

Multi-charmed hadron production in heavy ion collisions

2nd CENuM Workshop

July 4th, 2020
Virtual Workshop via Zoom



Sungtae Cho
Kangwon National University

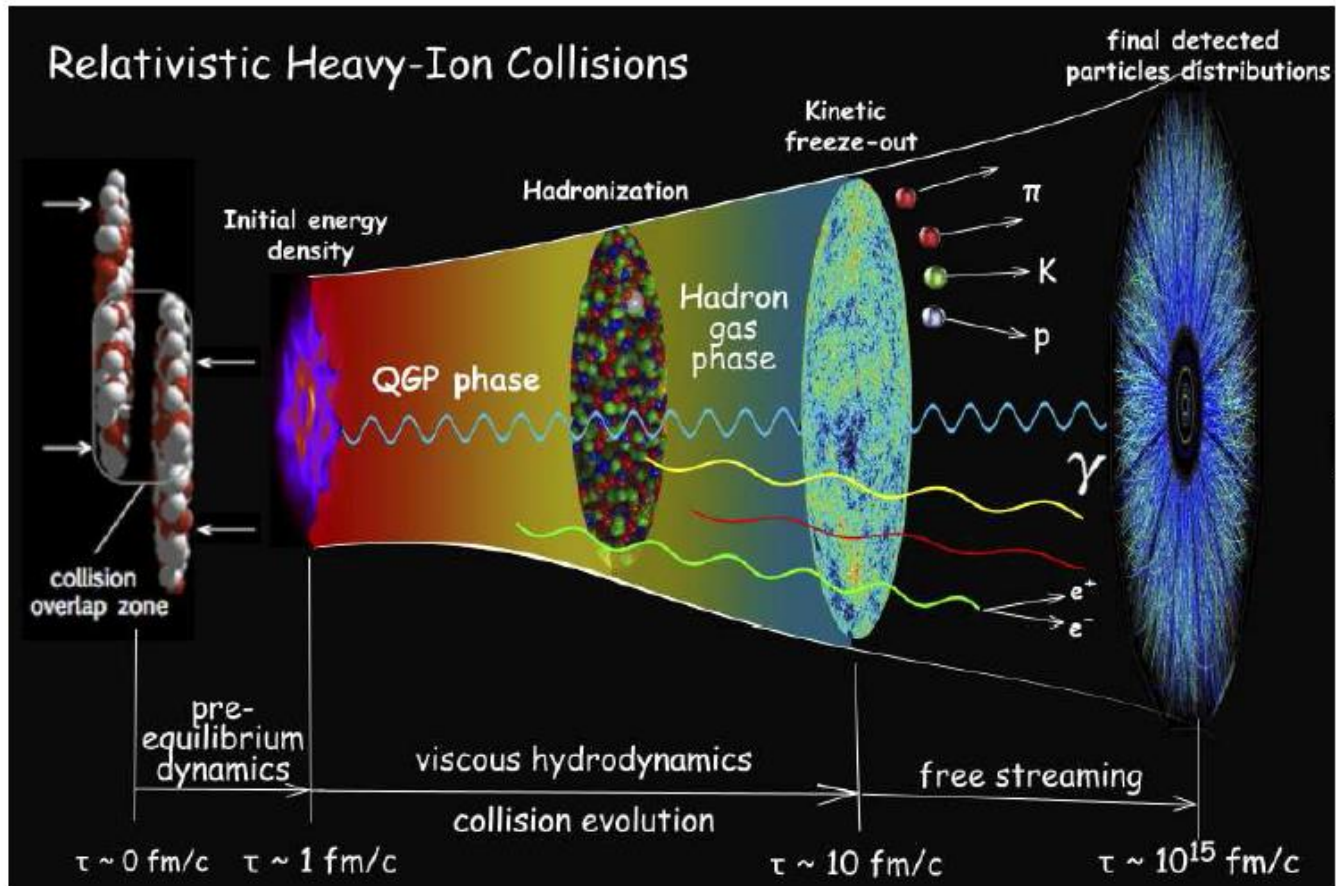
based on works in
Phys. Rev. C. **91**, 054914 (2015),
Phys. Rev. C. **101**, 024902 (2020),
Phys. Rev. C. **101**, 024909 (2020)

Outline

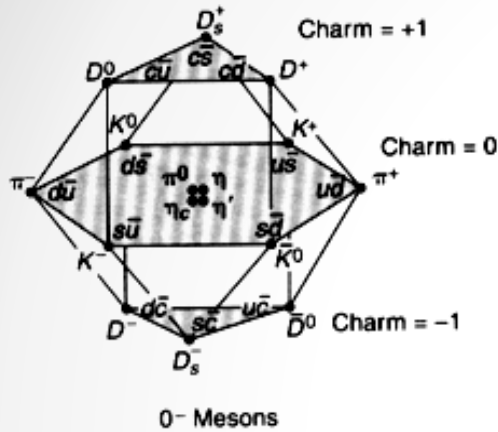
- Introduction
- Charmed hadrons in heavy ion collisions
- Multi-charmed Hadron production in heavy ion collisions
- Transverse momentum distribution of multi-charmed hadrons
- Conclusion

Introduction

– Relativistic heavy ion collisions

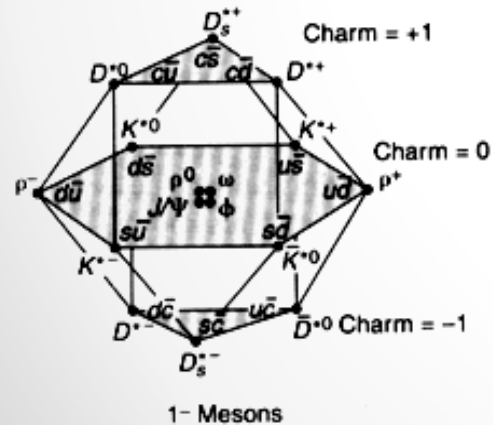


- Charmed hadrons, SU(4)

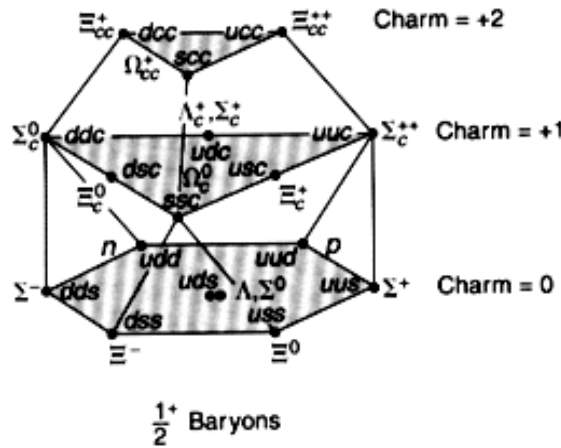


(a)

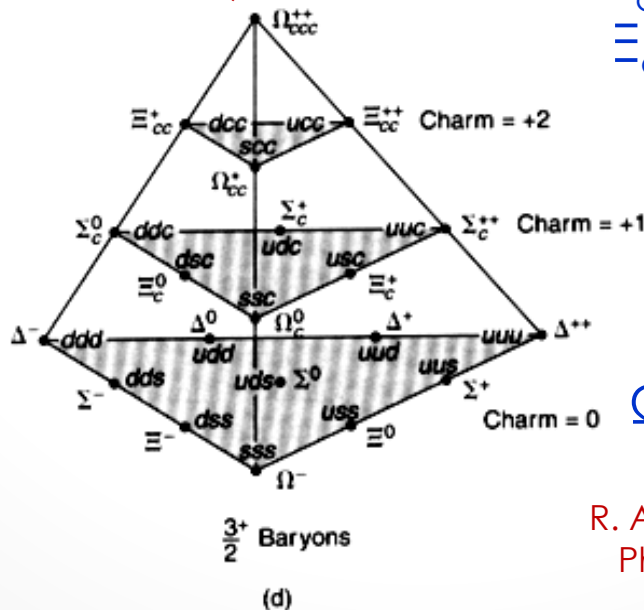
A. De Rújula, H. Georgi, And S. Glashaw,
 Phys. Rev. D **12**, 147 (1975)



(b)



(c)



(d)

