



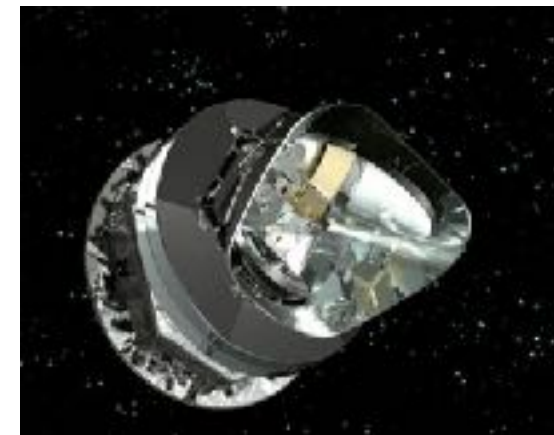
Beyond Higgs inflation and dark matter

Hyun Min Lee

Chung-Ang University, Korea

2019 Joint Workshop of FKPPL & TYL/FJPPL
Seogwipo KAL hotel, Jeju Island, May 9, 2019.

Finding **N**ew Physics: From **E**arth to **S**ky



- New Physics for Higgs and Hierarchy
Problem: supersymmetry, warped extra dimension, clockwork mechanism, etc.
- New Physics for Dark Matter: WIMP, FIMP, SIMP, new production mechanisms and detections.
- New Physics for Flavor Physics: fermion masses/mixing, flavor puzzles from rare decays, magnetic/electric dipole moments.

FNES Collaboration



French team

Korean team



Yann Mambrini
(LPT, Orsay)



Hyun Min Lee
(CAU)



Mathias Pierre
(Former student,
Postdoc in IFT, Madrid)



Soo-Min Choi
(PhD student, CAU)



Published work: [Vector SIMP dark matter](#), JHEP 1710, 162.

(collaboration with H. Murayama, E. Kuflik, Y. Hochberg)

Submitted: [Vector SIMP dark matter with approximate custodial symmetry](#), 1904.04109 [hep-ph].

Workshops and Visits

Korea: funded by BK21+, NRF

KIAS Research Station, 16-19 Oct, 2016

KIAS Workshop, 24-28 Oct, 2016

Chung-Ang University, 28 Oct - 2 Nov, 2017

France: funded by FKPPL

LPT, Orsay, 29-31 Jan, 2017

Dark Side of Universe, Annecy,
25-29 June, 2018

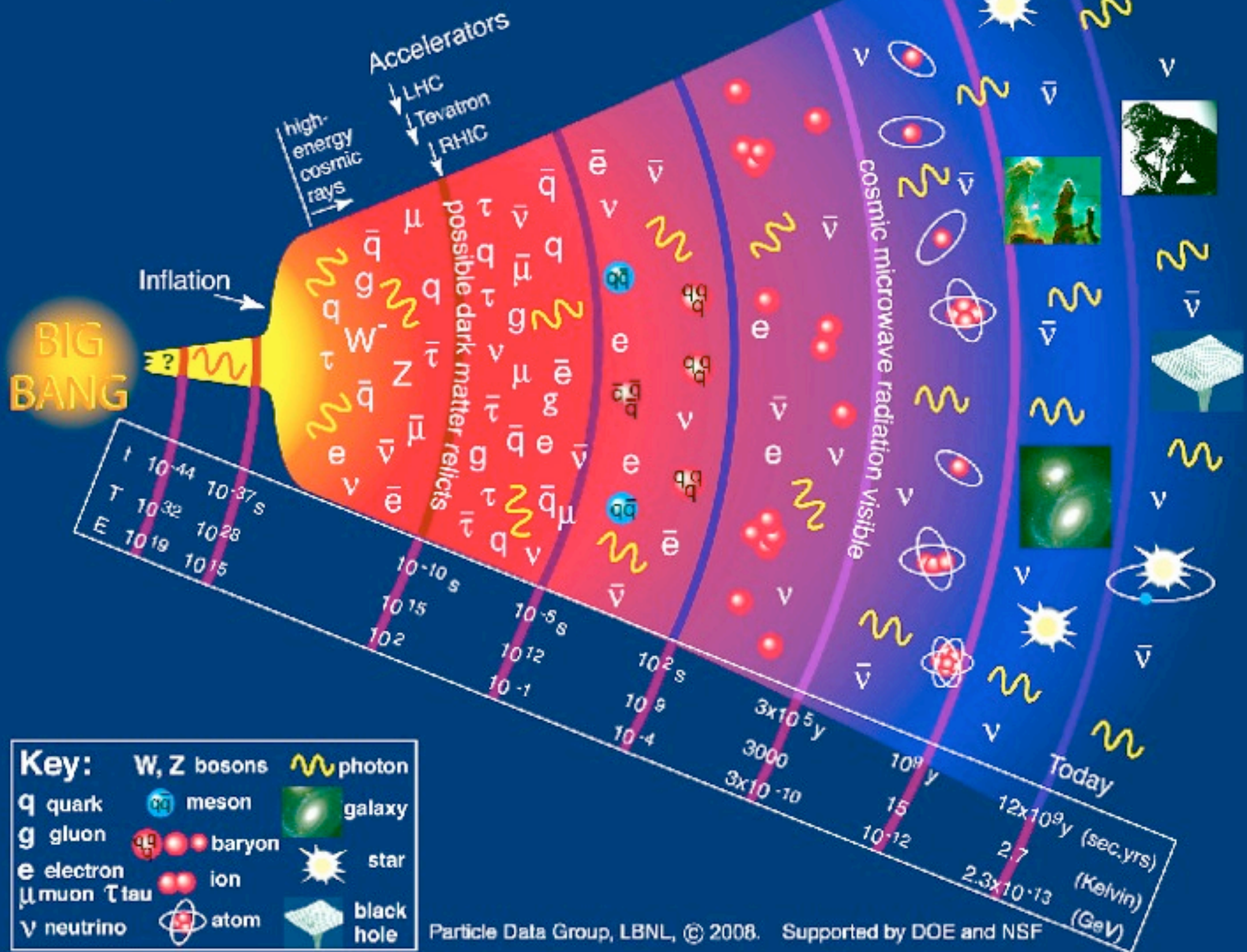
Astroparticle Symposium, Saclay,
28 Oct - 8 Nov, 2019



Outline

- Higgs inflation and beyond
- General sigma inflation
- Inflaton as dark matter
- Conclusions

History of the Universe



Particle Data Group, LBNL, © 2008. Supported by DOE and NSF

Instability of Higgs vacuum

- Quantum fluctuations change Higgs potential.

