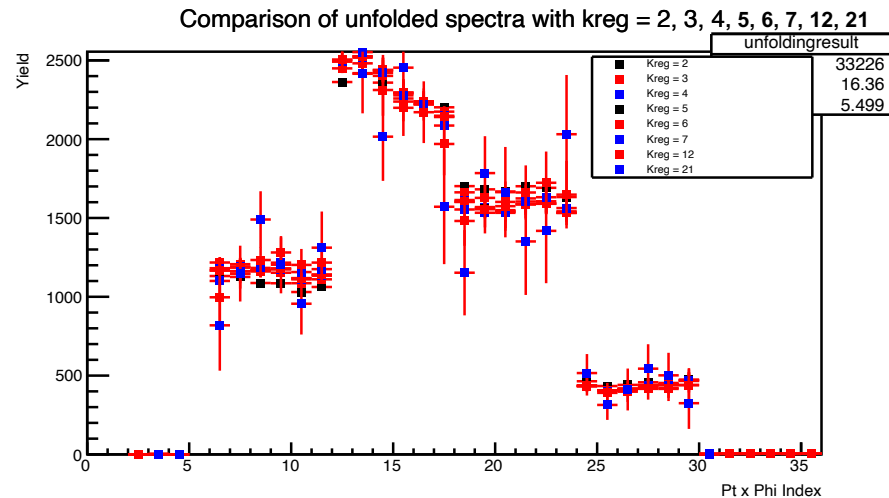
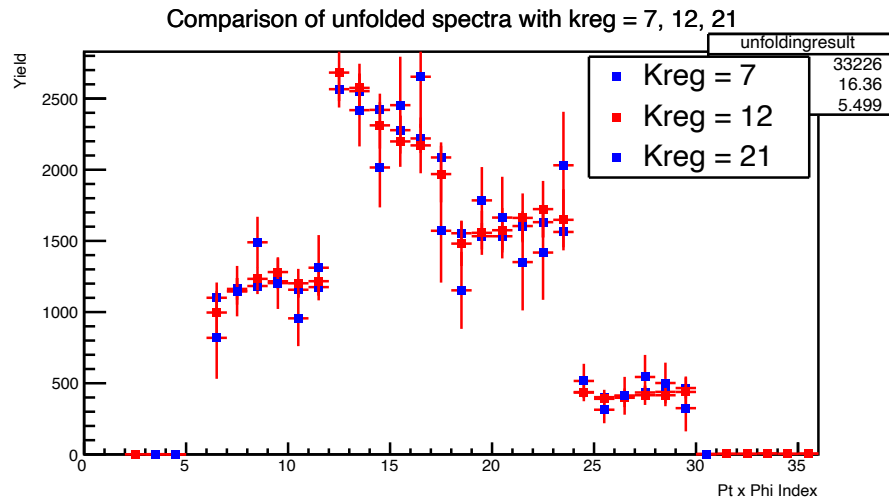
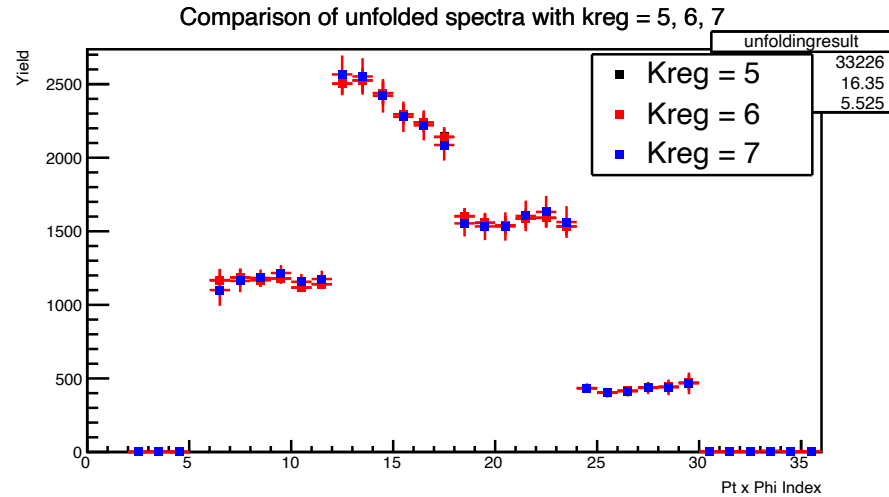
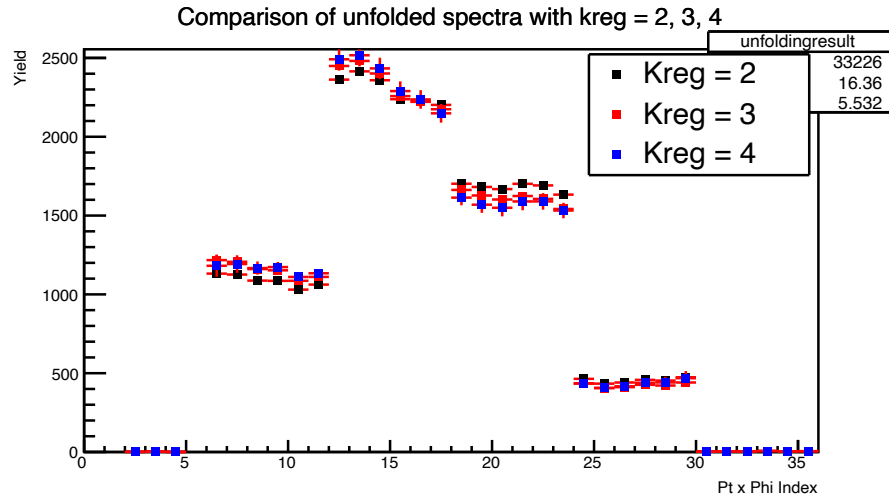


Magenta line: True distribution from dpmjet.

Solid black squares: the unfolded distribution.

# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Result



Transverse momentum ( $P_T$ ) and azimuth ( $\phi$ ) unfolding closure test results – all possible parameter comparison

# Transverse Momentum and Azimuth SVD Unfolding Closure Test

## Unfolding Result

Summary of all possible kreg values and their corresponding minimum curvature values

Regularization parameter, Kreg	Minimum curvature value determines best optimum regularization parameter, the closer the value to zero the better			
2	1D		2D	
	0.000002	Best value	0.000002	Best value
3			0.000010	
4			0.000201	
5			0.000307	
6			0.000331	
7	0.343233.	~34%	0.009416	
12			0.009416	
21			0.583000	~ 60%



# Run 15 neutron asymmetry for inclusive pp collisions in the ZDC – 2D Unfolding

## Strategy

To unfold the ZDC neutron asymmetry for inclusive pp collisions run 15 data, one strategy is to:

- Translate the available pt dependent  $A_N$ 's into yields.
- Apply the 2D unfolding in  $P_T$  and azimuth,  $\Phi$
- Extract the unfolded asymmetries ( $A_N$ 's) with systematic uncertainty.

Above strategy requires creation of artificial asymmetries and reweighting procedures of pp One Pion Exchange (OPE) Monte Carlo training sample.