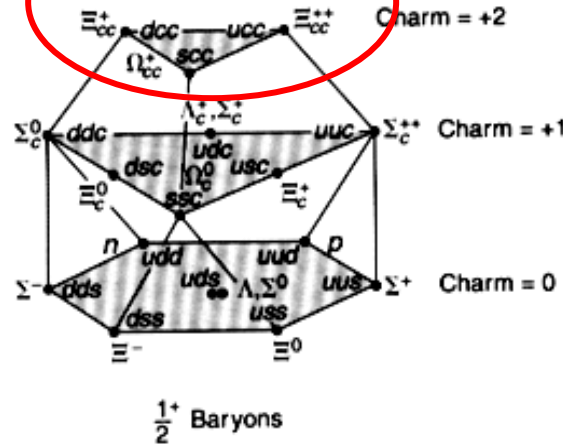
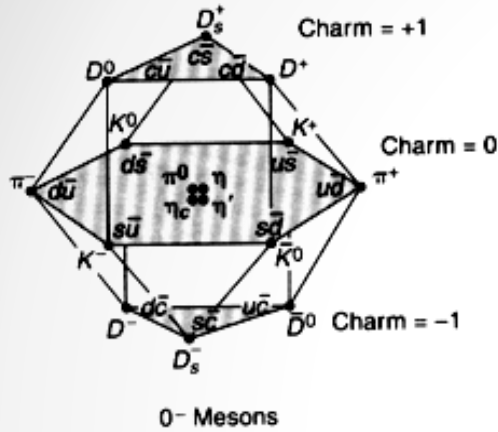
1) Charmonium states :
 $\eta_c, J/\psi, \chi_c, \psi'$

2) Charmed baryons and mesons : $D, D^*, D_s, D_s^*, \Lambda_c(2286), \Lambda_c(2595), \Lambda_c(2625), \Sigma_c(2455), \Sigma_c(2520), \Xi_c(2470), \Xi_c(2578), \Xi_c(2645), \Omega_c(2695), \Omega_c(2770)$

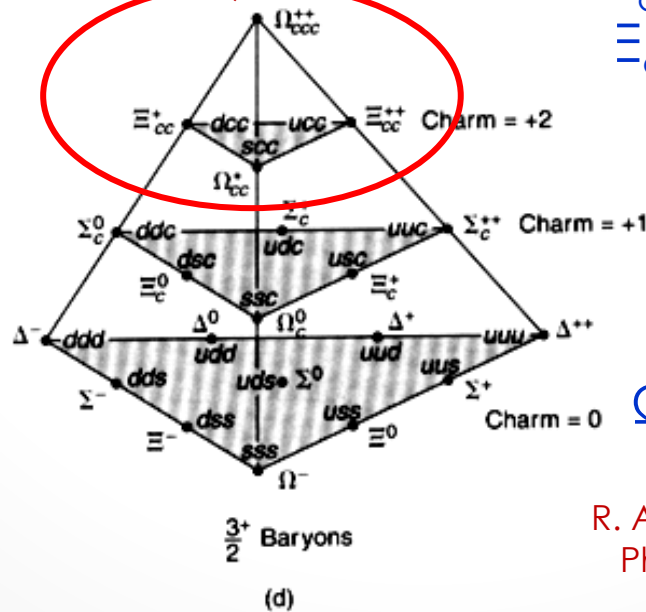
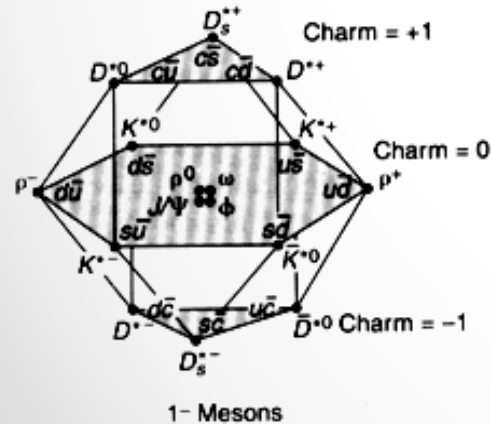
3) Doubly and triply charmed hadrons, exotic hadrons : $\Xi_{cc}^{\pm}, \Xi_{cc}^{*\pm}, \Omega_{cc}, \Omega_{cc}^*, \Omega_{ccc}, T_{cc}, X(3872)$

R. A. Briceno, H.-W. Lin, and D. R. Bolton,
 Phys. Rev. D **86** 094504 (2012)

- Charmed hadrons, SU(4)



A. De Rújula, H. Georgi, And S. Glashow,
 Phys. Rev. D **12**, 147 (1975)



1) Charmonium states : $\eta_c, J/\psi, \chi_c, \psi'$

2) Charmed baryons and mesons : $D, D^*, D_s, D_s^*, \Lambda_c(2286), \Lambda_c(2595), \Lambda_c(2625), \Sigma_c(2455), \Sigma_c(2520), \Xi_c(2470), \Xi_c(2578), \Xi_c(2645), \Omega_c(2695), \Omega_c(2770)$

3) Doubly and triply charmed hadrons, exotic hadrons : $\Xi_{cc}, \Xi_{cc}^*, \Omega_{cc}, \Omega_{cc}^*, \Omega_{ccc}, T_{cc}, X(3872)$

R. A. Briceno, H.-W. Lin, and D. R. Bolton,
 Phys. Rev. D **86** 094504 (2012)



– Recent measurements of a doubly charmed baryon in 2017

PRL **119**, 112001 (2017)

PHYSICAL REVIEW LETTERS

WOOK CHUNG
15 SEPTEMBER 2017



Observation of the Doubly Charmed Baryon Ξ_{cc}^{++}

R. Aaij *et al.**

(LHCb Collaboration)

(Received 6 July 2017; revised manuscript received 2 August 2017; published 11 September 2017)

– T_{cc} ($ccqq$) mesons

Particle	m [MeV]	(I, J^P)
T_{cc}^1	3797	$(0, 1^+)$

S. Cho *et al.* (EXHIC Collaboration), Phys. Rev. C **84**, 064910 (2011)

S. Cho *et al.* (EXHIC Collaboration), Prog. Part. Nucl. Phys. **95**, 279 (2017)

J. Hong, S. Cho, T. Song, and S-H. Lee, Phys. Rev. C **98**, 014913 (2018)

– $X(3872)$ mesons

$X(3872)$

$$I^G(J^{PC}) = 0^+(1^{++})$$

Mass $m = 3871.68 \pm 0.17$ MeV

$m_{X(3872)} - m_{J/\psi} = 775 \pm 4$ MeV

$m_{X(3872)} - m_{\psi(2S)}$

Full width $\Gamma < 1.2$ MeV, CL = 90%

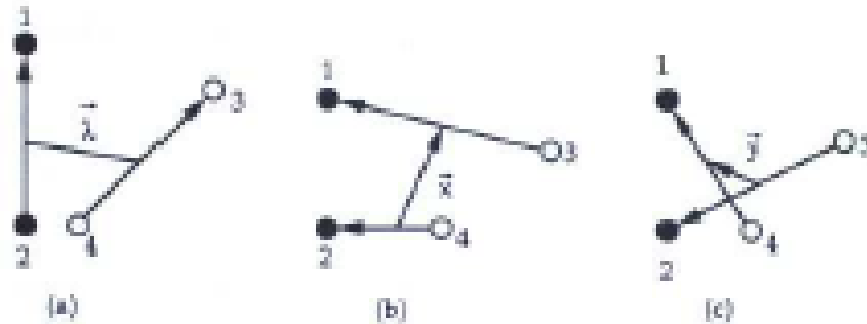
J. Beringer *et al.* (PDG), Phys. Rev. D **86**, 010001 (2012)

S.K. Choi *et al.* [Belle Collaboration], Phys. Rev. Lett. **90**, 242001 (2003)

