CENuM-RULiC Joint Workshop on Extreme Nuclear States and Reactions November 1, 2019

Search for tetra- and tri-neutron resonance states

~ Three-nucleon force study with a personal recollection ~

> Hideyuku Sakai RIKEN Nishina Center



Contents

- 1. Three-body force in nuclear system
- 2. Looking for 3BF (3NF)
- 3. Tetraneutron search
- 4. Trineutron search
- 5. 4NF
- 6. Small suggestion
- 7. Summary

Three-body force in Nuclear system

How to identify 3NF?



First modern three-nucleon force (3NF)



FM were too early to verify their 3NF, experimentally.
 Correct QM Schrodinger eq. for 3BS (Faddeev eq. 1961)
 2NF was not yet established (established around 1990.)

Note: To solve Faddeev eq. super CPU is needed (be available at late 1980)

Various 3NFs (operator form)

$a^2 \vec{\sigma} \cdot \vec{\sigma} \cdot \vec{\sigma}$						
$V^{(j)}_{ m 3NF} \;=\; rac{g^2}{4m_N^2} rac{\sigma_i \cdot q}{q^2 + m_\pi^2} rac{\sigma_k \cdot q}{q'^2 + m_\pi^2} \; F^2_{\pi NN}(q^2) \; F^2_{\pi NN}(q'^2) \;$		3NF model	a	b	С	d
$\times \left\{ \boldsymbol{\xi}^{\alpha\beta} \Big[\boldsymbol{a} + \boldsymbol{b} \boldsymbol{q} \cdot \boldsymbol{q}' + \boldsymbol{c} \left(\boldsymbol{q}^2 + \boldsymbol{q}'^2 \right) \Big] - \boldsymbol{d} \left(\tau_j^{\gamma} \boldsymbol{\epsilon}^{\alpha\beta\gamma} \vec{\sigma}_j \cdot \boldsymbol{q} \times \boldsymbol{q}' \right) \right\} \tau_i^{\alpha} \tau_k^{\beta}$		FM	0.0	-1.15	0.0	-0.29
		ТМ	1.13	-2.62	1.05	-0.60
$F_{\pi NN}(q^2) \;=\; rac{\Lambda^2 - m_\pi^2}{\Lambda^2 + q^2}.$		Urbana IX	0.0	-1.20	0.0	-0.30
		Brazil	1.05	-2.29	1.05	-0.77
m + q		Texas	1.87	-3.82	0.0	-1.12
b, d p-wave a s-wave	С	Ruhr	0.51	-1.82	0.0	-0.48
	$ \setminus $	TM'	-0.87	-2.62	0.0	-0.60
$\begin{bmatrix} \pi \\ \mu \\$	N N N					

Chiral EFT (modern force)

- (may be) Connected to QCD
- > Interactions: π , N, contact-term
- 2NF,3NF: extracted naturally on the same bases.



Looking for 3NF

Looking for 3NF

-- Binding energy of ³H (simplest 3 nucleon system)--



$$BE(^{3}H) = [M_{p} + 2M_{n} - M(^{3}H)]c^{2} = \Delta Mc^{2}$$

= 8.48 MeV

2N potential	w/o 3NF (MeV)	with 3NF (MeV)
CDBONN	8.013	8.48
Nijmegen I	7.741	8.48
Njimegen II	7.659	8.48
Nijmegen 93	7.668	8.48
AV-18	7.628	8.48
experiment		8.48

2NF : various modern forces 3NF : Fujita-Miyazawa

One parameter exists. $\Lambda : \pi$ -N form factor adjusted

Once Λ fixed, parameter free Faddeev calc.

Looking for 3NF in pd scattering

•Precise *pd* scattering



Faddeev cal. Excellent fit! No 3NF effect visible! (No need of experiment !)



• Prediction of H.Witała. PRL 81(1998) 1183.





Measure Xsec $d\sigma/d\Omega$ at minimum. \rightarrow require high precision data



 p_{in} picks-up n_{targ} to form d_{exch} .

Results for p+d scattering at 135 MeV

135 MeV (a half of light velocity)



Sakamoto et al., PLB367(1996)60. Sakai et al., PRL 84(2000)5288. Sekiguchi et al., PR C65(2002)034003.