## Algorithm

Asymmetry creation and and extraction algorithm is as follows:

## Algorithm

1. Create two spin states using TRandom Number Generator:  
Spin up (1)  
Spin down (0)
2. Create spin depended weight according to Taylor series of a polynomial in the form:

$$w = 1 + (a + b * P_{T,T} + c * P_{T,T}^2 + d * P_{T,T}^3) \cos(\varphi_T + spin * \pi)$$

the parameters are:

**a** = constant

**b** = linear

**c** = quadratic

**d** = cube

spin \* pi = phase shift

spin = 0 (down)

1 (up)

**Note:** Other functional forms can also be scanned and tried to describe data asymmetries.

## Algorithm...

3. Scan parameters for different functional forms over a wide range using chi-square based on the reconstructed asymmetries from monte carlo samples and run 15 pp asymmetry results (Minjung's result) to find the best parameter, i.e. parameter with lowest,

$$\chi^2 = \sum_i \frac{(A_{N,i}^{Minjung} - A_{N,i}^{w,reco})^2}{(\Delta A_{N,i}^{2,Minjung} + \Delta A_{N,i}^{2,w,reco})}$$

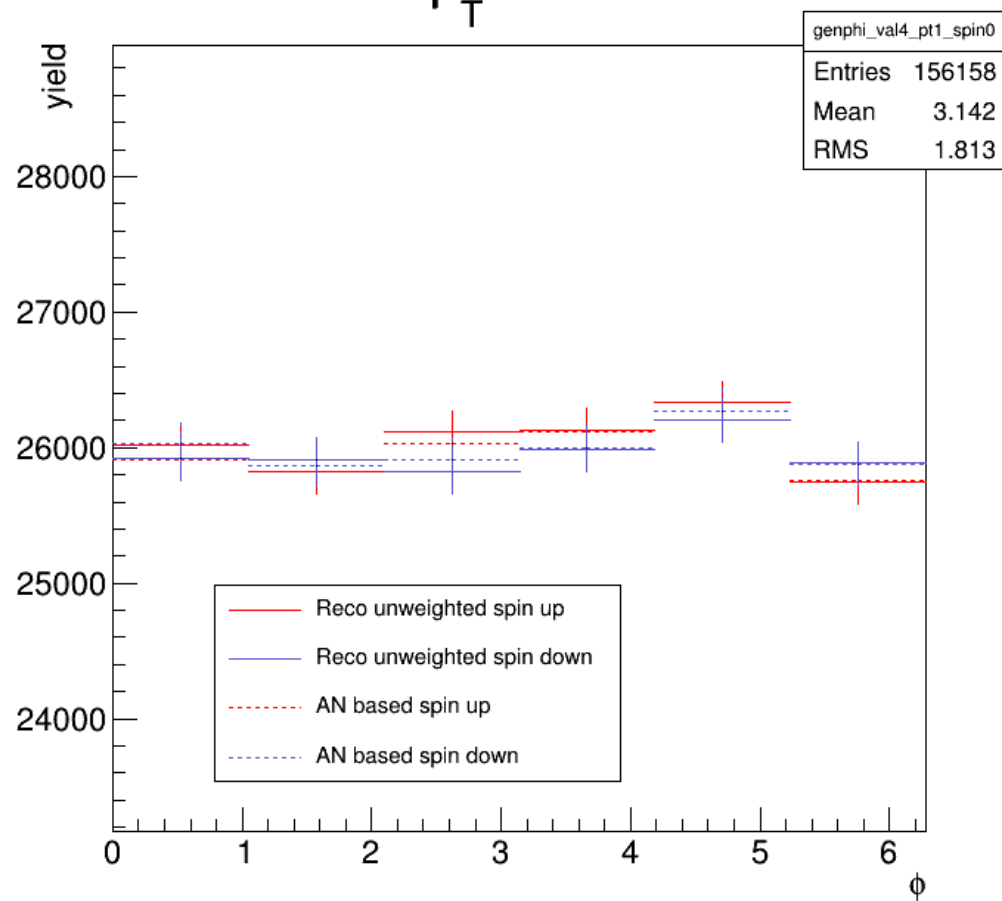
4. Extract the asymmetry using the best Chi-squared parameters,

$$A_N = \frac{N_{\Phi\uparrow} - N_{\Phi\downarrow}}{N_{\Phi\uparrow} + N_{\Phi\downarrow}}$$