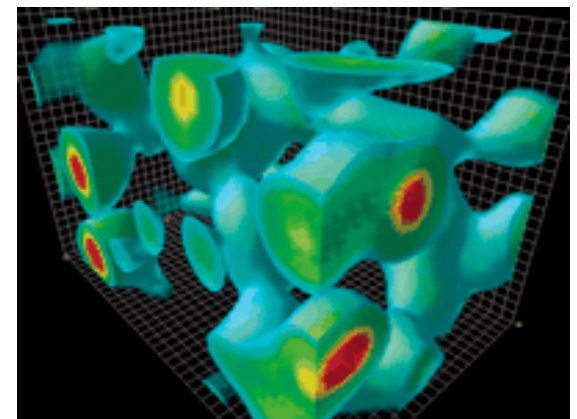
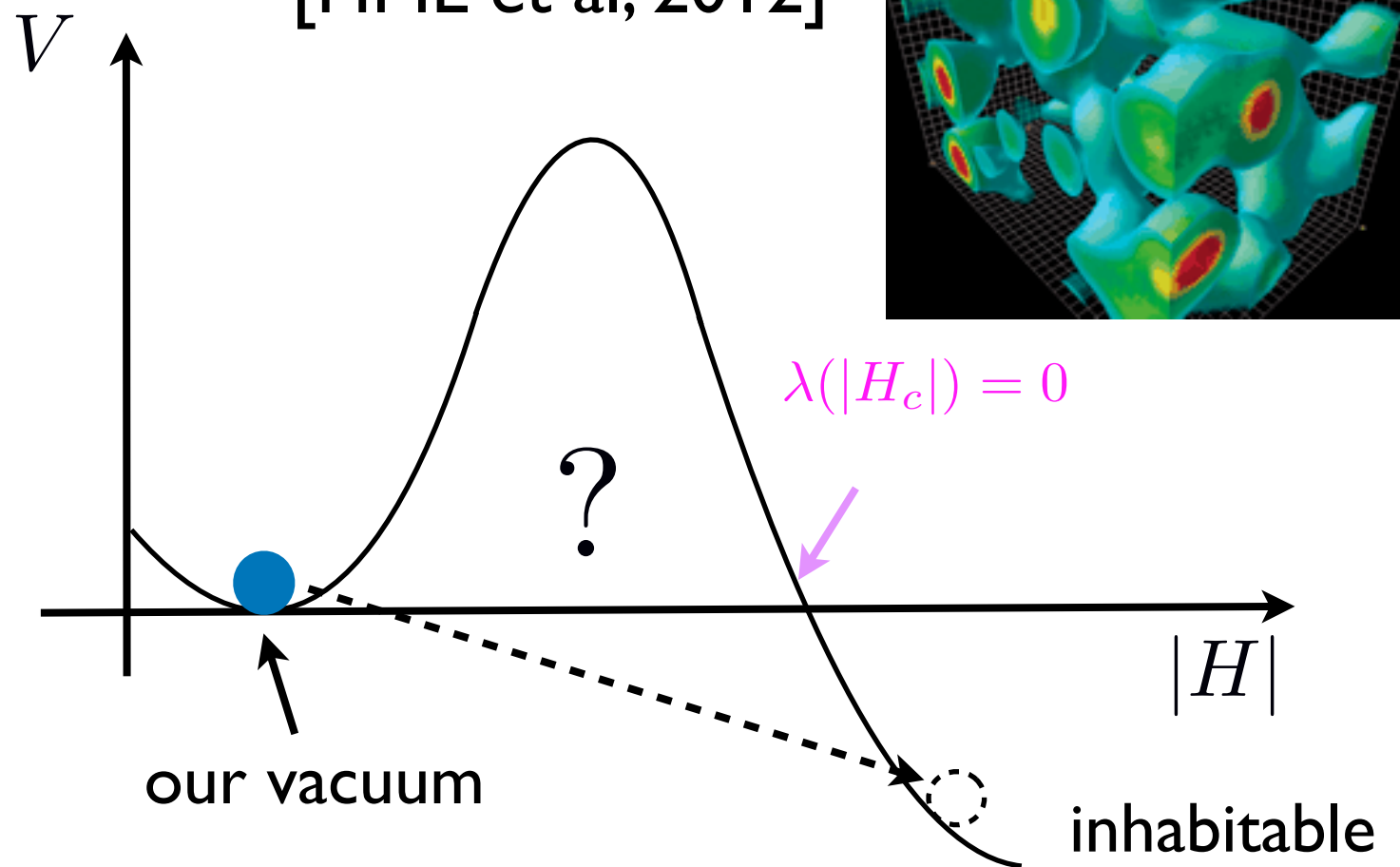
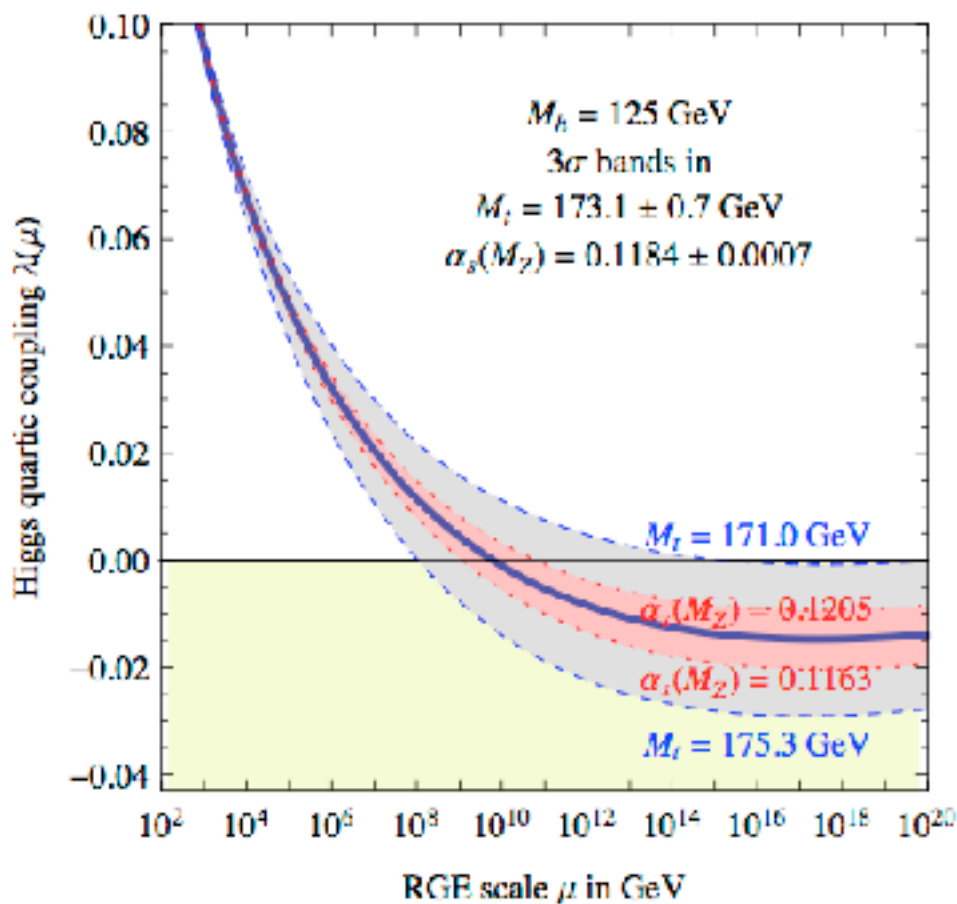
$$V = -\mu^2 |H|^2 + \lambda |H|^4$$