- Internal structure of X(3872) mesons

1) Possible structures of X(3872) mesons, 3 independent relative coordinates

D. M. Brink and Fl. Stancu,
Phys. Rev. D 49, 4665 (1994)



2) The relative coordinates and momentum of X(3872) mesons

$$\vec{R} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + m_3 \vec{r}_3 + m_4 \vec{r}_4}{m_1 + m_2 + m_3 + m_4}$$

$$\vec{r}'_1 = \vec{r}_1 - \vec{r}_2$$

$$\vec{r}'_2 = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2}{m_1 + m_2} - \vec{r}_3$$

$$\vec{r}'_3 = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + m_3 \vec{r}_3}{m_1 + m_2 + m_3} - \vec{r}_4$$

$$\vec{k} = \vec{p}'_{lT} + \vec{p}'_{\bar{l}T} + \vec{p}'_{cT} + \vec{p}'_{\bar{c}T},$$

$$\vec{k}_1 = \frac{m_{\bar{l}} \vec{p}'_{lT} - m_l \vec{p}'_{\bar{l}T}}{m_l + m_{\bar{l}}},$$

$$\vec{k}_2 = \frac{m_c (\vec{p}'_{lT} + \vec{p}'_{\bar{l}T}) - (m_l + m_{\bar{l}}) \vec{p}'_{cT}}{m_l + m_{\bar{l}} + m_c},$$

$$\vec{k}_3 = \frac{m_{\bar{c}} (\vec{p}'_{lT} + \vec{p}'_{\bar{l}T} + \vec{p}'_{cT}) - (m_l + m_{\bar{l}} + m_c) \vec{p}'_{\bar{c}T}}{m_l + m_{\bar{l}} + m_c + m_{\bar{c}}} \quad (A2)$$

$$\vec{k} = \vec{p}'_{lT} + \vec{p}'_{\bar{l}T} + \vec{p}'_{cT} + \vec{p}'_{\bar{c}T},$$

$$\vec{k}_1 = \frac{m_{\bar{l}} \vec{p}'_{lT} - m_l \vec{p}'_{\bar{l}T}}{m_l + m_{\bar{l}}},$$

$$\vec{k}_2 = \frac{m_c \vec{p}'_{cT} - m_{\bar{c}} \vec{p}'_{\bar{c}T}}{m_c + m_{\bar{c}}},$$

$$\vec{k}_3 = \frac{(m_c + m_{\bar{c}}) (\vec{p}'_{lT} + \vec{p}'_{\bar{l}T}) - (m_l + m_{\bar{l}}) (\vec{p}'_{cT} + \vec{p}'_{\bar{c}T})}{m_l + m_{\bar{l}} + m_c + m_{\bar{c}}}, \quad \bullet 7$$

Physics Potential – some examples

- Heavy-flavor and quarkonia
 - Multiply Heavy Flavoured hadrons. e.g.: Ξ_{cc} , Ω_{cc} , Ω_{ccc}
 - $\chi_{c1,2}$ states
 - Ultimate precision on B mesons at low p_T
 - X, Y, Z charmonium-like states (e.g. X(3872))
- Low-mass dielectrons
 - Precision measurement of the thermal dilepton continuum, $0 < m < 3\text{GeV}$
- Real soft photons
 - down to 50MeV/c
- Real ultra-soft photons
 - Very low p_T photons: $1\text{MeV}/c < p_T^\gamma < 100\text{MeV}/c$
 - dedicated small forward spectrometer at $3.5 < |\eta| < 5$



Hadron formation from deconfined QGP



Chiral symmetry restoration ρ -a1 sector



QGP Radiation uncharted phase space region



Test of soft theorems

L. Musa (CERN), Strangeness in Quark Matter 2019, Bari, June 10-15

Parallel Session - Heavy flavor IV (16:20-18:00)

-Conveners: Tserruya, Itzhak (Weizmann Institute of Science (IL))

time	[id] title	presenter
17:20	[232] LHCb measurements of the exotic tetraquark candidate X(3872) in high multiplicity pp and pPb collisions	DURHAM FOR THE LHCb COLLABORATION, John Matthew (Los Alamos National Laboratory)
17:40	[517] Observation of X(3872) in PbPb collisions with the CMS detector	LEE FOR THE CMS COLLABORATION, Yen-Jie (Massachusetts Inst. of Technology (US))

Ratio of X(3872) to $\psi(2S)$ Yields in pp and PbPb

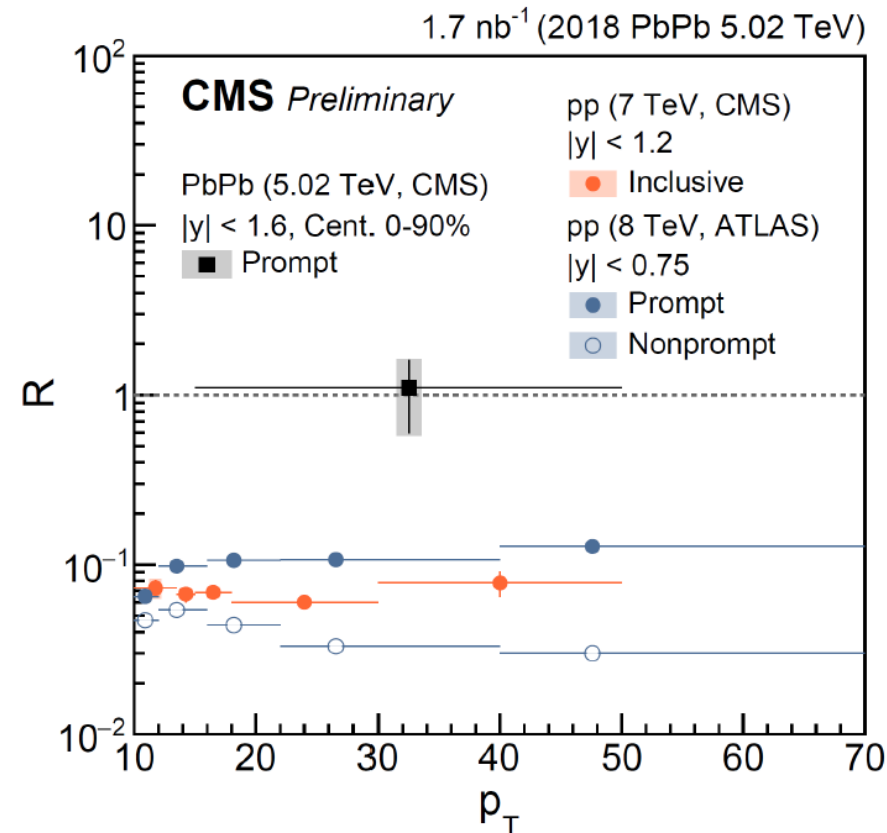
$$R = N_{X(3872)}^{(\text{Corr})} / N_{\psi(2S)}^{(\text{Corr})}$$

In PbPb collisions:

$$R = 1.10 \pm 0.51 \text{ (stat.)} \pm 0.53 \text{ (syst.)}$$

Indication of R enhancement in PbPb collisions with respect to pp at 7 and 8 TeV

CMS-PAS-HIN-19-005



Yen-jie Lee (MIT), Quark Matter 2019, Wuhan, November 4-9

– Recent publications on X(3872) mesons

Deciphering the nature of X(3872) in heavy ion collisions

Hui Zhang,^{1,*} Jinfeng Liao,^{2,†} Enke Wang,^{1,‡} Qian Wang,^{1,3,§} and Hongxi Xing^{1,¶}

¹*Guangdong Provincial Key Laboratory of Nuclear Science,
Institute of Quantum Matter, South China Normal University, Guangzhou 510006, China*

²*Physics Department and Center for Exploration of Energy and Matter,
Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA*

³*Theoretical Physics Center for Science Facilities,
Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China*

X(3872) Transport in Heavy-Ion Collisions

Biaogang Wu,¹ Xiaojian Du,² Matthew Sibila,³ and Ralf Rapp¹

¹*Cyclotron Institute and Department of Physics and Astronomy,
Texas A&M University, College Station, TX 77843-3366, USA*

²*Fakultät für Physik, Universität Bielefeld, D-33615 Bielefeld, Germany*

³*Department of Physics & Astronomy, Ohio Northern University, Ada, OH 45810, USA*

(Dated: June 18, 2020)

The nature of X(3872) from high-multiplicity pp collisions

Angelo Esposito,¹ Elena G. Ferreira,² Alessandro Pilloni,^{3,4} Antonio D. Polosa,⁵ and Carlos A. Salgado²

¹*Theoretical Particle Physics Laboratory (LPTP),
Institute of Physics, EPFL, 1015 Lausanne, Switzerland*

²*Instituto Galego de Física de Altas Enerxías – IGFAE,
Universidade de Santiago de Compostela, E-15782 Santiago de Compostela, Galicia-Spain*

³*European Centre for Theoretical Studies in Nuclear Physics and related Areas
(ECT*) and Fondazione Bruno Kessler, Villazzano (Trento), I-38123, Italy*

⁴*INFN Sezione di Genova, Genova, I-16146, Italy*

⁵*Dipartimento di Fisica and INFN, Sapienza Università di Roma, Piazzale Aldo Moro 2, I-00185 Roma, Italy*