# Unweighted and Weighted Azimuth Distribution – One Pion Exchange (OPE) MC

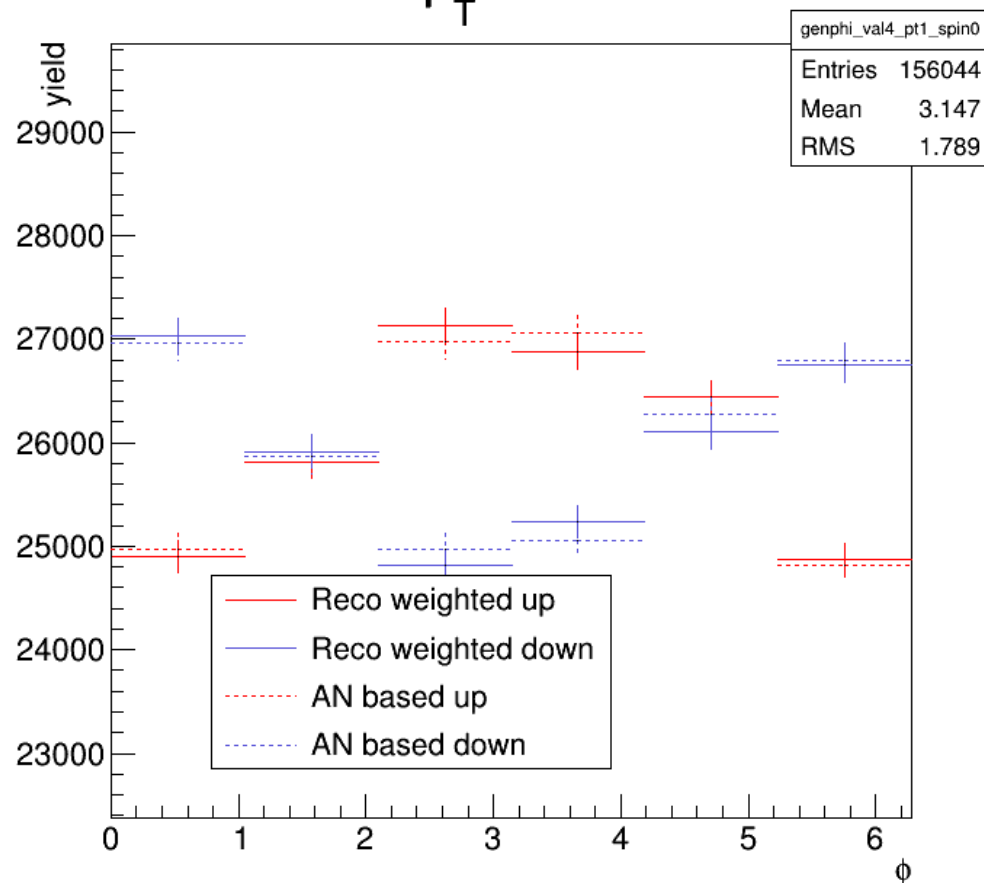
Unweighted

$p_T$  bin 1



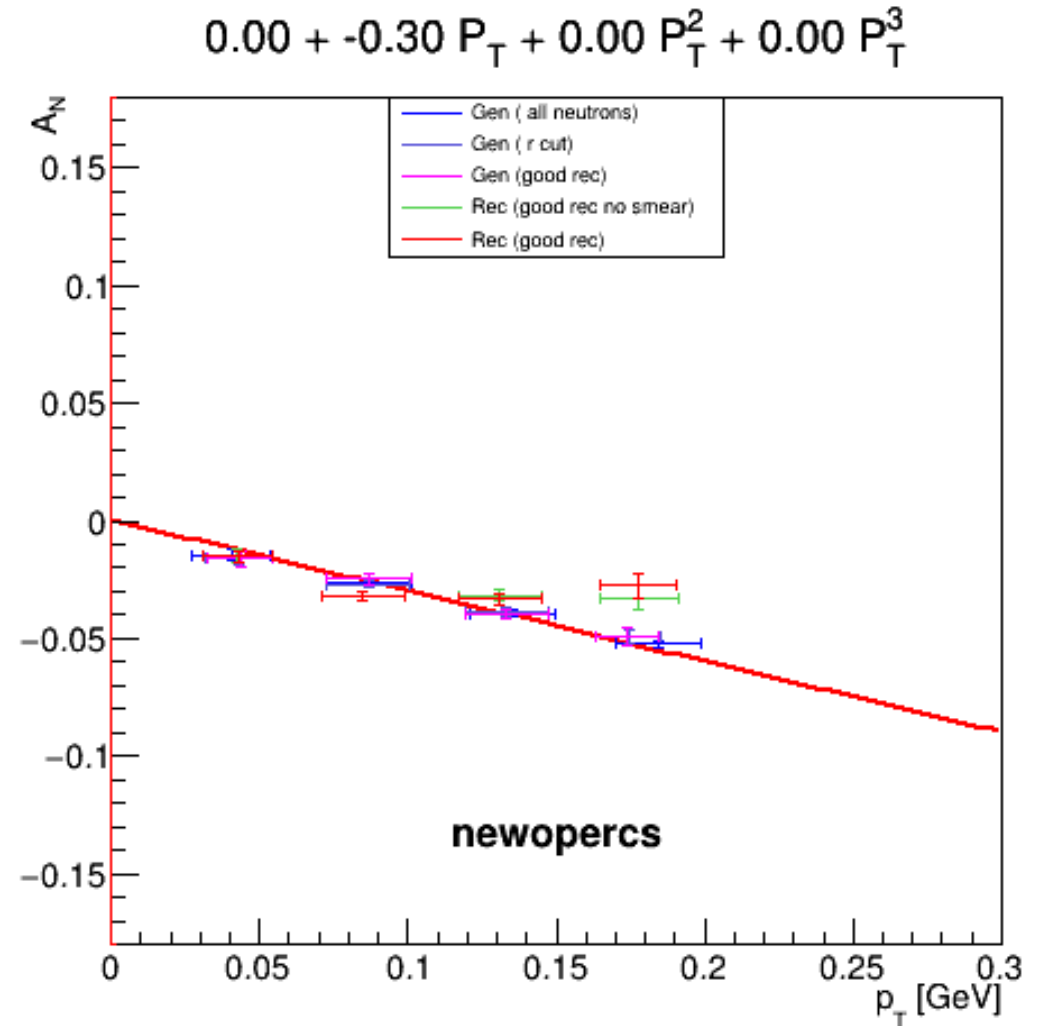
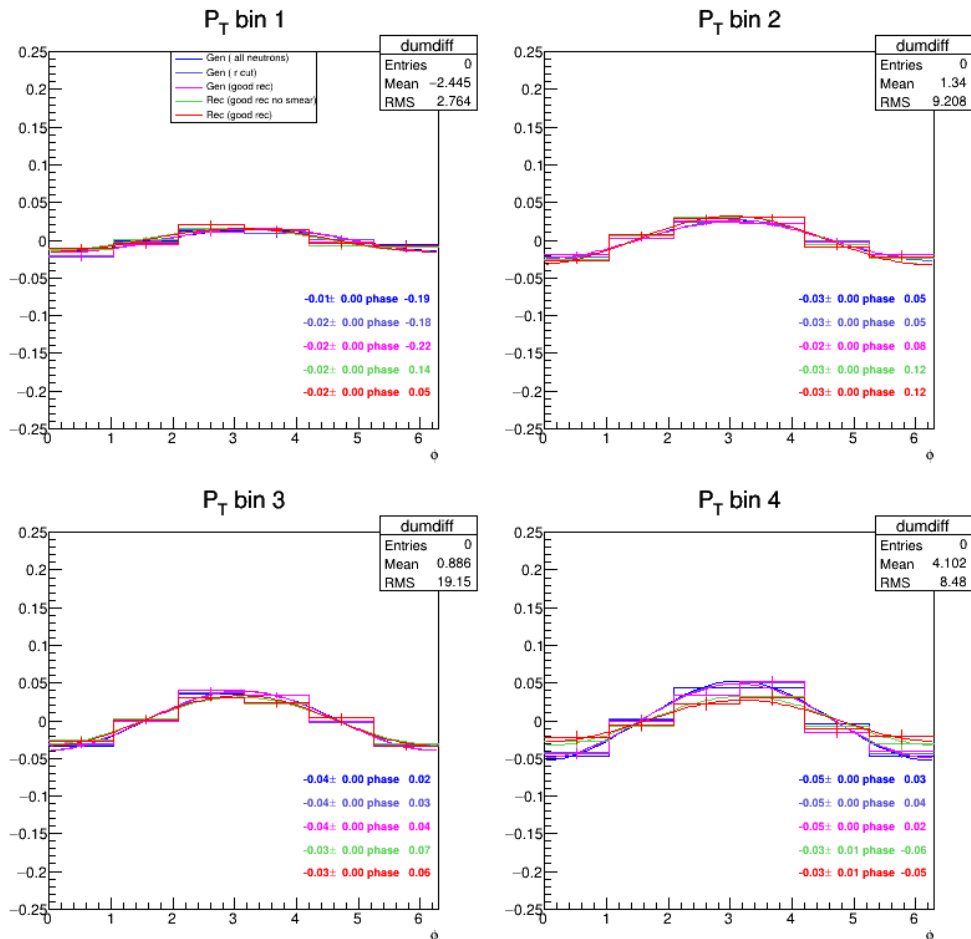
Weighted