$$m_H \ll M_P \sim 10^{18} \text{ GeV}/c^2;$$

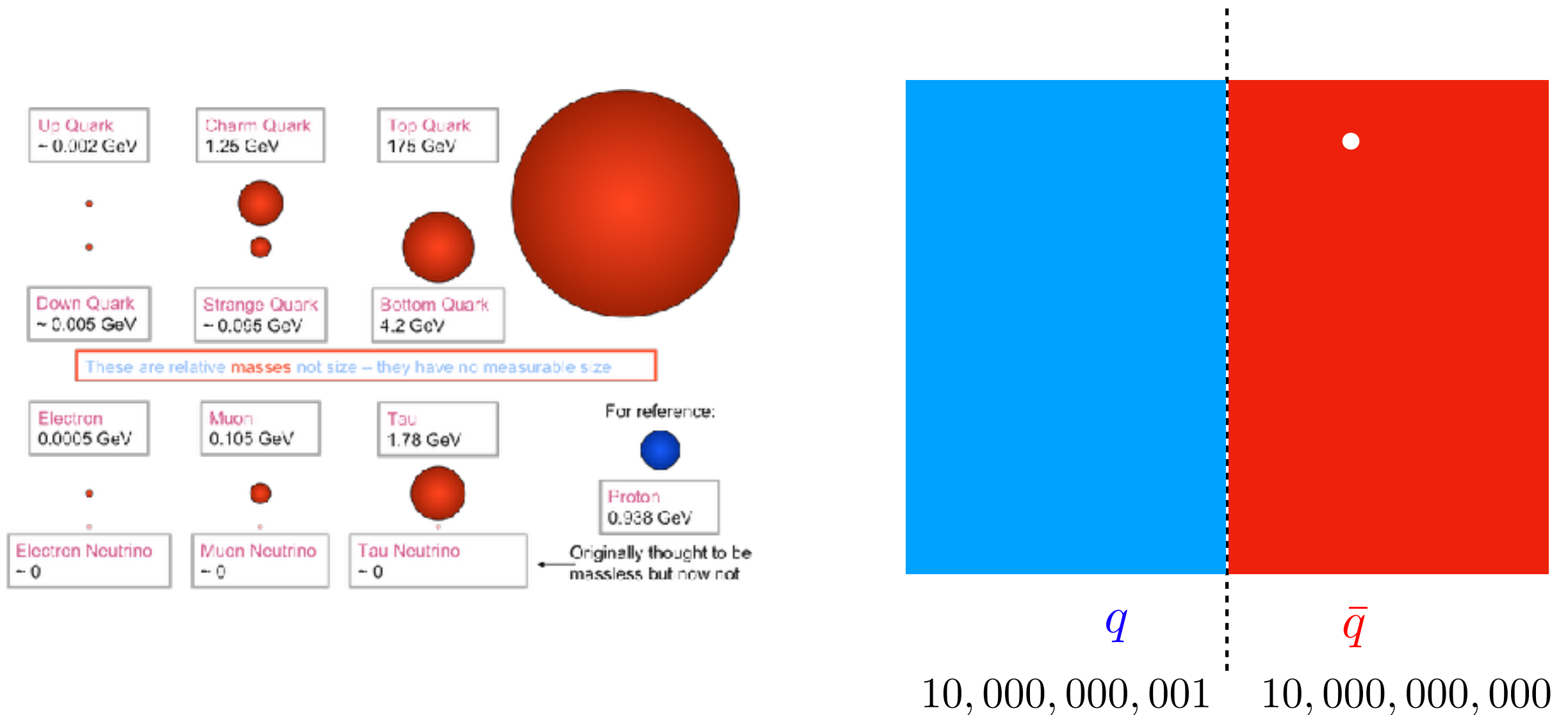
$$\lambda(v) = \frac{m_H^2}{2v^2} = 0.13$$

$$\lambda(\mu) \approx \lambda(v) - \frac{3}{8\pi^2} y_t^4(v) \ln\left(\frac{\mu}{v}\right) \rightarrow \text{Stability of Higgs vacuum}$$

[HML et al, 2012]



Flavor puzzles



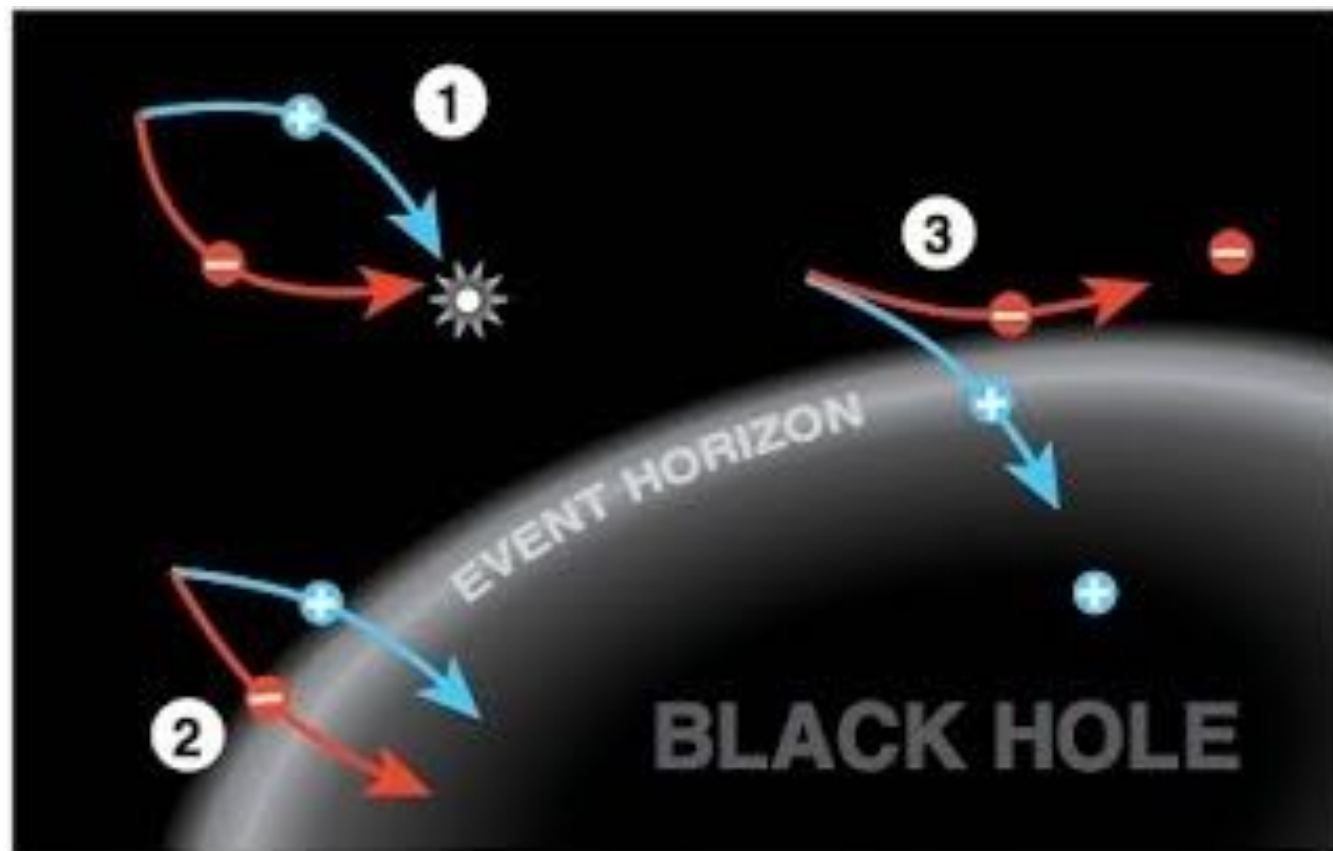
- Quark and lepton masses? Origin of neutrino masses?

$$m_e/m_t \sim 10^{-6}, \quad \Delta m_\nu^2 \sim 10^{-3} \text{eV}^2$$

- Origin of matter asymmetry?

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} = (5.8 - 6.6) \times 10^{-10}$$

Gravity and Big Bang



Cosmic refugees. Virtual particles that escape destruction near a black hole (case 3) create detectable radiation but can't carry information.

Path integral for gravity:

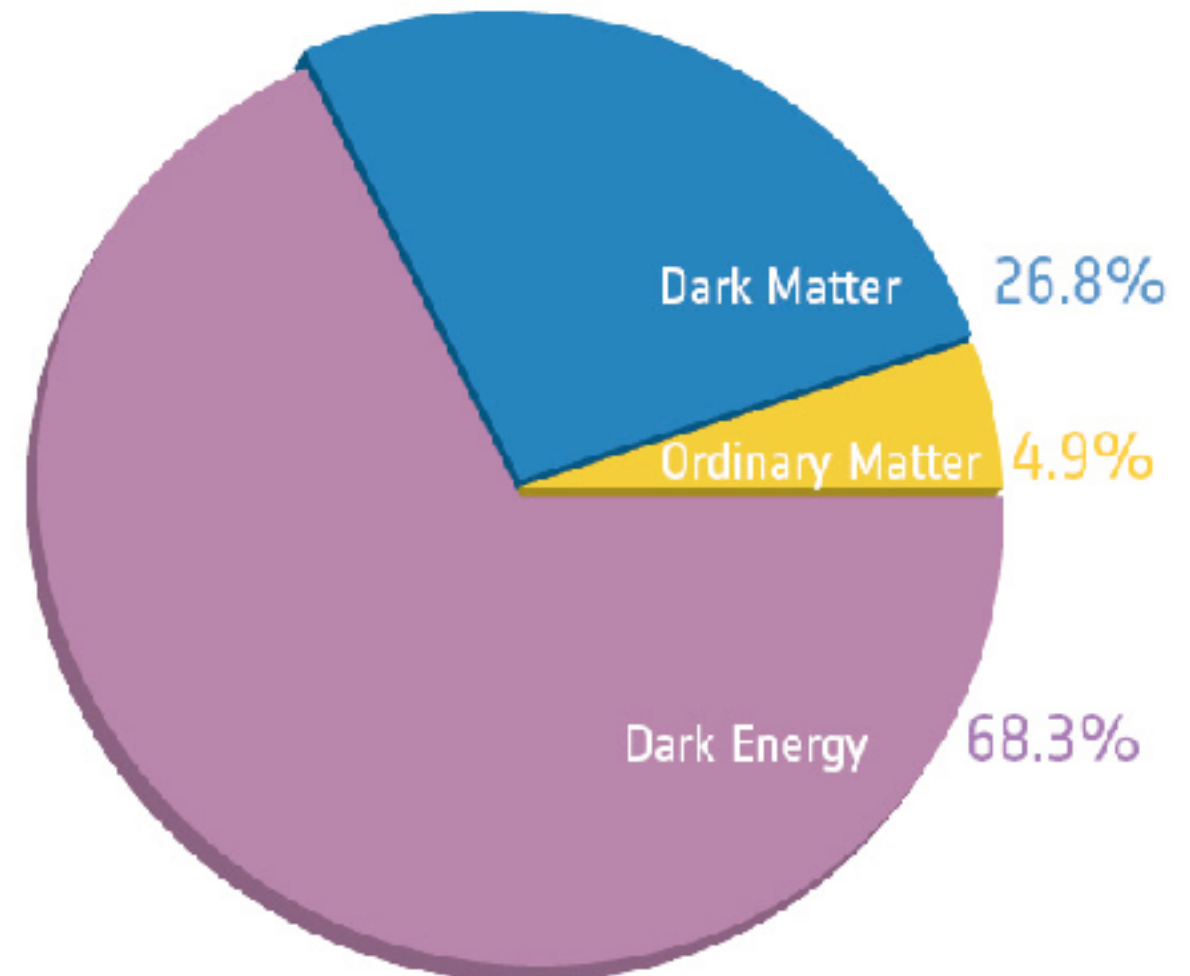
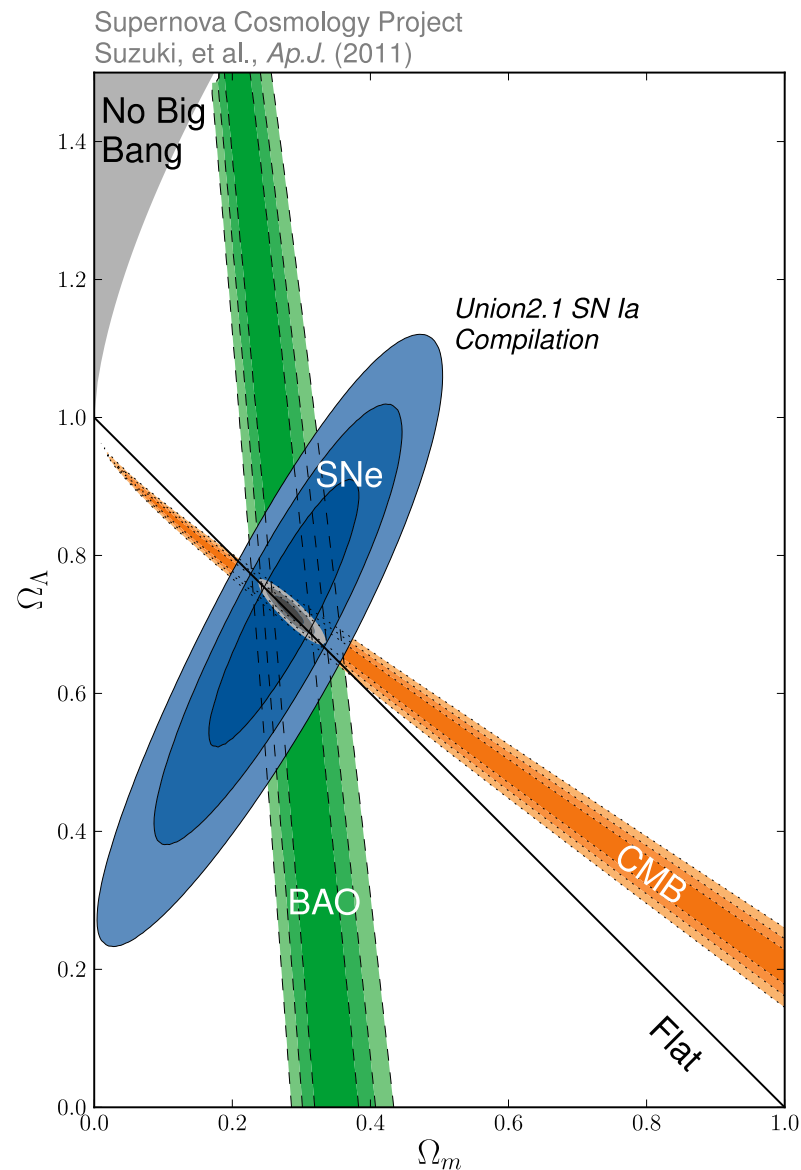
$$\int dg d\psi_{\text{SM}} e^{i \int d^4x \sqrt{-g} \mathcal{L}_{\text{tot}}},$$
$$\mathcal{L}_{\text{tot}} = \frac{1}{16\pi G} R - \Lambda + \mathcal{L}_{\text{SM}}$$

$$M_P^2 = \frac{1}{8\pi G},$$

$$\Lambda = 10^{-122} M_P^4 \ll M_P^4.$$

- Quantum mechanical description of gravity?
- Origin of initial conditions for Big Bang?
- Origin of Planck mass & Cosmological constant?

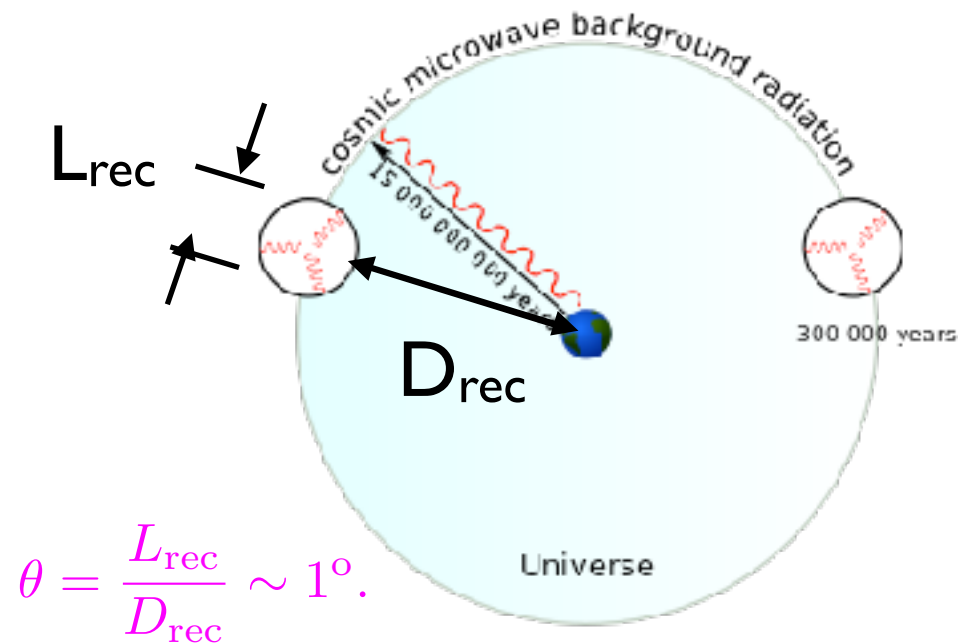
Dark matter and energy



- Observed Universe is composed of 5% atoms and 95% of dark matter and dark energy.
- Origin of dark matter and dark energy?