Charmed hadrons in heavy ion collisions

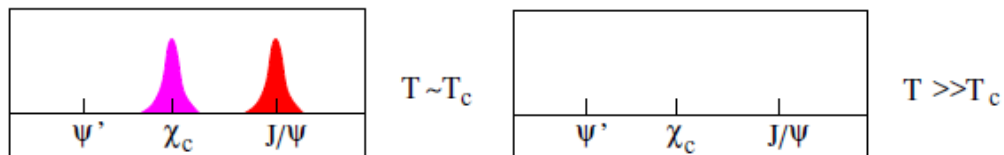
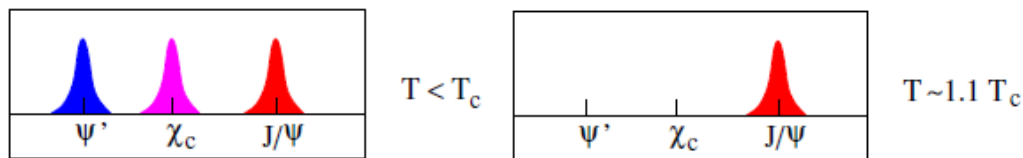
– Charmonium states

T. Matsui and H. Satz, Phys. Lett. B **178** 416 (1986)

1) J/ψ suppression and Debye screening

At $T > T_c$ color charges are Debye screened in QGP, and the Debye screening prevents the formation of the bound states

2) The different charmonium states melt sequentially as a function of their binding strength;
the most loosely bound state disappears first, the ground state last



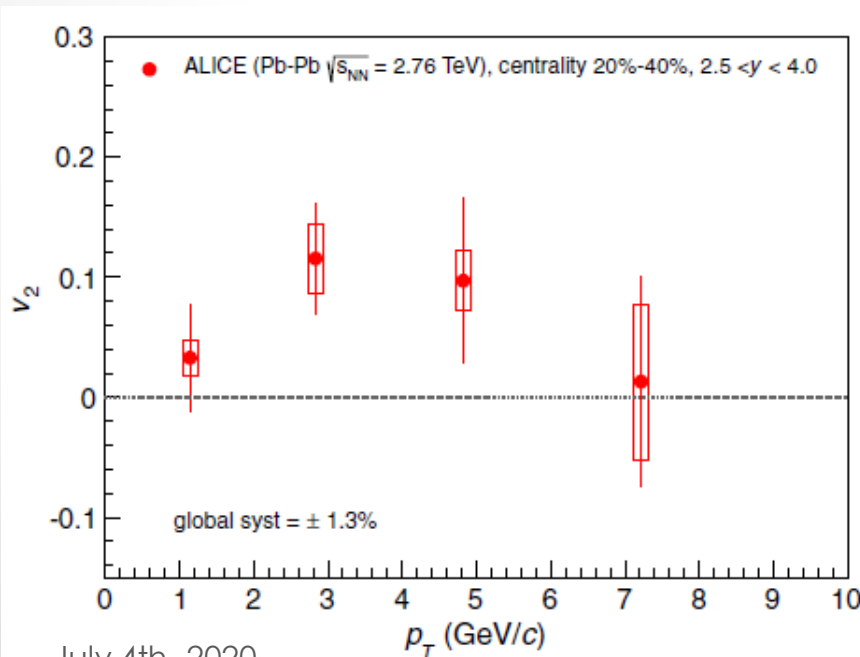
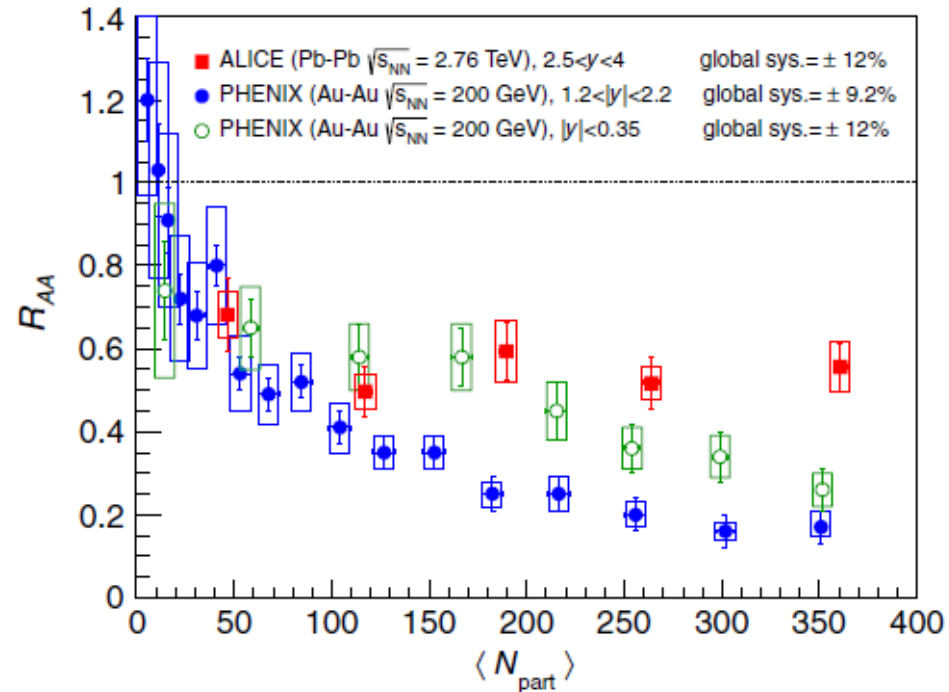
H. Satz, J. Phys. G.
32, R25 (2006)

$T \gg T_c$ 2nd CENuM Workshop • 11

– Regeneration of J/ψ mesons

1) The nuclear modification factor of J/ψ mesons

B. Abelev et al, (ALICE Collaboration),
Phys. Rev. Lett. **109**, 072301



2) Elliptic flows, v₂ of the J/ψ

E. Abbas et al, Phys. Rev. Lett. **111**, 162301 (2013)

Multi-charmed hadron production in heavy ion collisions



– Yields of hadrons in the coalescence model

V. Greco, C. M. Ko, and P. Levai, Phys. Rev. C **68**, 034904 (2003)

R. J. Freis, B. Muller, C. Nonaka, and S. Bass, Phys. Rev. C **68**, 044902 (2003)

$$N^{Coal} = g \int \left[\prod_{i=1}^n \frac{1}{g_i} \frac{p_i \cdot d\sigma_i}{(2\pi)^3} \frac{d^3 p_i}{E_i} f(x_i, p_i) \right] f^W(x_1, \dots, x_n : p_1, \dots, p_n)$$

1) The Wigner function, the coalescence probability function

$$\begin{aligned} f^W(x_1, \dots, x_n : p_1, \dots, p_n) \\ = \int \prod_{i=1}^n dy_i e^{p_i y_i} \psi^* \left(x_1 + \frac{y_1}{2}, \dots, x_n + \frac{y_n}{2} \right) \psi \left(x_1 - \frac{y_1}{2}, \dots, x_n - \frac{y_n}{2} \right) \end{aligned}$$

2) A Lorentz-invariant phase space integration of a space-like hyper-surface constraints the number of particles in the system

$$\int p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3 E_i} f(x_i, p_i) = N_i$$