$p_T$  bin 1



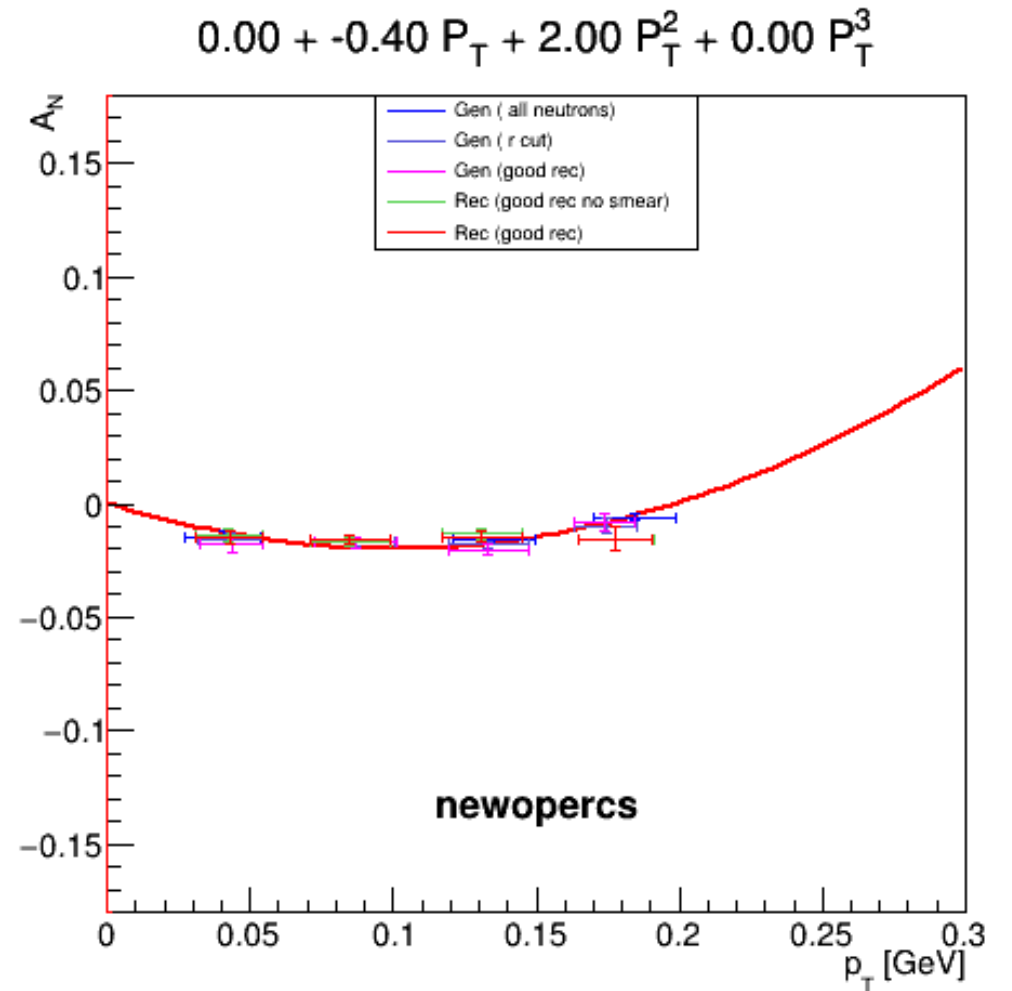
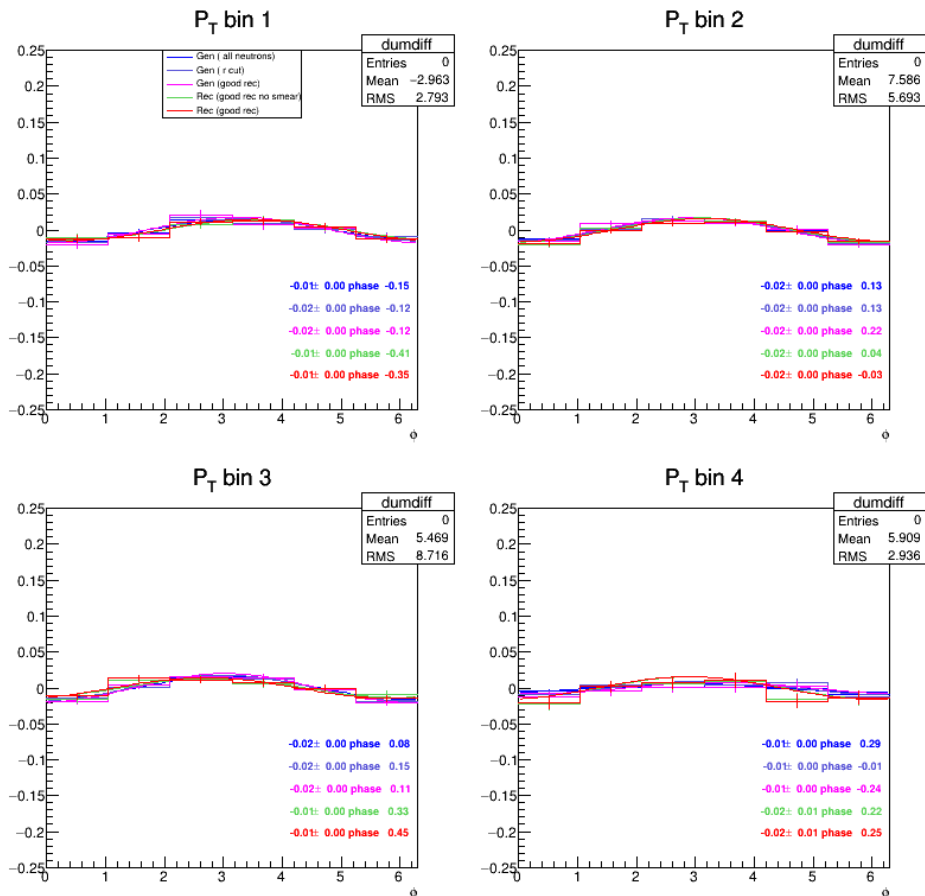
# A Scan of Created Asymmetries – One Pion Exchange (OPE) MC

## Asymmetry based on linear function



# A Scan of Created Asymmetries – One Pion Exchange (OPE) MC

## Asymmetry based on quadratic function



# Summary

- Closure test works well with a regularization parameter = 2. For regularization parameters  $> 7$  statistical fluctuations become very large. Similar trend is observed in both 1D and 2D unfolding cases.
- Regularization parameters  $< 7$  difference comparison form a good estimate of the unfolding systematic errors.
- Scanned neutron asymmetries for linear and quadratic functions for OPE using parameters chosen intuitively.
- Optimize algorithm by using chi square to scan linear, quadratic and cubic terms over a wide range and determine the best parameters with a minimum chi square between reconstructed asymmetries and experimental data.