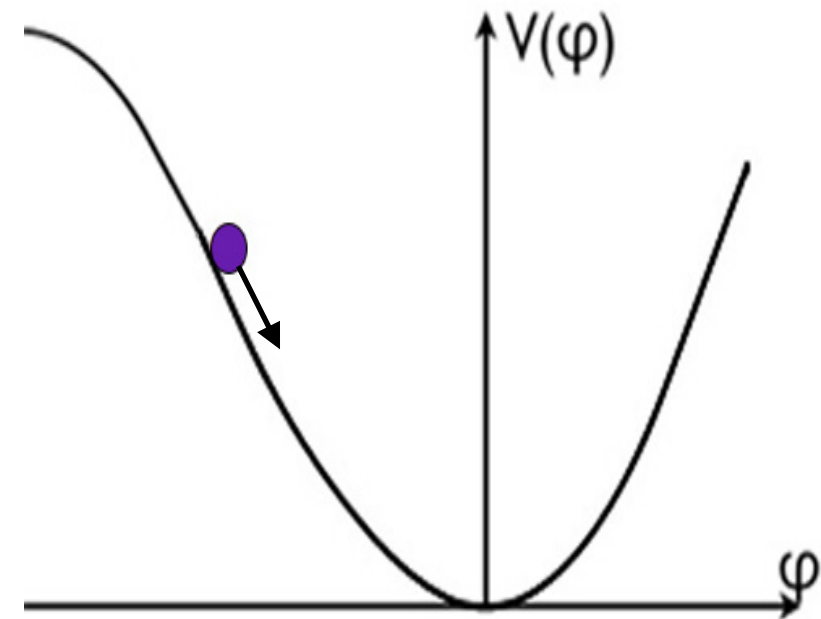
Cosmic inflation

- Early varying vacuum energy with “inflaton” makes the expansion possible at all and sets the initial conditions.



Causally connected
at recombination

How uniform CMB I in 10^4 ?



$$ds^2 = -dt^2 + e^{2Ht} d\vec{x}^2$$

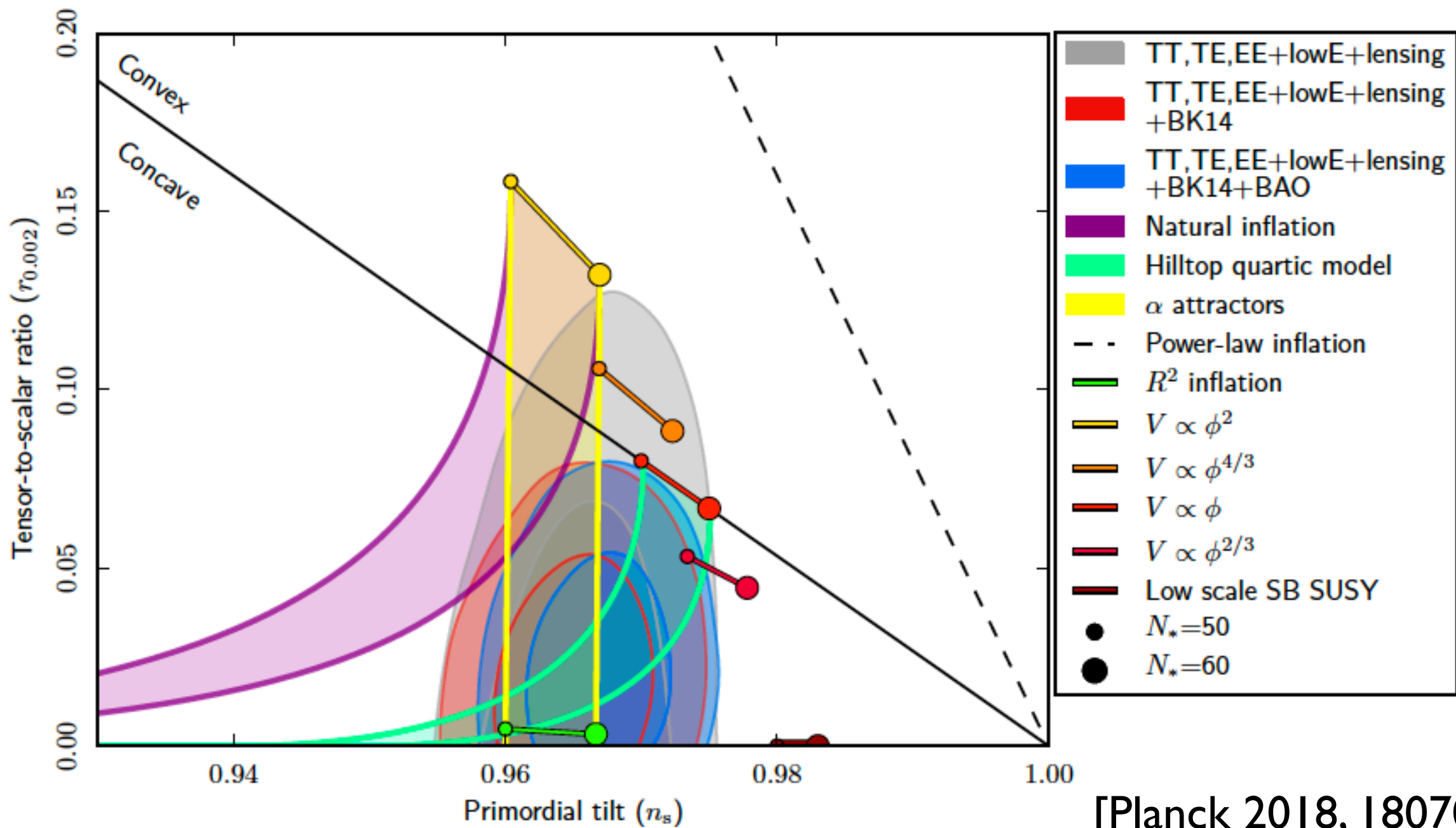
Number of efoldings:

$$N = \int_{t_i}^{t_f} H dt = 60$$

- Slow-roll inflation is constrained by CMB anisotropies.

$$n_s = 1 - 6\epsilon + 2\eta, \quad r = 16\epsilon, \quad \epsilon \sim \frac{(V')^2}{V^2} \ll 1, \quad \eta \sim \frac{V''}{V} \ll 1.$$