– Hadron production by recombination

: Transverse momentum distributions of hadron yields

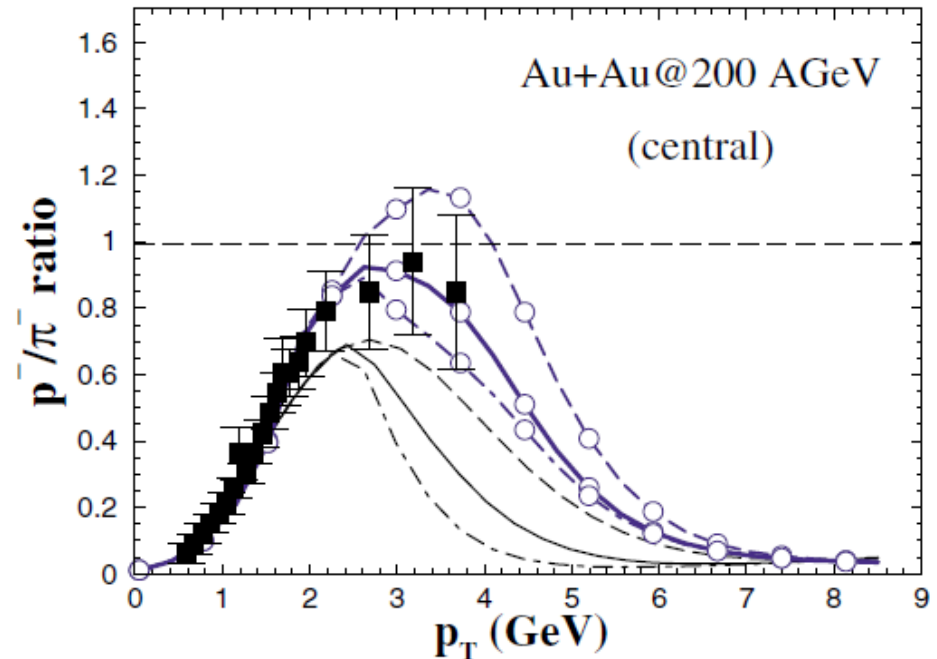
1) The puzzle in antiproton/pion ratio

V. Greco, C. M. Ko, and P. Levai, Phys. Rev. Lett. **90**, 202302 (2003)

R. J. Freis, B. Muller, C. Nonaka, and S. Bass, Phys. Rev. Lett. **90**, 202303 (2003)

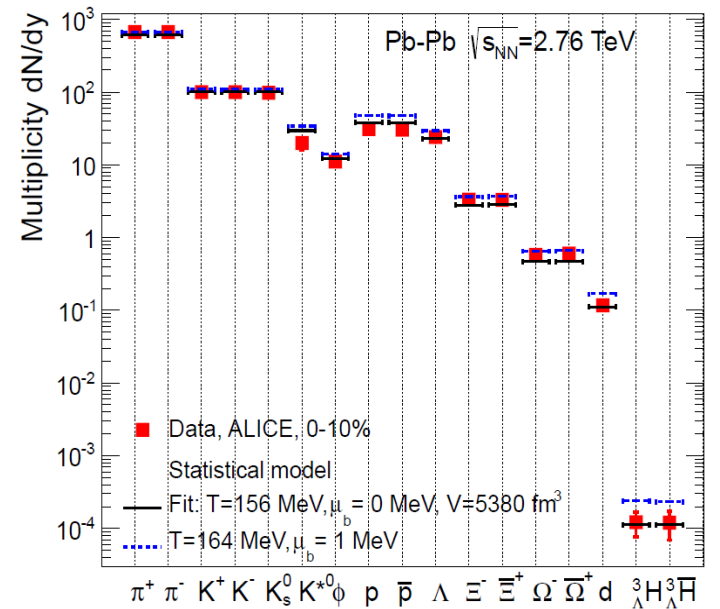
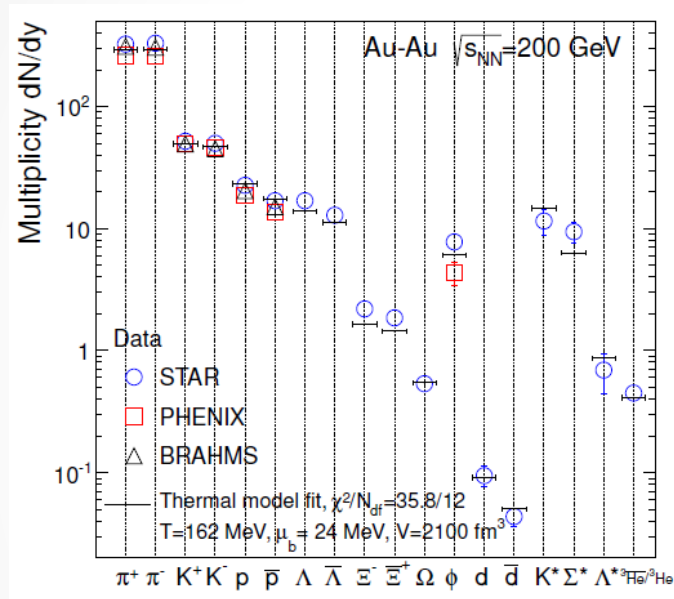
originated from a competition between two particle production mechanisms

: A fragmentation dominates at large transverse momenta and a coalescence prevails at lower transverse momenta



– Multi-charmed hadron production

1) Yields in the statistical hadronization model



A. Andronic, P. Braun-Munzinger, K. Redlich and J. Stachel, Nucl. Phys. A **904-905**, 535c (2013)

J. Stachel, A. Andronic, P. Braun-Munzinger, and K. Redlich, J. Phys. Conf. Ser. **509**, 012019 (2014)

S. Cho and S. H. Lee, Phys. Rev. C **101**, 024902 (2020)

	RHIC		LHC			RHIC		LHC	
	Stat.	Coal.	Stat.	Coal.		Stat.	Coal.	Stat.	Coal.
Ξ_{cc}	1.0×10^{-2}	1.3×10^{-3}	2.8×10^{-2}	4.9×10^{-3}	Ω_{ccc}	1.1×10^{-4}	1.1×10^{-6}	4.0×10^{-4}	5.3×10^{-6}
Ξ_{cc}^*	6.4×10^{-3}	9.0×10^{-4}	1.8×10^{-2}	3.3×10^{-3}	T_{cc}	8.9×10^{-4}	5.3×10^{-5}	2.7×10^{-3}	1.3×10^{-4}
Ω_{scc}	2.8×10^{-3}	2.5×10^{-4}	8.0×10^{-3}	9.0×10^{-4}	X_2	5.7×10^{-4}	5.6×10^{-4}	1.7×10^{-3}	1.7×10^{-3}
Ω_{scc}^*	1.5×10^{-3}	1.6×10^{-4}	4.3×10^{-3}	6.0×10^{-4}	X_4	5.7×10^{-4}	5.3×10^{-5}	1.7×10^{-3}	1.3×10^{-4}

Transverse momentum distributions of multi-charmed hadrons



S. Cho and S. H. Lee, Phys. Rev. C **101**, 024902 (2020)

1) Multi-charmed hadron Yields in the coalescence model

$$N_{\Xi_{cc}} = g_{\Xi_{cc}} \int p_l \cdot d\sigma_l p_{c_1} \cdot d\sigma_{c_1} p_{c_2} \cdot d\sigma_{c_2} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{c_1}}{(2\pi)^3 E_{c_1}} \frac{d^3 \vec{p}_{c_2}}{(2\pi)^3 E_{c_2}} f_l(r_l, p_l) f_{c_1}(r_{c_1}, p_{c_1})$$

$$\times f_{c_2}(r_{c_2}, p_{c_2}) W_{\Xi_{cc}}(r_l, r_{c_1}, r_{c_2}; p_l, p_{c_1}, p_{c_2})$$

$$N_X = g_X \int p_l \cdot d\sigma_l p_{\bar{l}} \cdot d\sigma_{\bar{l}} p_c \cdot d\sigma_c p_{\bar{c}} \cdot d\sigma_{\bar{c}} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{\bar{l}}}{(2\pi)^3 E_{\bar{l}}} \frac{d^3 \vec{p}_c}{(2\pi)^3 E_c} \frac{d^3 \vec{p}_{\bar{c}}}{(2\pi)^3 E_{\bar{c}}}$$

$$\times f_l(r_l, p_l) f_{\bar{l}}(r_{\bar{l}}, p_{\bar{l}}) f_c(r_c, p_c) f_{\bar{c}}(r_{\bar{c}}, p_{\bar{c}}) W_X(r_l, r_{\bar{l}}, r_c, r_{\bar{c}}; p_l, p_{\bar{l}}, p_c, p_{\bar{c}})$$

2) Transverse momentum distributions

$$\frac{d^2 N_{\Xi_{cc}}}{d^2 \vec{p}_T} = \frac{g_{\Xi_{cc}}}{V^2} \int d^3 \vec{r}_1 d^3 \vec{r}_2 d^2 \vec{p}_{lT} d^2 \vec{p}_{c_1T} d^2 \vec{p}_{c_2T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{c_1T} - \vec{p}_{c_2T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}}$$

$$\times \frac{d^2 N_{c_1}}{d^2 \vec{p}_{c_1T}} \frac{d^2 N_{c_2}}{d^2 \vec{p}_{c_2T}} W_{\Xi_{cc}}(\vec{r}'_1, \vec{r}'_2, \vec{r}'_3, \vec{k}_1, \vec{k}_2, \vec{k}_3),$$

$$\frac{d^2 N_X}{d^2 \vec{p}_T} = \frac{g_X}{V^3} \int d^3 \vec{r}_1 d^3 \vec{r}_2 d^3 \vec{r}_3 d^2 \vec{p}_{lT} d^2 \vec{p}_{\bar{l}T} d^2 \vec{p}_{cT} d^2 \vec{p}_{\bar{c}T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{\bar{l}T} - \vec{p}_{cT} - \vec{p}_{\bar{c}T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}} \frac{d^2 N_{\bar{l}}}{d^2 \vec{p}_{\bar{l}T}}$$

$$\times \frac{d^2 N_c}{d^2 \vec{p}_{cT}} \frac{d^2 N_{\bar{c}}}{d^2 \vec{p}_{\bar{c}T}} W_X(\vec{r}'_1, \vec{r}'_2, \vec{r}'_3, \vec{k}_1, \vec{k}_2, \vec{k}_3)$$