## Short Term Plan

Period	Task
July 1 ~ July 15	<ul style="list-style-type: none"><li>▪ Optimization of weight to mimic the actual pT dependence of pp data using best parameters from Chi-square.</li></ul>
July 16 ~ July 31	<ul style="list-style-type: none"><li>▪ Apply best parameters to extract neutron asymmetries that mimic pp experimental data asymmetries and compiling the analysis note.</li></ul>

# Working Group



Korea Univ. CENuM  
Director Prof. B.  
Hong – Thesis  
Advisor



RIKEN and RBRC's  
Dr. H. En'yo (Rad.  
Lab. Head)



RIKEN and RBRC's Dr.  
Y. Akiba (Spokesperson  
- PHENIX)



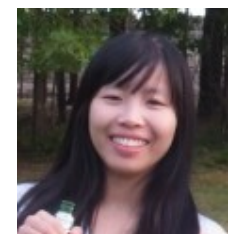
BNL's Dr. A. Bazilevsky (left) and  
RIKEN (RBRC)'s Dr. I.  
Nakagawa(right)



RIKEN and  
RBRC's Dr. Y.  
Goto



RIKEN and RBRC's Dr.  
R. Seidl (Spin PWG  
Convener)

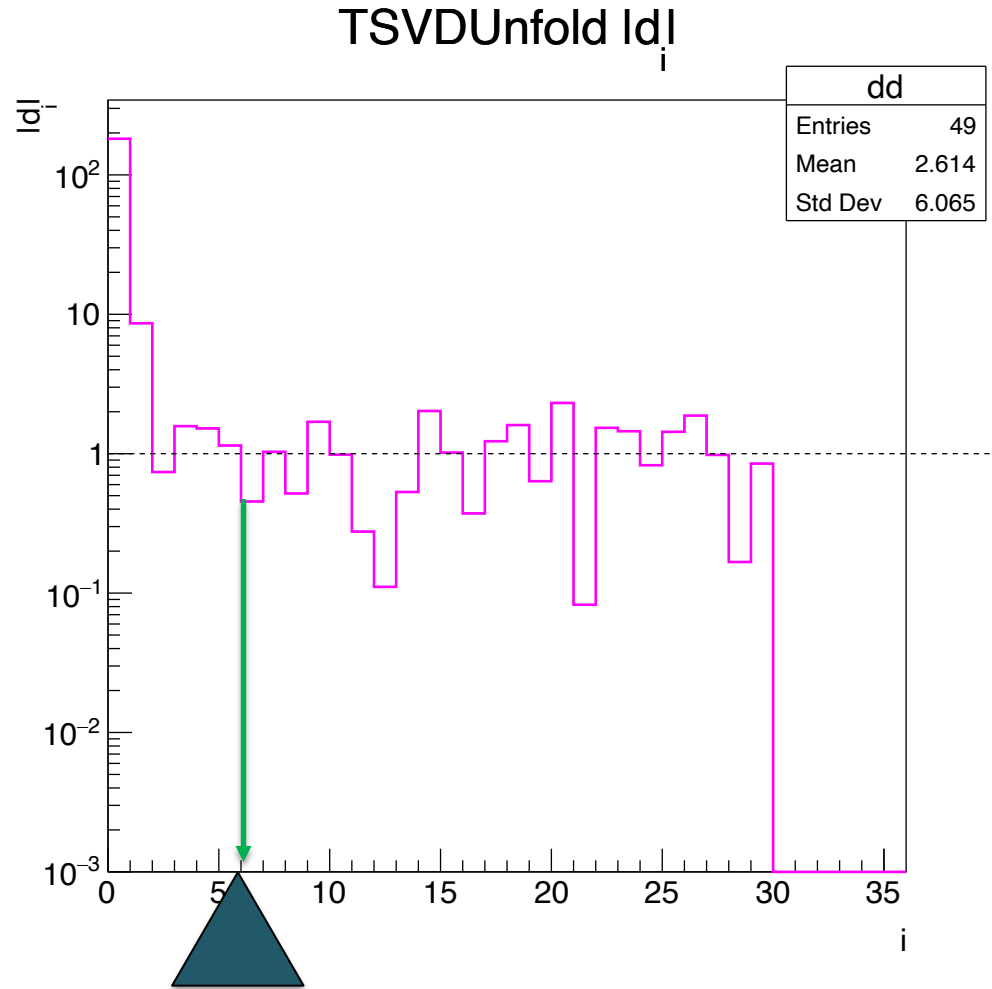


SBU's Dr. Sanghwa  
Park (Spin PWG  
Convener)

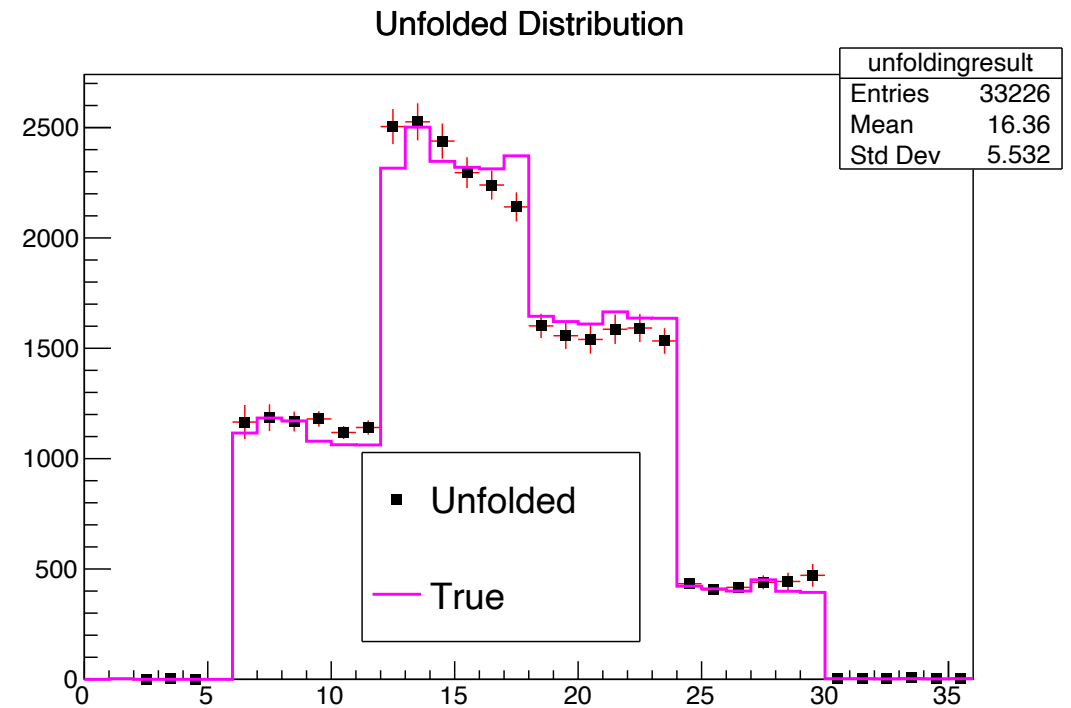


**BACKUP**

# Two-dimensional pt unfolding closure test – Regularization parameter = 6



Unfolded the measured pt distribution using regularization parameter = 6  
Minimum curvature = 0.000331