Results with 2NF only Faddeev cal.

No free parameter calculations



Results with 2NF + 3NF



Calculations reproduce beautifully data. \Rightarrow Effects of 3NF confirmed ! Sensitive only to T=1/2 3NF.

Systematic study



Our pd data available for 70-320 MeV

Contact: Kimiko Sekiguchi, Tohoku Univ.



Sekiguchi et al.

PRC **65**, 034003 (2002) PRL **95**, 162301 (2005) PRC **79**, 054008 (2009) PRC **83**, 061001 (2011) PRC **89**, 064007 (2014) PRC **96**, 064001 (2017)

Discrepancy increases at backward anglesSome important ingredient is still missing

Anecdote

We established 3NF effects in pd scattering around 2,000.

In 2007 we held a symposium FM50 to commemorate Fujita-Miyazawa 3NF theory at University of Tokyo.





It took 50 years! Needed time for Faddeev theory and 2NF.
Next challenge : T=3/2 3NF and 4NF?

How I was involved in few-body physics

Started with a construction of polarized ion source (1992 ~1994)



Adoped d_{pol} + p scattering for a beam polarimetry

Complete polarization observables (Ay, Ayy, Axx, Axz) successfully measured for the first time d-p at $E_d^{lab}= 270 \text{ MeV}$ 1.0 at intermediate energy. j < 40.5 (I was very proud of this and 0.0 did not pay strong attention to X-sec.) -0.5And submitted to Phys. Lett. on June 13, 1995. 0.5 0.0 0.5 0.0 -0.51.0 0.5 0.0 60 120 180 $\theta_{\rm c.m.}$ (degree)

PHYSICS LETTERS B

ROLE H. SIEMSSEN



Re: PLB/RHS 742

Measurement of the vector and tensor analyzing powers for the d-p elastic scattering at $E_d = 270 \text{ MeV}$ N. Sakamoto *et al.*

This paper presents new data on vector and tensor analyzing powers in d-p scattering at 270 MeV. The data are compared to Faddeev calculations. While good agreement between data and calculations is found for the analyzing powers, systematic discrepancies occur in the cross section.

The paper has a number of shortcomings that make it <u>unsuitable for publication</u> in Phys. Lett.:

- The polarization of the beam is measured only before acceleration in the cyclotron. No evidence is presented that the cyclotron would not lead to partial depolarization.
- The cross section measurements, with estimated 10 20% systematical errors and fluctuations larger than the error bars (fig.2) are hardly "state of the art".
- Interpretation of the data in terms of the asymptotic S/D-state ratio is inappropriate given the high momentum transfers involved. S/D-state ratios should be determined

the reader. The details of the separable expansion (table 2) would better be left to a

paper by Koike et al who do the calculation. (The statement on the use of a nondescript

For the reasons listed above I cannot recommend publication in Phys. Lett. B. Major

concerning the presentation of the results, the details of

workstation used for the calculations is not helpful either).

reworking would be needed to make the paper acceptable.

• The cross section measurements, with estimated 10 - 20% systematical errors and fluctuations larger than the error bars (fig.2) are hardly "state of the art".

Sincerely yours,

Rolf H. Siemssen

c.c.: Dr. H. Sakai (KVI)

NORTH-HOLLAND PHYSICS AND MATERIALS SCIENCE (Fleevier Science Publishers BV.) P.D. Box 103, 1000 AC Amsterdam, The Netherlands Cables: FSPOM Amsterdam, *Telex* 10704 espon al, *Telephone*: 20 8802434, *Telefare*: 20 5862580

After getting better X-sec data, revised paper was resubmitted.