Planck data



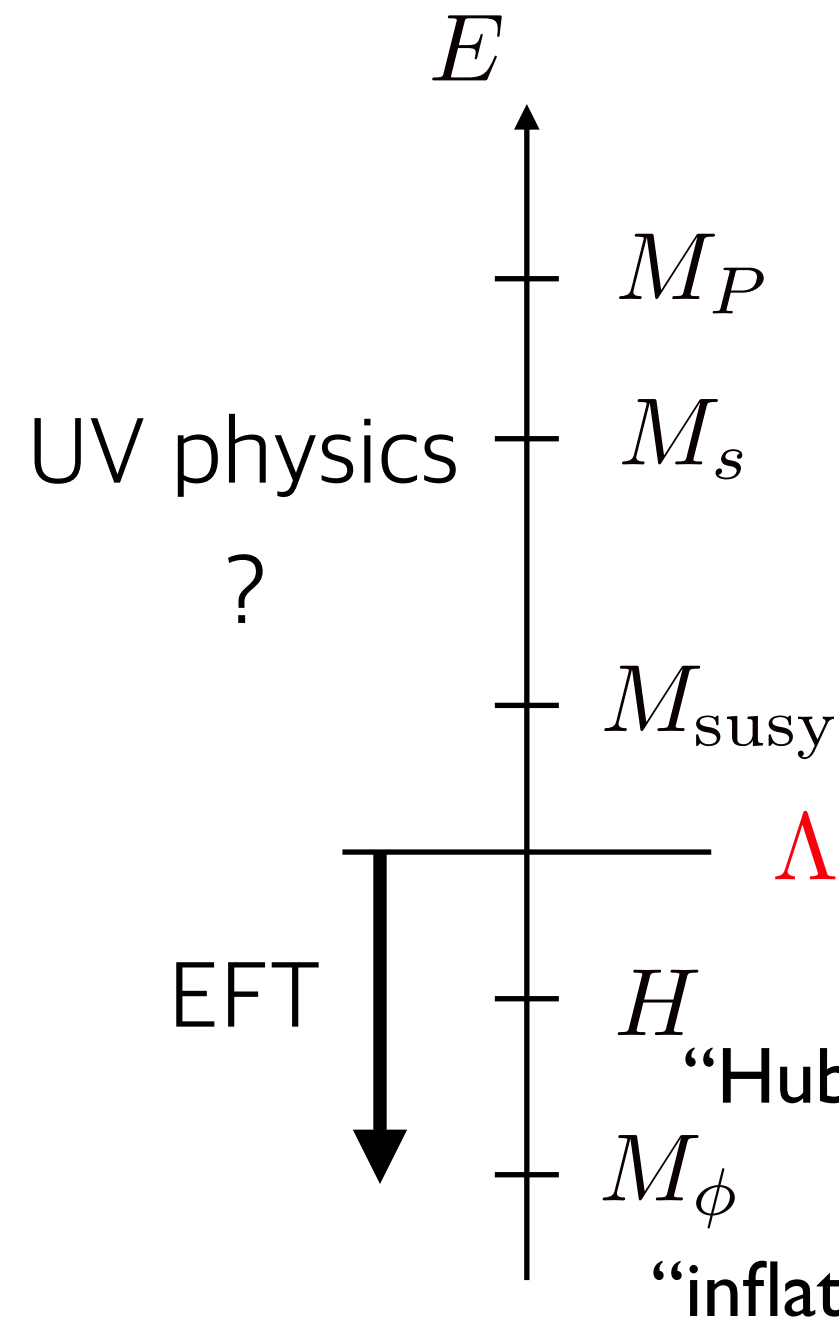
$$n_s = 0.9659 \pm 0.0041$$

$$r_{0.002} < 0.10 \quad (95\% \text{ CL, Planck TT+lowE+lensing})$$

$$n_s = 0.9653 \pm 0.0041$$

$$r_{0.002} < 0.064 \quad (95\% \text{ CL, Planck TT,TE,EE+lowE+lensing+BK14}).$$

Inflation as EFT



$$\epsilon \sim \frac{(V')^2}{V^2} \ll 1, \quad \eta \sim \frac{V''}{V} \ll 1.$$

$$\rightarrow M_\phi \ll H \sim \sqrt{V} \ll \Lambda$$

- Effective field theory for inflation must work in a well-defined energy window.

$$\mathcal{L} = \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m_\phi^2 \phi^2 - \frac{1}{3}B\phi^3 - \frac{1}{4}\lambda\phi^4 - \sum_{n=1}^{\infty} \frac{c_n \phi^{n+4}}{\Lambda^n}.$$

- What controls UV physics (or keeps unitarity) for entire range of inflaton fields?

Higgs inflation

[Bezrukov, Shaposhnikov (2007)]

- Bottom-up approach: Higgs boson as inflaton.

$$\mathcal{L} = \sqrt{-g} \left(\frac{1}{2} \mathcal{R} + \xi |H|^2 \mathcal{R} - |D_\mu H|^2 - \lambda_H (|H|^2 - v^2/2)^2 \right)$$

$$\longrightarrow \mathcal{L}_E = \sqrt{-g_E} \left(\frac{1}{2} \mathcal{R}(g_E) - \frac{3\xi^2}{\Omega^2} (\partial_\mu |H|^2)^2 - \frac{1}{\Omega} |D_\mu H|^2 - \frac{V}{\Omega^2} \right)$$

$$g_{\mu\nu} = \Omega^{-1} g_{E,\mu\nu}, \quad \Omega = 1 + 2\xi |H|^2$$

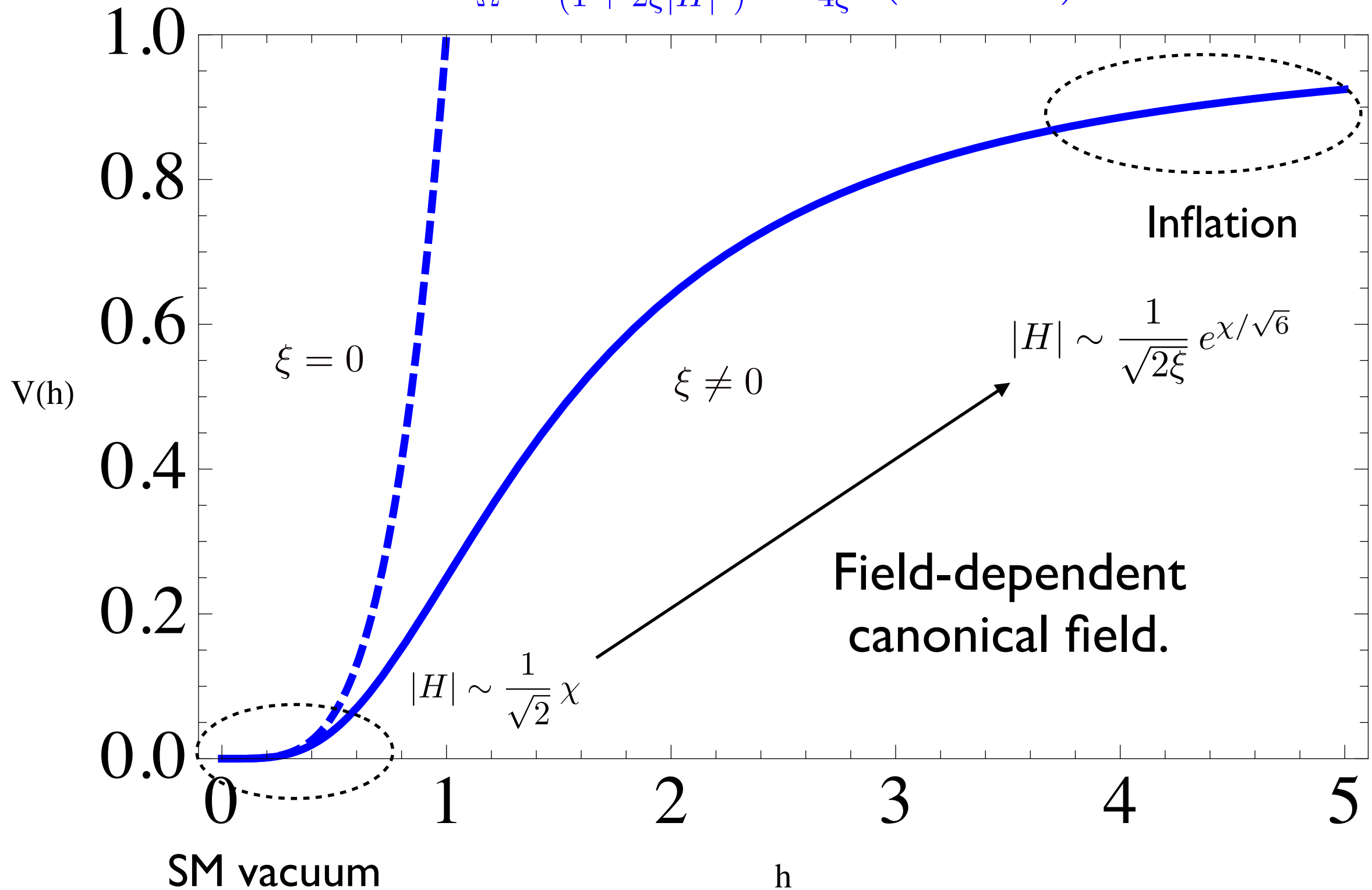
Adding a non-minimal coupling makes inflation work!