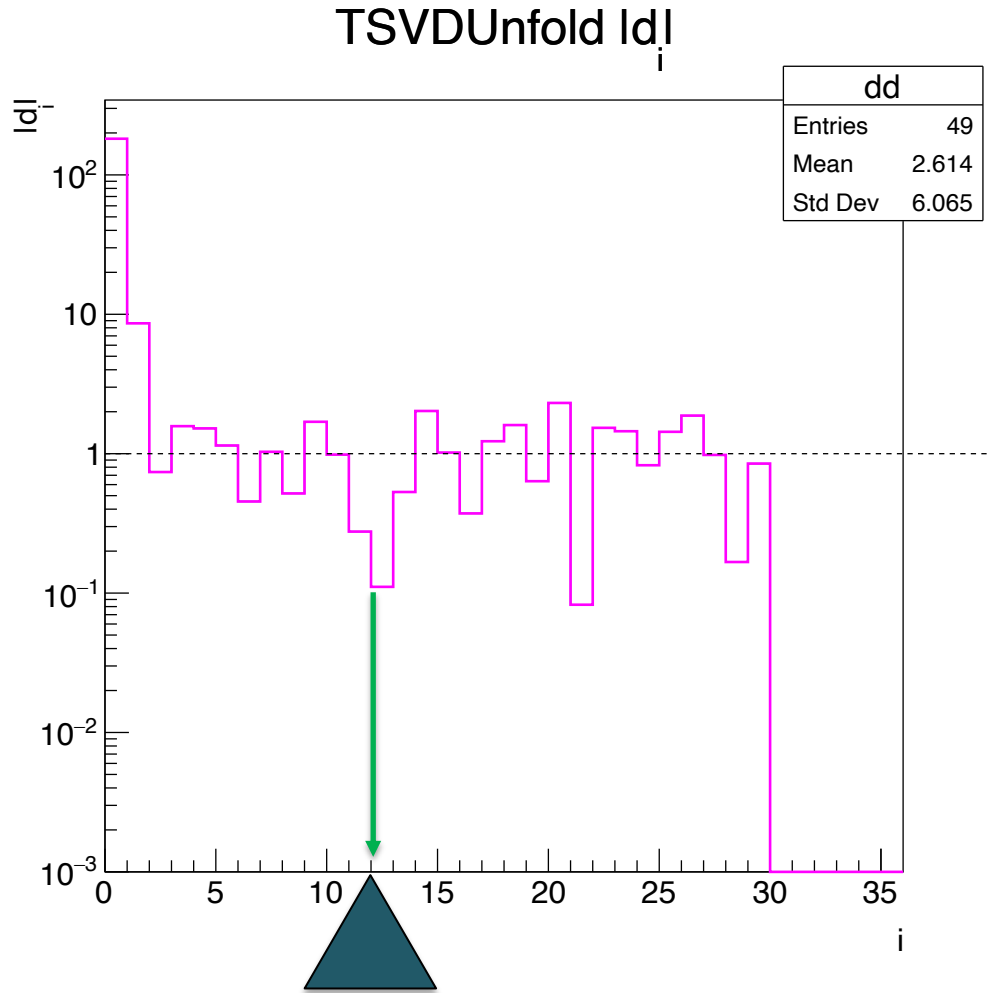


Magenta line: True distribution from dpmjet MC.

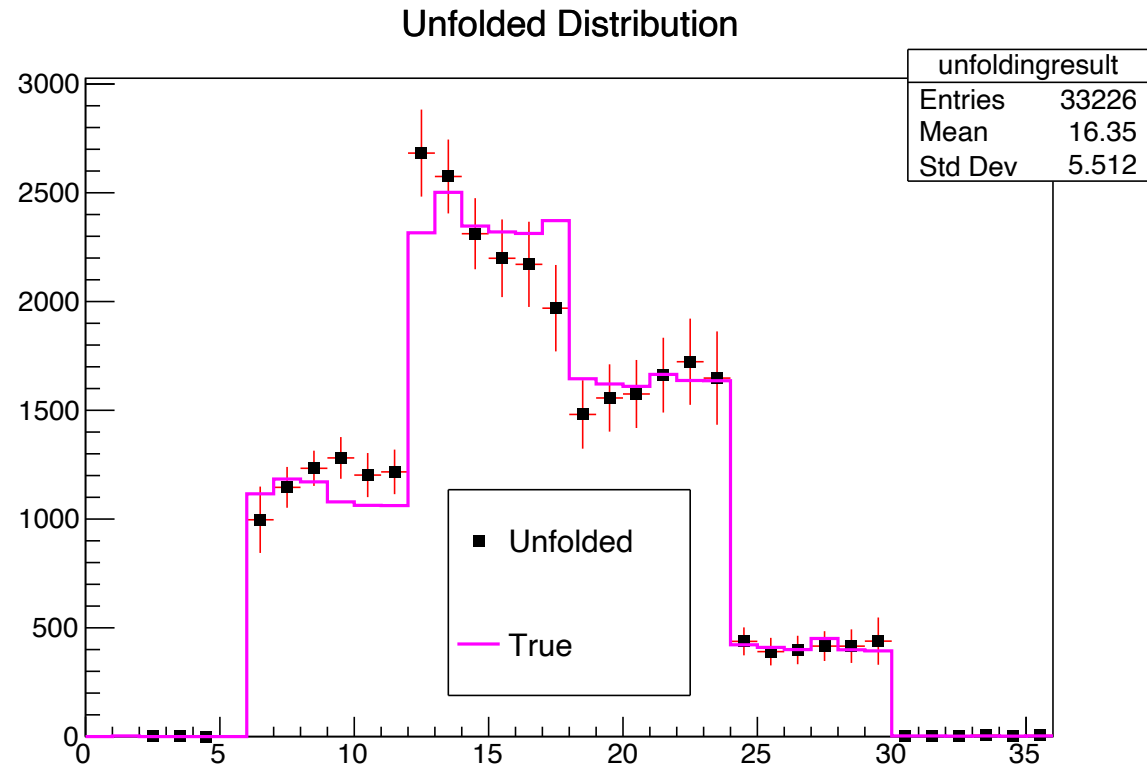
Solid black boxes: Unfolded distribution.

Unfolded distribution has been scaled to match the statistics between dpmjet and pythia.

# Two-dimensional pt unfolding closure test – Regularization parameter = 12



Unfolded the measured pt distribution using regularization parameter = 12  
Minimum curvature = 0.009416