18 January 1996

PHYSICS LETTERS B

Physics Letters B 367 (1996) 60-64

Measurement of the vector and tensor analyzing powers for the d-p elastic scattering at $E_d = 270$ MeV

N. Sakamoto^a, H. Okamura^a, T. Uesaka^a, S. Ishida^{a,1}, H. Otsu^a, T. Wakasa^a, Y. Satou^a, T. Niizeki^b, K. Katoh^b, T. Yamashita^b, K. Hatanaka^c, Y. Koike^d, H. Sakai^a

^a Department of Physics, University of Tokyo, Bunkyo-ku, Tokyo 113, Japan

^b Department of Physics, Tokyo Institute of Technology, Meguro-ku, Tokyo 152, Japan

^c Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka 567, Japan

^d Department of Physics, Hosei University, Chiyoda-ku, Tokyo 102, Japan

Received 13 June 1995; revised manuscript received 18 October 1995 Editor: R.H. Siemssen

Abstract

The differential cross sections and the vector and tensor analyzing powers A_y , A_{yy} , A_{xx} , and A_{xz} for the *d-p* elastic scattering were measured at $E_d^{\text{lab}} = 270$ MeV over the c.m. angular range from 57° to 138°. The data are compared with a Faddeev calculation. A good description is obtained for all components of the analyzing powers, while a discrepancy of about 30% is found in the cross section around $\theta_{\text{c.m.}} = 120^{\circ}$.

Sakamoto paper, PL B367(1996)60



Koike,s calc.
Faddeev calc.
With Coulomb
Separable potential
No 3NF

■A_y,A_{xx},A_{yy},A_{xz} reproduced well for measured angular range

My surmise at that time

Without deteriorating good fits to all Aij, 30% diff. in X-sec cannot be recovered. After this measurement, the rigorous Faddeev calc. appeared and I was seriously involved in FB physics.

3NF is included in the title in the PRL

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PHYSICAL REVIEW LETTERS

5 JUNE 2000

140

 $\theta_{\rm c.m.}$ [deg]

 $\theta_{\rm c.m.}$ [deg]

160

Precise Measurement of dp Elastic Scattering at 270 MeV and Three-Nucleon Force Effects

H. Sakai,^{1,5,*} K. Sekiguchi,¹ H. Witała,² W. Glöckle,³ M. Hatano,¹ H. Kamada,³ H. Kato,¹ Y. Maeda,¹ 7. Satou,⁵ K. Suda,⁴ A. Tamii,¹ T. Uesaka,⁴ State-of-the-art $d\sigma/d\Omega$, x_{xx} , A_{yy} , A_{xz} , P_y , K_{xx} , K_{vv} , K_{vv} , **Now everywhere 3NF !** 0 $rac{d\sigma}{d\Omega} \, [\mathrm{mb/sr}]$ 0.4 $K_{xx}^{y'}$ 0.3 0.2 **Research develops unexpectedly** 0.1 0.0 0.2 **Serendipity**? 0.6 0.4 $K_{yy}^{y'}$ **Right time by lucky** 0.2 **NN-int. established** >NN+3NF Faddeev calc. available 0.6 0.2 0.4 0.0 PIS: dedicated only for deuteron P^{y} 0.2 -0.20.1 > Polarimetry by *dp* scattering 0.0 0.4 0.2 **>etc.** 0.1 K_{xz}^{y} 0.0 -0.2 [---60 120 180 120 180

So far T=1/2 3NF

Next challenge: T=3/2 Requires n-n-n/p-p-p system

Tetraneutron with SHARAQ

Multi-neutron system to study T=3/2 3NF



Spokesperson: K. Kisamori, S. Shimoura



K. Kisamori et al., PRL116, 052501 (2016)

Tetraneutron (⁴n) prior to our experiment

Marques *et al.*, PRC65(02)044006

- > Neutron cluster search ${}^{14}\text{Be} \rightarrow {}^{10}\text{Be} + {}^{4}\text{n}$
- > Hint of bound tetraneutron !



PHYSICAL REVIEW C 72, 034003 (2005)

Is a physically observable tetraneutron resonance compatible with realistic nuclear interactions?

Rimantas Lazauskas* DPTA/Service de Physique Nucléaire, CEA/DAM Ile de France, BP 12, F-916

4NF introduced to artificially bind tetraneutron !

Jaume Carbonell[†]

Laboratoire de Physique Subatomique et de Cosmologie, 53, avenue des Martyrs, F-38026 Grenoble Cedex, France[‡] (Received 22 April 2005; published 20 September 2005)

The possible existence of four-neutron resonances close to the physical energy region is explored. Faddeev-Yakubovsky equations have been solved in configuration space using realistic nucleon-nucleon interaction models. Complex scaling and analytical continuation in the coupling constant methods were used to follow the resonance pole trajectories, which emerge out of artificially bound tetraneutron states. The final pole positions for fourneutron states lie in the third energy quadrant with negative real energy parts and should thus not be physically observable.