3) Transverse momentum distributions of charm and light quarks

$$\frac{dN_c}{d^2p_T} = \begin{cases} a_0 \exp[-a_1 p_T^{a_2}] & p_T \leq p_0 \\ a_0 \exp[-a_1 p_T^{a_2}] + a_3(1 + p_T^{a_4})^{-a_5} & p_T \geq p_0 \end{cases}$$

$$\frac{d^2N_l}{d^2p_T} = g_l \frac{V}{(2\pi)^3} m_T e^{-m_T/T_{eff}},$$

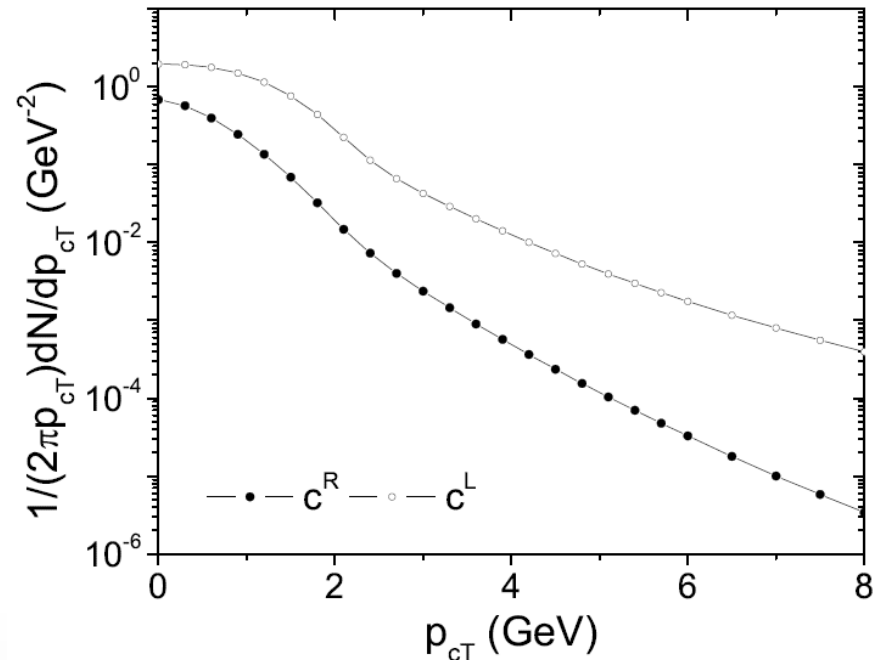
	a_0	a_1	a_2	a_3	a_4	a_5
RHIC						
$p_T \leq p_0$	0.69	1.22	1.57			
$p_T \geq p_0$	1.08	3.04	0.71	3.79	2.02	3.48
LHC						
$p_T \leq p_0$	1.97	0.35	2.47			
$p_T \geq p_0$	7.95	3.49	3.59	87335	0.5	14.31

S. Plumari, V. Minissale, S. K. Das, G. Coci and V. Greco, Eur. Phys. J. C **78**:348 (2017)

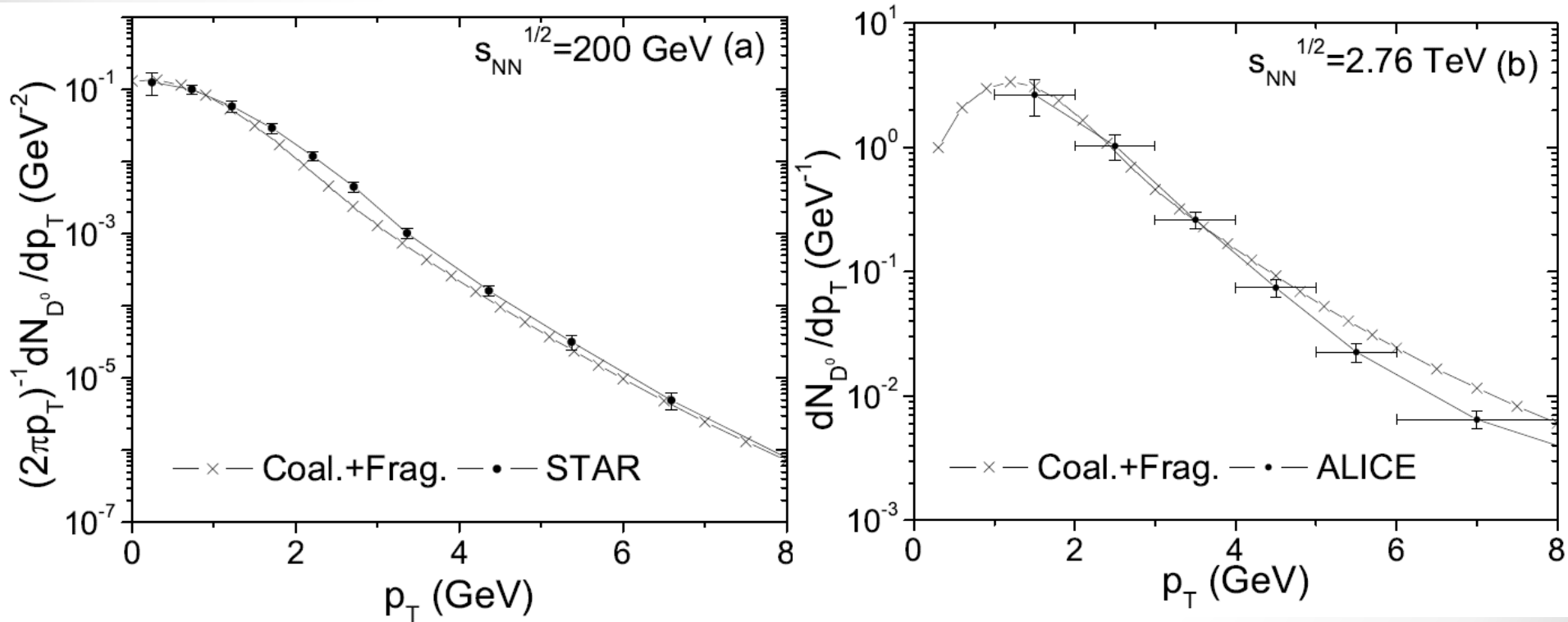
Y. Oh, C. M. Ko, S.-H. Lee, and S. Yasui, Phys. Rev. C **79** 044905 (2009)

S. Cho *et al.* (EXHIC Collaboration), Prog. Part. Nucl. Phys. **95**, 279 (2017)

	RHIC		LHC (2.76 TeV)	
	Sc. 1	Sc. 2	Sc. 1	Sc. 2
T_H (MeV)		162		156
V_H (fm ³)		2100		5380
μ_B (MeV)		24		0
μ_s (MeV)		10		0
γ_c				39
γ_b		4.0×10^7		8.6×10^8
T_C (MeV)	162	166	156	166
V_C (fm ³)	2100	1791	5380	3533
$N_u = N_d$	320	302	700	593
$N_s = N_{\bar{s}}$	183	176	386	347
$N_c = N_{\bar{c}}$		4.1		11
$N_b = N_{\bar{b}}$		0.03		0.44