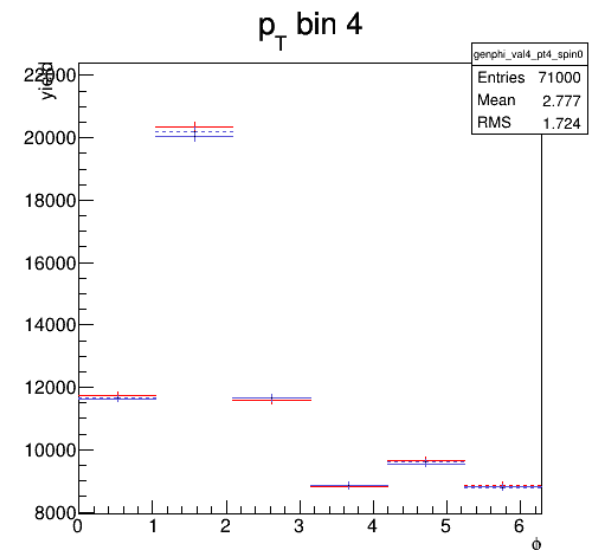
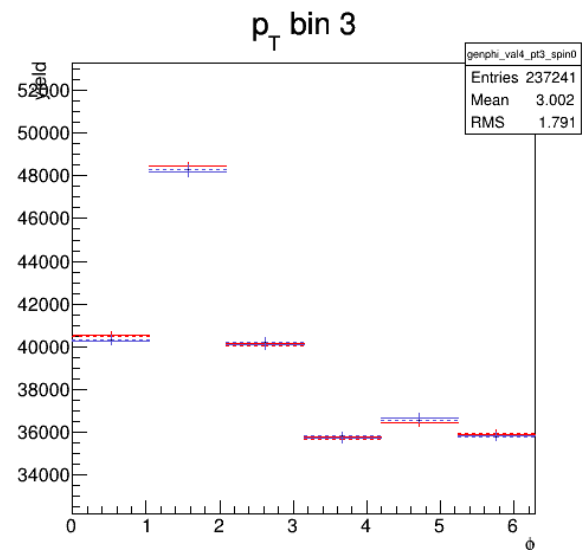
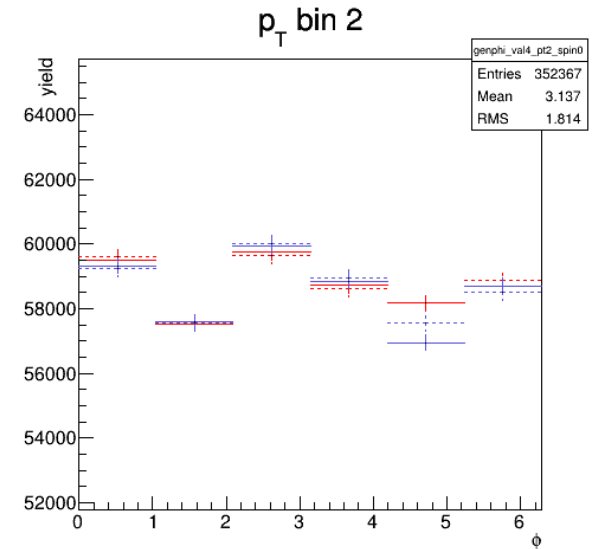
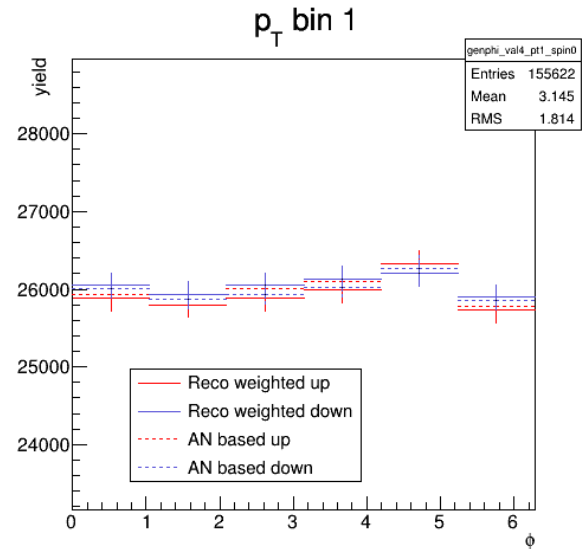
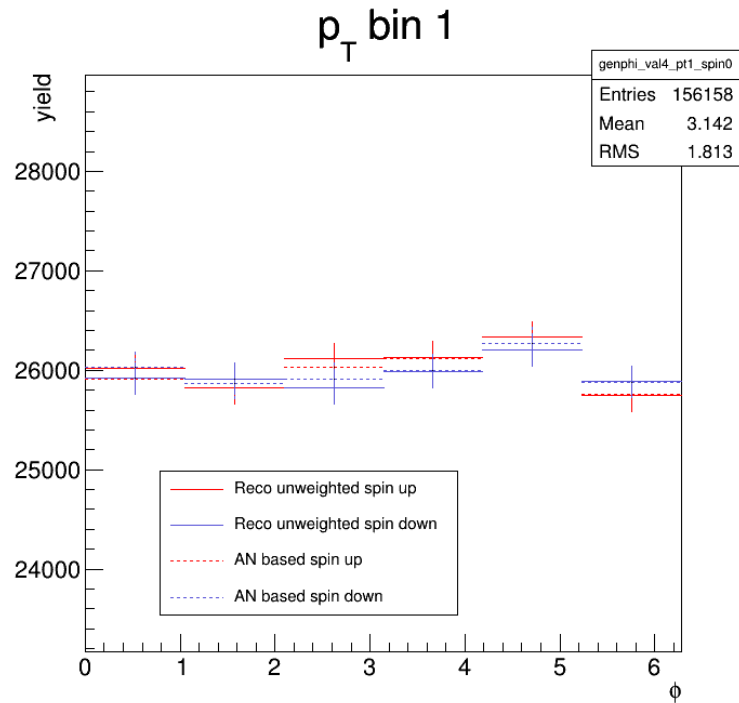


Magenta line: True distribution from dpmjet MC.

Solid black boxes: Unfolded distribution.

Unfolded distribution has been scaled to match the statistics between dpmjet and pythia.

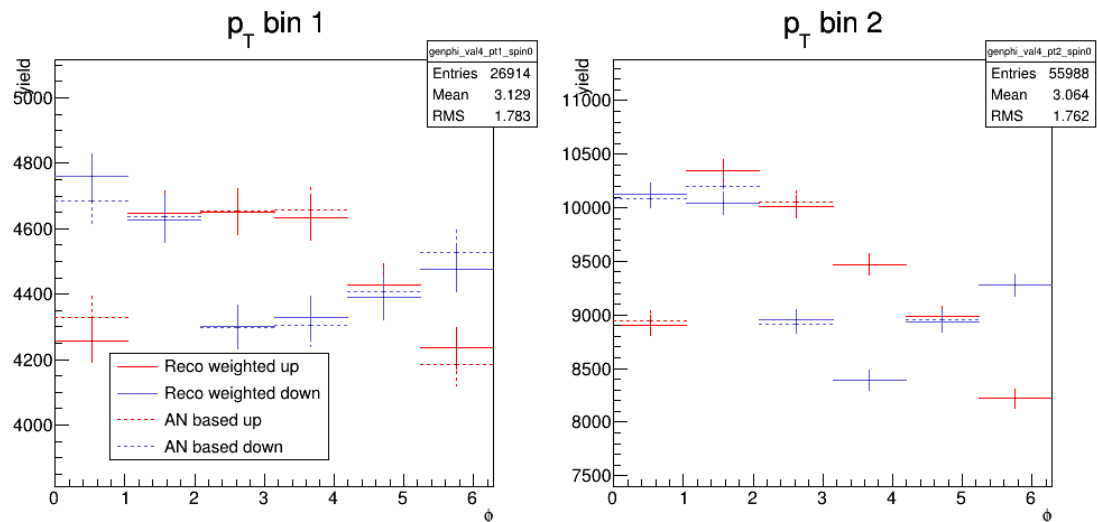
# OPE Monte Carlo ( Unweighted )