Exothermic DCHEX reaction to create ⁴n

⁴He(⁸He,⁸Be)⁴n reaction

8Be \rightarrow 2 α observed







Measurement of ⁴n at rest with SHARQ

⁸Be: 2α measured at SHARAQ magnetic spectrometer
 SHARAQ :constructed under ICHOR Project (Spokesperson H. Sakai)



Result of ⁴He(⁸He,⁸Be)4n

K. Kisamori, Shimoura, Sakai et al., Phys. Rev. Lett. 116, 052501 (2016).



• 4 counts (resonance!) • $E_R = 0.83 \pm 0.65(\text{stat.}) \pm 1.25(\text{sys.})$ MeV • $\Gamma \le 2.6$ MeV(FWHM) • $\sigma = 3.8^{+2.9}_{-1.8}$ nb • significance = 4.9 σ

Recoilless exothermic CHEX reaction!

T=3/2 3NF must play an important role.
 → also important for multineutron system as well as neutron stars.



Recent theoretical works on ⁴n (yes)

A.M. Shirokov et al., PRL 117(2016)182502

NCSM calculation with DISP16 interaction: No 3NF! Non-local



4-body phase shift (HH coordinate) shows resonance around E_r =0.8 MeV with Γ =1.4 MeV.

S. Gandolfi et al., PRL 118(2017)232501

Ab initio calc. with 2N+3N in chiral EFT



 E_R =1.84 MeV with Γ=0.28 MeV. E_R (³n) < E_R (⁴n) Trineutron resonance at 1 MeV!

Recent theoretical works on ⁴n (No)

• E.Hiyama et al., PRC 93(2016)044004

- Solve Faddeev-Yakubovsky (FY) equations
- $\succ~$ Complex scaling method to get E_r and Γ



Too strong attraction is necessary for ⁴n resonance, which makes ⁴H bound!

- A. Deltuva, PLB 782(2018)238
- **>** Exact continuum eq. for trans. ope.
- AGS equation (momentum space)



To produce a resonance, 5 times more attraction is necessary.

Recent theoretical works on ⁴n (Yes/No)

K. Fossez, PRL 119(2017)032501

No Core Gamow SM+density reno. G 2 neutrons in the continuum

No 3NF.



 E_r may be compatible with exp. but Γ_r must be larger than 3.7 MeV.

We confirm the existence of a pole of the scattering matrix associated with the spin and parity $J^{\pi} = 0^+$ in this system as shown in previous studies; however, the proper inclusion of the couplings to the continuum shows that this pole must be a feature in scattering experiments and not a genuine nuclear state. Physically this can be interpreted as a reaction process involving four neutrons, which is too short to form a nucleus.



-- New measurement --

Spokesperson: S. Masuoka, S. Shimoura



Measurement was carried out in June 2016 to get more statistics

New measurement (still preliminary)





Merit of exothermic DCHEX reaction:
 1. Keep size of 4n in 1.7 fm ⇒T=3/2 3NF works !
 2. Recoil-less (q~0) ⇒ cm of 4 neutrons is at rest

Results of ¹H(⁸He,pα)4n are eagerly awaited. (Single-step knockout reaction. Huge X-sec.)

Search for tri-neutron (³n) resonace to study T=3/2 3NF

Recent theoretical works on ³n after ⁴n



Tri-neutron search by CHEX reaction

For tri-neutron search (same as the tetra-neutron search)

- Create 3n system at rest by exothermic CHEX reaction
- Best choice is ³H(⁹Li, ⁹Be)3n. Q=+4.4 MeV
- Recoilless condition (q=0) can be achieved.
- Alternative might be ³H(*t*, ³He)3n. Q=–6.9 MeV (not exothermic)
- In any case, ³H Target needed

Single CE: ${}^{3}\text{H} \rightarrow {}^{3}\text{n}$



SD: σ(ΔL=1)~finite angle
→ large q transfer (~100 MeV/c))
→give up recoilless condition

Large opportunity of observing 3n resonance . (It depends on S/N(QFS)).