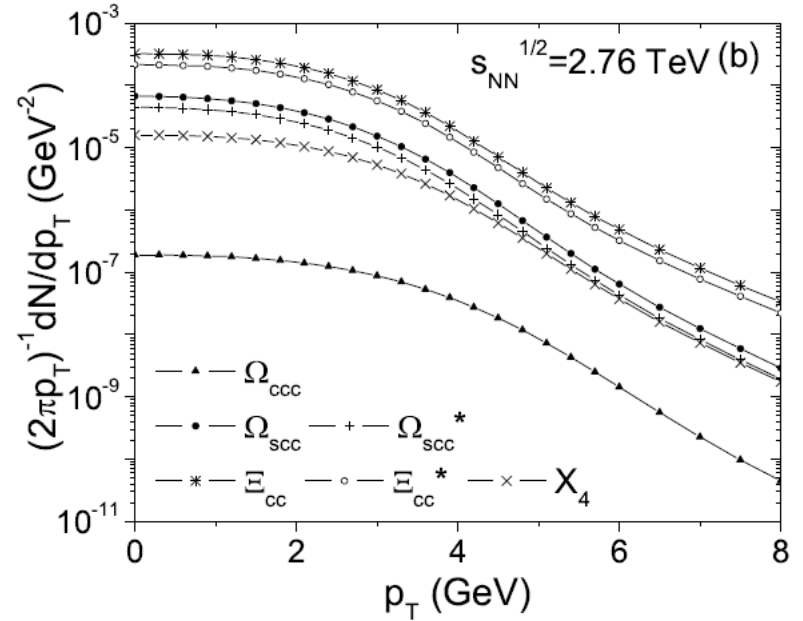
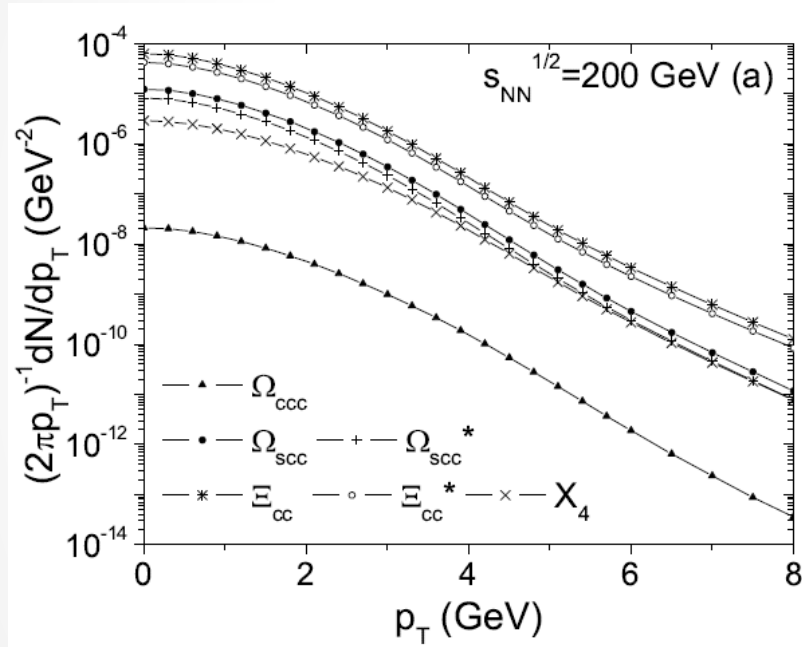
4) Transverse momentum distributions of D^0 mesons



J. Adam et al. [STAR Collaboration], Phys. Rev. C **99**, no. 3, 034908 (2019).

J. Adam et al. [ALICE Collaboration], JHEP **1603**, 081 (2016).

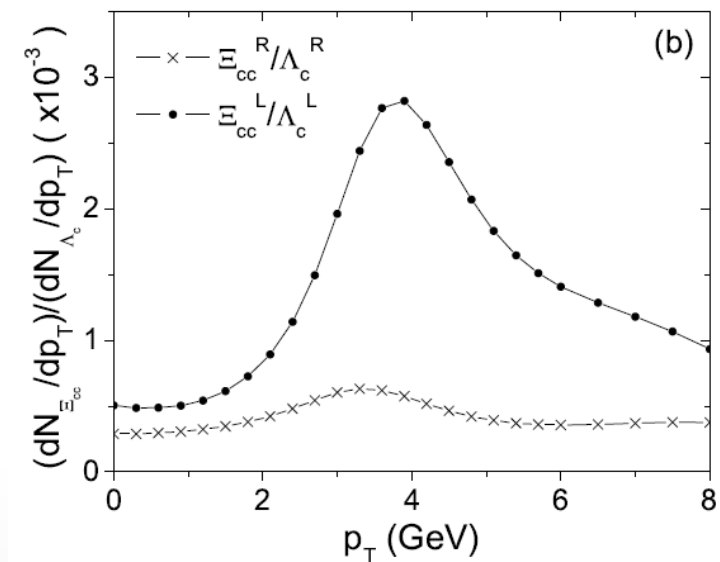
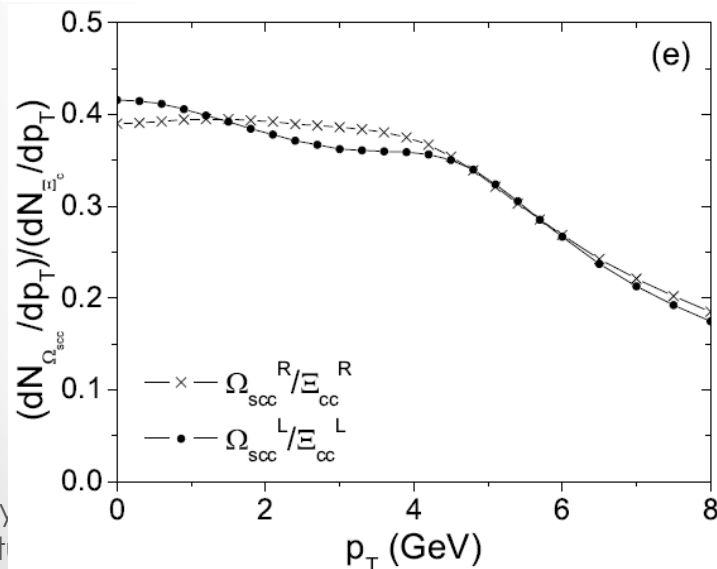
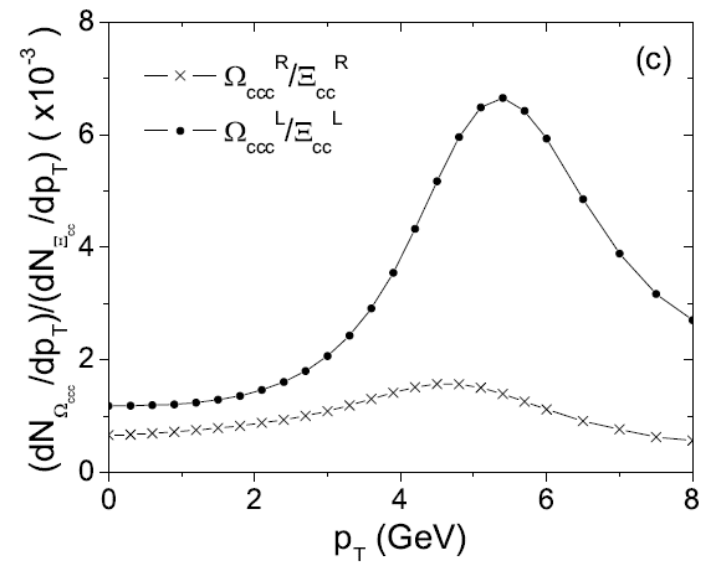
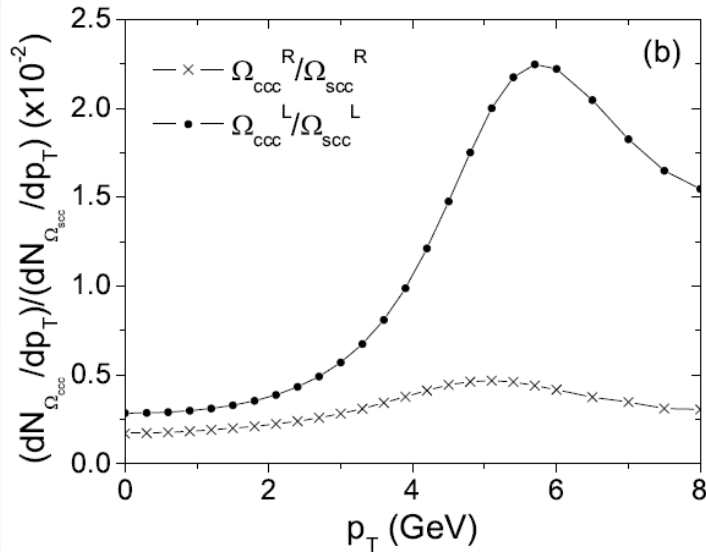
5) Transverse momentum distributions of multi-charmed hadrons