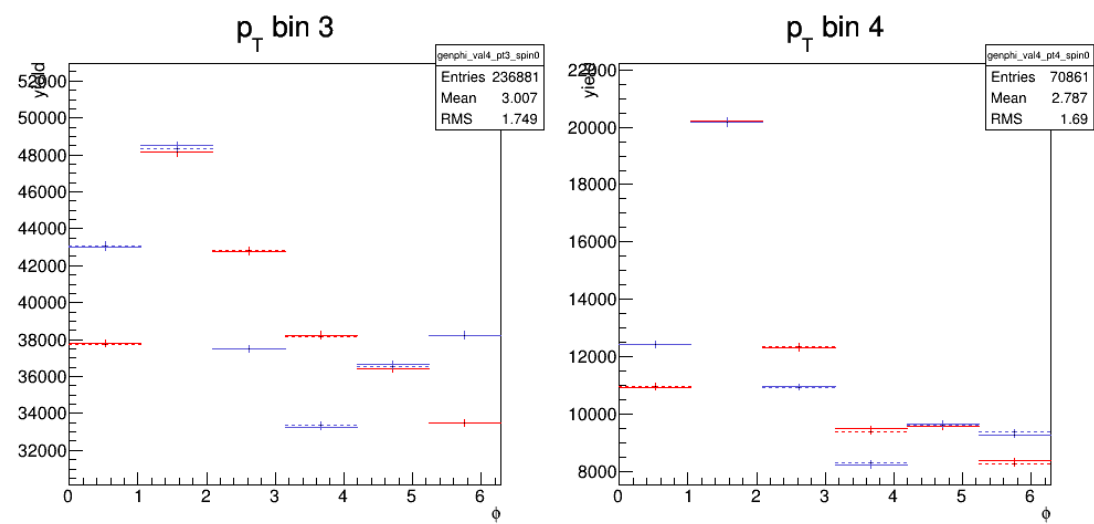
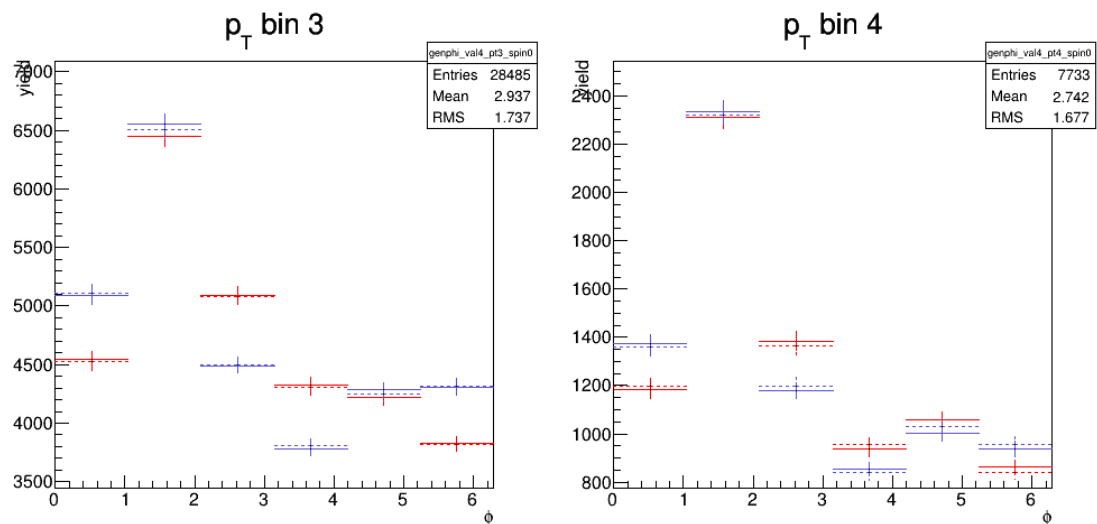
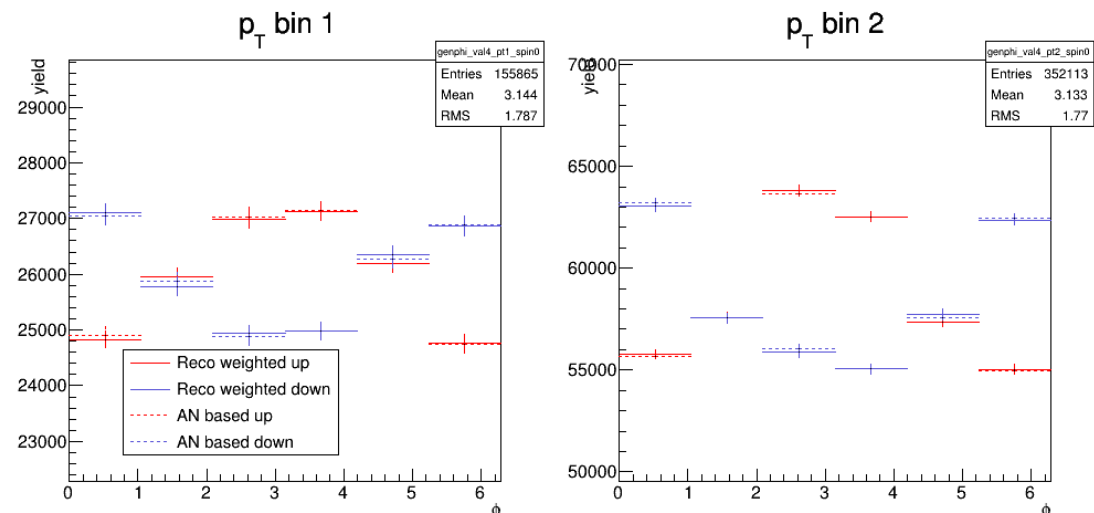
- Reconstructed azimuthal without weight
- Reconstructed azimuthal angle without weight
- Neutron asymmetry (A\_N) without weight
- Neutron asymmetry (A\_N) without weight

# Weighted Monte Carlo

## DPMJET

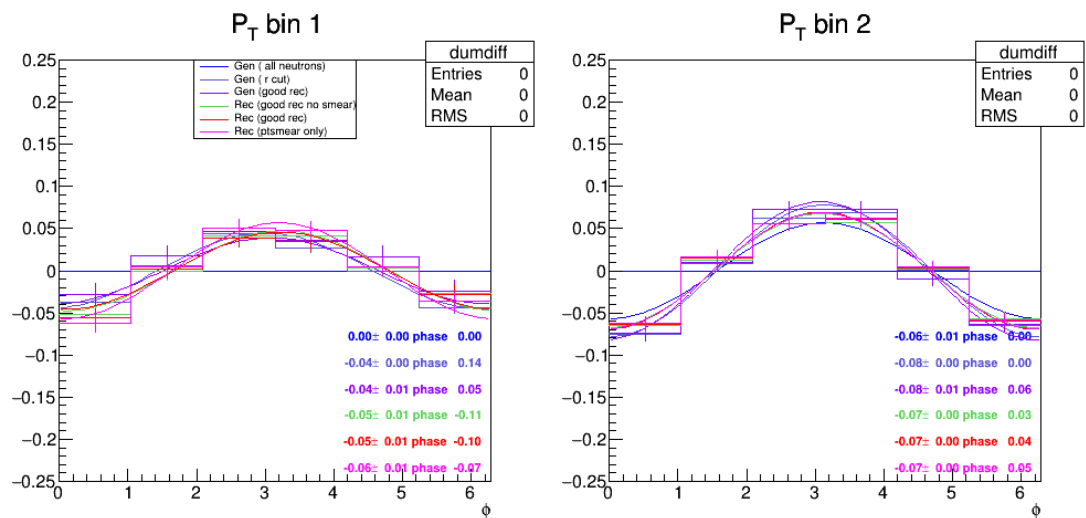


## NEWOPERCS



# Weighted Monte Carlo

## DPMJET



## NEWOPERCS