Considering isospin symmetry, ${}^{3}\text{He}({}^{3}\text{He}, t)$ 3p is very interesting (3p \leftrightarrow 3n).

Study of three-nucleon resonance states via ³He(³He,*t*)3p and ³H(*t*, ³He)3n

Spokesperson: K. Miki, D. Sakai





³p (new) and ³n (plan) measurements



> E502 exp. Done.
 > GRAIDEN at RCNP
 > E(3He)=140 MeV/u
 > ΔE~0.4 MeV
 > Ex=0 - 25 MeV
 > θ(lab)=0 - 6 degrees

Proposal accepted (NP1712-SHARAQ11)
 SHARAQ at RIBF
 E(t)~140 MeV/u

Tritium target, in preparation

³He(³He,t)3p measurement (preliminary)



Broad peak at Ex~10 MeV

σ(θ) peaks at ~3°, expected for L=1.
QFS background?

³He(p,n)3p vs. ³He(³He,t)3p at 0°

PHYSICAL REVIEW C 77, 054611 (2008)

Complete set of polarization transfer coefficients for the ${}^{3}\text{He}(p, n)$ reaction at 346 MeV and 0 degrees



Isospin symmetry and 3n resonance energy

• Wakasa derived

 $E_r({}^3\text{Li}) = 9 \pm 1 \text{ MeV} \\ \Gamma_r({}^3\text{Li}) = 10.5 \pm 1 \text{ MeV} \qquad J^{\pi}(3p) = 1/2 \text{-suggested}$

$$E_x(^3n) = E_x(^3p) - \left[\Delta \varepsilon_{Coul} + (m(^3n) - m(^3p))\right] = 9 - 3.4 - 2.4 \sim 3 MeV$$



Tetraneutron resonance may exist at Ex ~ 3 MeV !
 Width Γ and S/N ?



Please look forward to 3H(t,3He)3n measurement. Stay tuned.



How about four nucleon force (4NF)?

Binding energy ⁴He [MeV]

Potential	w/o 3NF	With 3NF
CDBONN	26.26	28.40
Nijmegen I	24.98	28.60
Njimegen II	24.56	28.56
AV-18	24.25	28.36
Exp. value		28.30

6 pairs : 2NF

4 pairs : 3NF

1 pair : 4NF



Reproduced only with 3NF
\rightarrow 4NF : very small, if exists at all.

χEFT prediction

 $\langle V_{NN} \rangle \sim 20 \,\mathrm{MeV/pair}\,,$

 $\langle V_{3Nf} \rangle \sim 1 \,\mathrm{MeV/triplet}\,,$

 $\langle V_{4Nf} \rangle \lesssim 0.1 \,\mathrm{MeV/quartet}$.

J.L. Friar : FBS Suppl. 99(2018)1



Three nucleon force (3NF)

- Proton + deuteron scattering \Rightarrow 30% discrepancy in X-sec.
- Clear signature of 3NF (sensitive to T=1/2)

Tetraneutron (4n) search

- Exothermic DCHEX. ⁴He(⁸He,⁸Be)4n
- 4 counts at Ex~1 MeV; resonance?
- New meas. ; still in analysis

Trineutron (3n) search

- In measurement with ³H(t,³He)In is in plan. Tritium target?
- 3p data is taken with ³He(³He,*t*)3p.
- Predicts E_r(3n)~3 MeV

Next target : T=3/2 3NF, 4NF or ...

Tritium beam @ ISOL +SCL3+KOBRA

~my small suggestion~ Could be totally nonsense

18.5 MeV tritium beam@SCL3 A/q=3

Open up unique facility in the world

- **Few-body physics**
- Nuclear spectroscopy, (t,p)/(t,3He)/etc. (astrophysics? (α,p)~(t,γ))
- •How to produce tritium beam
 - ➤ ISOL (possible ?)
 - > Better to construct a dedicated small target system
 - p(70MeV)+ 4He/7Li→ t+etc.
 (only light particles, n,p,d,t,α are produced)
 - etc.
- Many Difficulties
 Radiation safety
 - ≻etc.

Thank you ! 감사 !

RAON(樂) 연구 시설을 이용한 연구 성과가 매우 오르는 것을 간절히기도합니다