$$\checkmark \quad \frac{\Delta T}{T} \sim 10^{-4} \longrightarrow \frac{\sqrt{\lambda_H}}{\xi} = 2 \times 10^{-5} \quad \text{“Large non-minimal coupling”}$$

$$\checkmark \quad n_s = 1 - \frac{2}{N} = 0.966, \quad r = \frac{12}{N^2} = 0.0033 \quad \text{“Perfect for Planck data”}$$

Higgs inflation

$$\frac{V}{\Omega} = \frac{\lambda_H |H|^4}{(1 + 2\xi |H|^2)^2} \sim \frac{\lambda_H}{4\xi^2} \left(1 - e^{-\frac{2}{\sqrt{6}} x}\right)$$



Higgs inflation as EFT

[Han, Willenbrock (2004); Burgess, HML, Trott (2009, 2010); Barbon, Espinosa (2009); Hertzberg (2010)]

- Higgs self-interactions

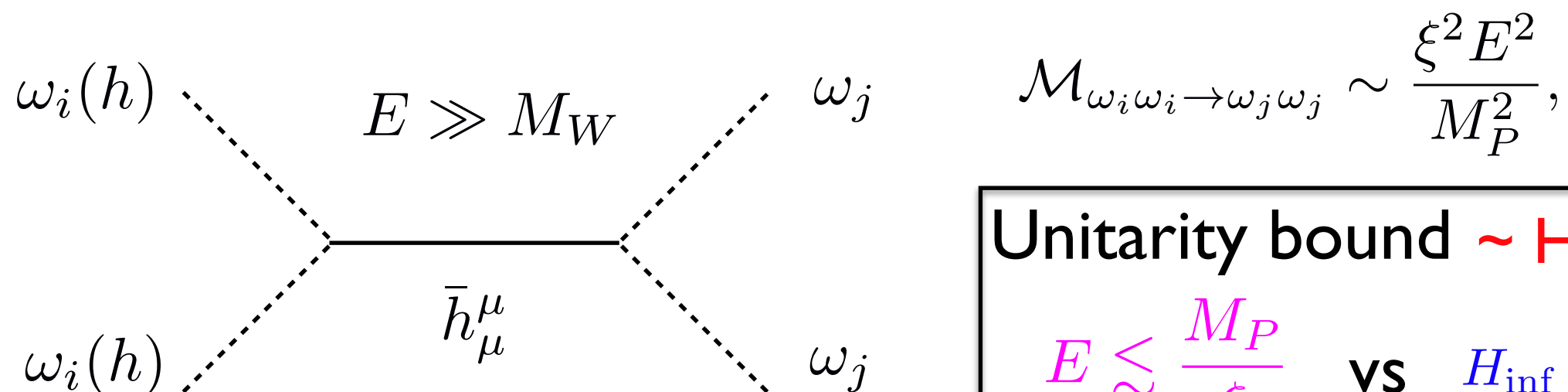
$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} -\omega_2(x) - i\omega_1(x) \\ \varphi(x) + h(x) + i\omega_3(x) \end{pmatrix}, \quad g_{\mu\nu}(x) = \hat{g}_{\mu\nu}(x) + \frac{h_{\mu\nu}(x)}{M_P}.$$

➔ $\mathcal{L}_{\text{int}} = \frac{1}{4} \left(\omega_1^2 + \omega_2^2 + \omega_3^2 + (\varphi + h)^2 \right) \frac{\xi}{\Lambda} \left(\square \bar{h}^\mu_\mu + 2\partial^\alpha \partial^\beta \bar{h}_{\alpha\beta} + \dots \right).$

cf. Einstein frame:

$$\mathcal{L}_{\text{eff}} = \frac{2\xi}{M_P^2} |H|^2 |D_\mu H|^2 - \frac{3\xi^2}{M_P^2} \partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H) + \frac{4\lambda_H \xi}{M_P^2} |H|^6 + \dots$$

- Effective field theory breaks down too early.



$$\mathcal{M}_{\omega_i \omega_i \rightarrow \omega_j \omega_j} \sim \frac{\xi^2 E^2}{M_P^2},$$

Unitarity bound ~ Hubble scale,

$$E \lesssim \frac{M_P}{\xi} \quad \text{vs} \quad H_{\text{inf}} \sim \frac{\sqrt{\lambda_H} M_P}{\xi}.$$

Beyond Higgs inflation

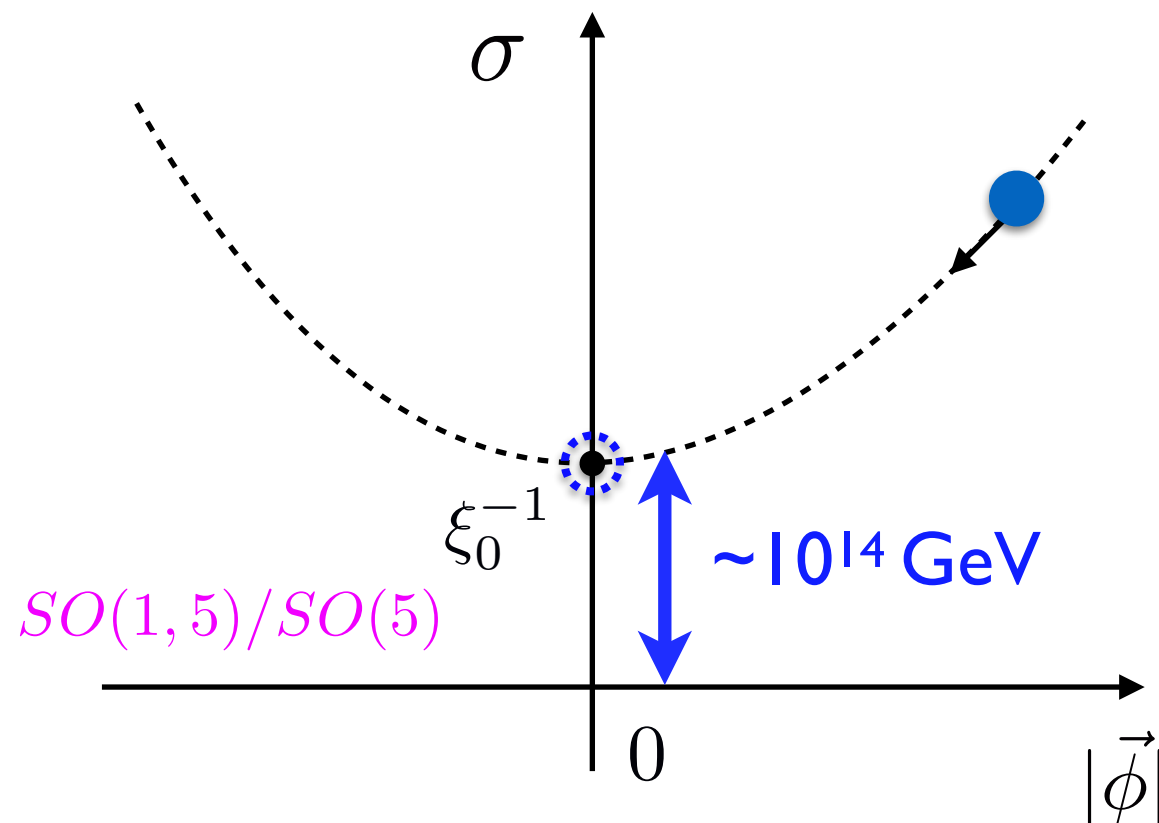
“Induced gravity” $\mathcal{L}_J = \sqrt{-g} \left[\xi_0 \sigma^2 \mathcal{R} - \frac{1}{2} (\partial_\mu \sigma)^2 - \lambda (\sigma^2 - \vec{\phi}^2 - \xi_0^{-1})^2 \right]$

Planck mass is induced by loops: [Zee, Smolin (1979)]

$$\int D\psi e^{iS(g,\psi)} = e^{i \int d^4x \sqrt{-g} (M_P^2 \mathcal{R} + \dots)}$$

➔ Higgs inflation just as EFT: $\mathcal{L}_{\text{eff}} = \sqrt{-g} (1 + \xi_0 \vec{\phi}^2) \mathcal{R}$

Higgs moves together with sigma field in hyperboloid!