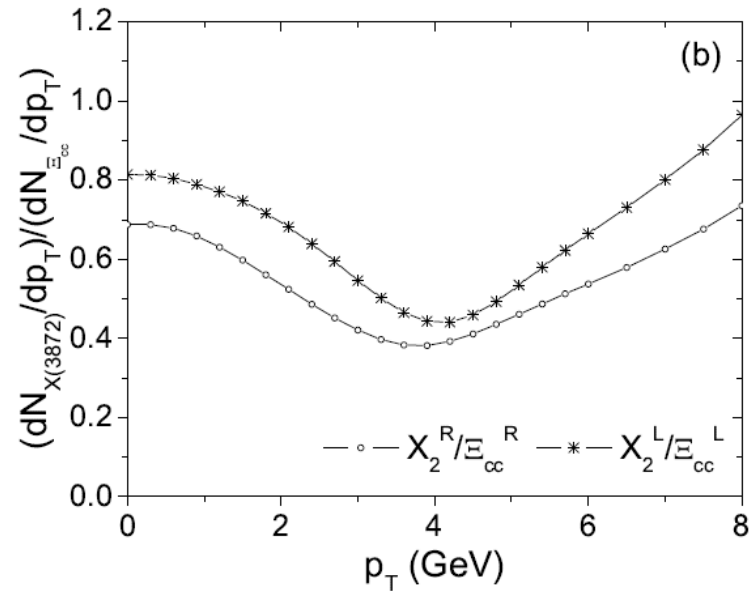
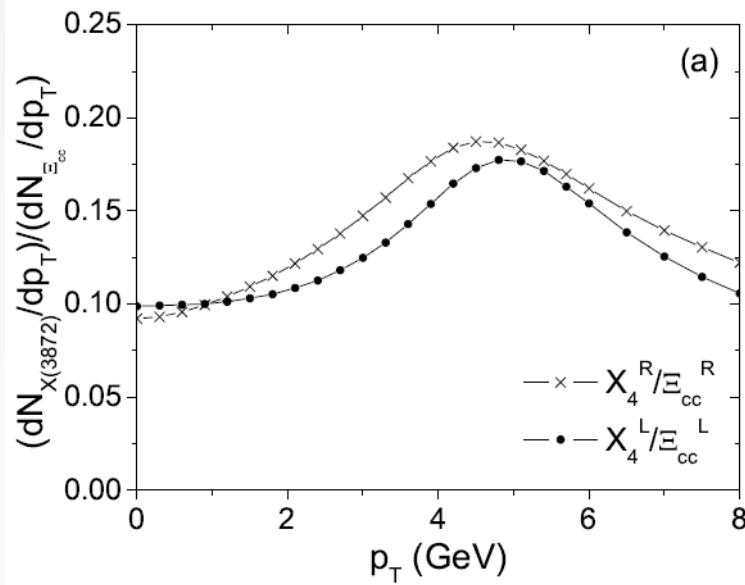
	RHIC	LHC
Ξ_{cc}	4.4×10^{-4}	6.7×10^{-3}
Ξ_{cc}^*	2.9×10^{-4}	4.5×10^{-3}
Ω_{scc}	8.6×10^{-5}	1.3×10^{-3}
Ω_{scc}^*	5.7×10^{-5}	8.5×10^{-4}
Ω_{ccc}	1.7×10^{-7}	5.9×10^{-6}
T_{cc}	2.2×10^{-5}	3.8×10^{-4}
X_4	2.4×10^{-5}	3.8×10^{-4}
X_2	2.6×10^{-4}	4.5×10^{-3}
D^0	0.71	6.0
Λ_c	0.63	4.0

6) Transverse momentum distribution ratios

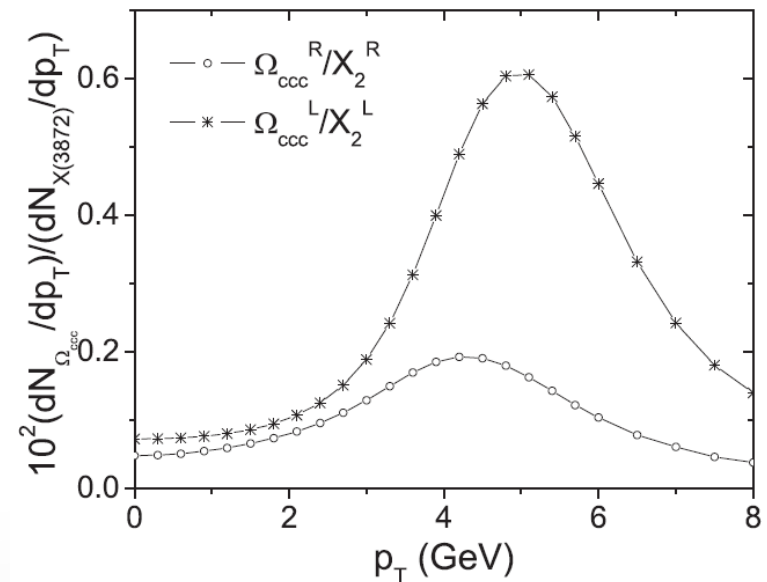
a) Baryon/baryon (ccc/ccq, ccc/ccs, ccq/ccs, and ccq/ccq)



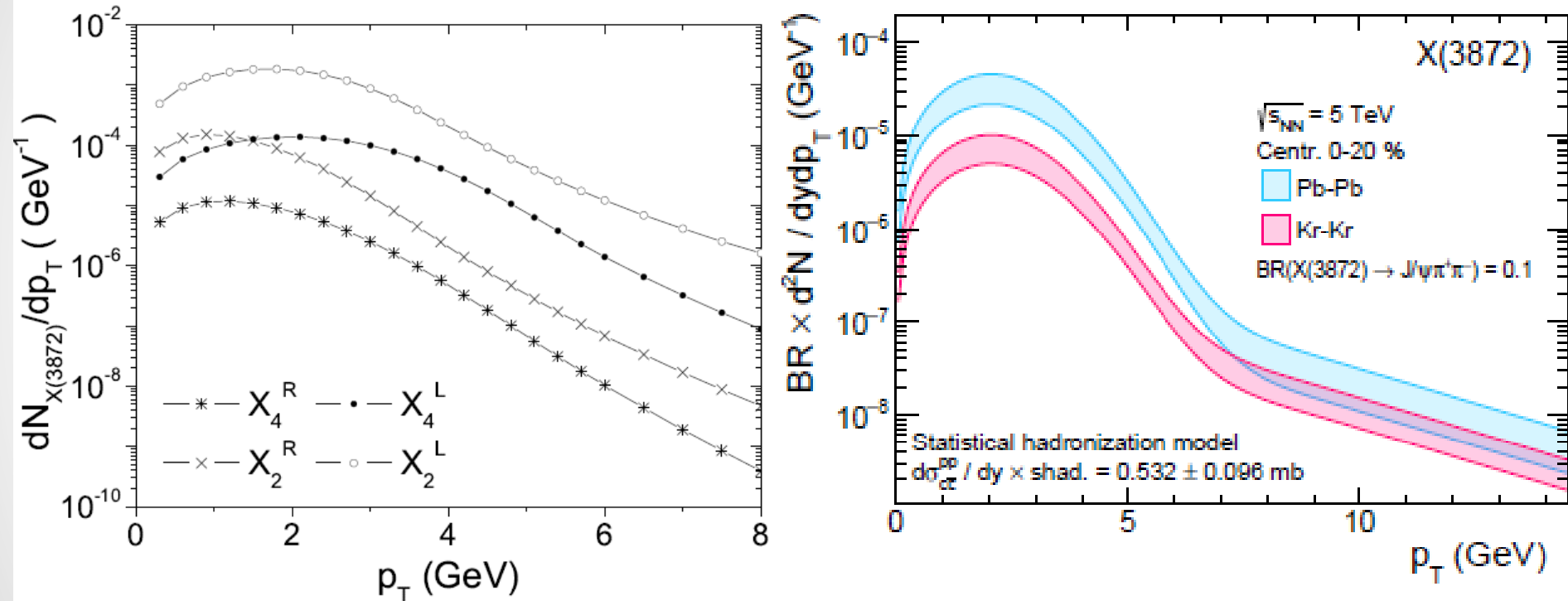
b) Meson/baryon (ccqq/ccq, or cc/ccq)



c) Baryon/meson (ccc/cc)



– Comparison with results from the statistical hadronization model



A. Andronic, P. Braun-Munzinger, M. K. Kohler, K. Redlich and J. Stachel, Phys. Lett. B **797**, 134836 (2019).

Conclusion

– Multi-charmed hadron production in heavy ion collisions

- 1) Heavy ion collision experiments provide excellent chances to study production of multi-charm hadrons as well as exotic hadrons
- 2) Transverse momentum distributions of charmed hadrons are directly affected by not only those of charm and light quarks but also numbers of constituent quarks.
- 3) Transverse momentum distribution ratios between multi-charm hadrons and $X(3872)$ mesons, or other combinations between heavy quark hadrons reflect the distribution of momentum among constituent quarks
- 4) Investigation on transverse momentum distribution of various charmed hadrons as well as those ratios can give us useful information on the properties of quark-gluon plasma



Thank you for your attention!