[Giudice, HML (2010)]

- 1) $SO(4) \Rightarrow SO(1,5)/SO(5)$
- 2) Higgs inflation-like.
- 3) Sigma field is very heavy.

$$m_\sigma^2 = 4\lambda H^2 \sim (10^{13} \text{ GeV})^2$$

Scalars dual to Starobinsky

- Starobinsky R^2 model is dual to a scalar-tensor theory.

[Starobinsky (1984); Giudice, HML (2014)]

$$\mathcal{L} = \sqrt{-g} \left(\frac{R}{2} + \xi^2 R^2 \right) \longleftrightarrow \mathcal{L} = \sqrt{-g} \left(\frac{R}{2} + \frac{1}{2} \xi \sigma^2 R - \frac{1}{16} \sigma^4 \right)$$

Hubbard-Stratonovich transf.

- Starobinsky model as a UV completion?

[Y. Ema (2017); Gorbunov, Tokareva (2018)]

$$\mathcal{L} = \sqrt{-g} \left(\frac{1}{2} (1 + \xi_H h^2 + \xi \sigma^2) R - \frac{1}{2} (\partial_\mu h)^2 - \frac{1}{16} \sigma^4 - V(h) \right)$$

$$\rightarrow \mathcal{L} = \sqrt{-g} \left(\frac{1}{2} \xi \hat{\sigma}^2 R - \frac{1}{2} (\partial_\mu h)^2 - \frac{1}{16} \left(\hat{\sigma}^2 - \frac{\xi_H}{\xi} h^2 - \frac{1}{\xi} \right)^2 - V(h) \right)$$

$$\xi \hat{\sigma}^2 = 1 + \xi_H h^2 + \xi \sigma^2$$

“belongs to sigma-field models”

General sigma inflation

Generalize sigma models with linear non-minimal coupling.

$$\mathcal{L}_J = \sqrt{-g} \left[-\frac{1}{2} (1 + \xi_1 \sigma + \xi_0 \sigma^2) \mathcal{R} + \frac{1}{2} (\partial_\mu \sigma)^2 + \frac{1}{2} m_\sigma^2 \sigma^2 - \lambda (\sigma^2 - \vec{\phi}^2)^2 \right]$$

$= \Omega$

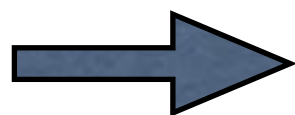
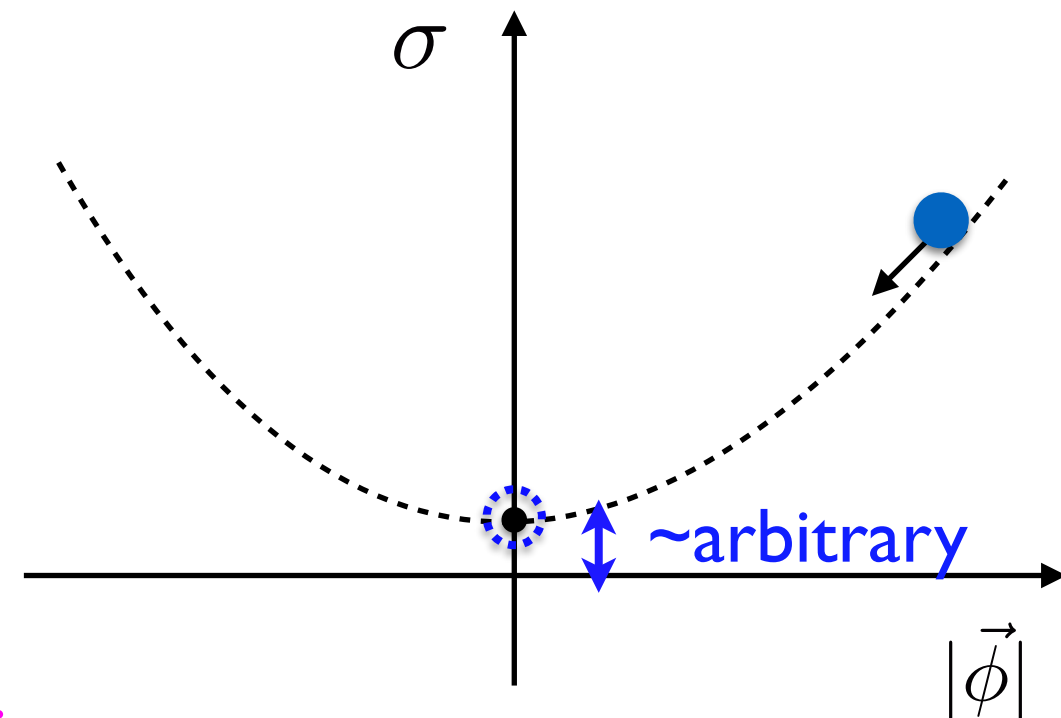
[HML (2018)]

Stable gravity:	$\xi_1^2 < 4\xi_0$
Unitarity:	$\xi_1 \sim \sqrt{\xi_0}$

Large sigma-graviton mixing:

$$\mathcal{L}_J \supset -\frac{1}{2} \xi_1 \sigma \delta \mathcal{R} = -\frac{1}{2} \xi_1 \sigma \square h + \dots$$

$$\mathcal{L}_E \supset \frac{3}{4} \frac{\Omega'^2}{\Omega^2} (\partial_\mu \sigma)^2 = \frac{3}{4} \xi_1^2 (\partial_\mu \sigma)^2 + \dots$$



- 1) Sigma interactions are suppressed.
- 2) Sigma mass parameters can be arbitrarily small.

Effective inflaton potential

Two field dynamics for inflation: $\begin{cases} e^{\frac{2}{\sqrt{6}}\chi} = \xi_1\sigma + \xi_2\sigma^2 + \xi_H\phi^2, \\ \tau = \frac{\phi}{\sigma}. \end{cases}$
 “vacua with stabilized field ratio”

(1) : $\tau = \sqrt{-\frac{\lambda_{\sigma H}}{2\lambda_H}} : \lambda_H > 0, \lambda_{\sigma H} < 0,$

(2) : $\tau = 0 : \lambda_H > 0, \lambda_{\sigma H} > 0,$

(3) : $\tau = \infty : \lambda_H < 0, \lambda_{\sigma H} < 0,$

(4) : $\tau = 0, \infty : \lambda_H < 0, \lambda_{\sigma H} > 0$

$$V_I = \frac{1}{4} \frac{\lambda_H \lambda_\sigma - \lambda_{\sigma H}^2/4}{\lambda_\sigma \xi_H^2 + \lambda_H \xi_2^2 - \lambda_{\sigma H} \xi_H \xi_2} \approx \frac{1}{4\xi_2^2} \left(\lambda_\sigma - \frac{\lambda_{\sigma H}^2}{4\lambda_H} \right),$$

$$V_I = \frac{\lambda_\sigma}{4\xi_2^2}$$

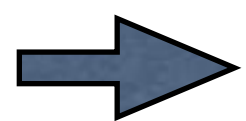
$$V_I = \frac{\lambda_H}{4\xi_H^2}, \quad \times$$

$$V_I = \frac{\lambda_\sigma}{4\xi_2^2} \quad \text{or} \quad \frac{\lambda_H}{4\xi_H^2},$$

← Unstable Higgs vacuum

\times

$\xi_2 \gg \xi_H = \mathcal{O}(1)$ assumed.



$\chi \gg 1 :$

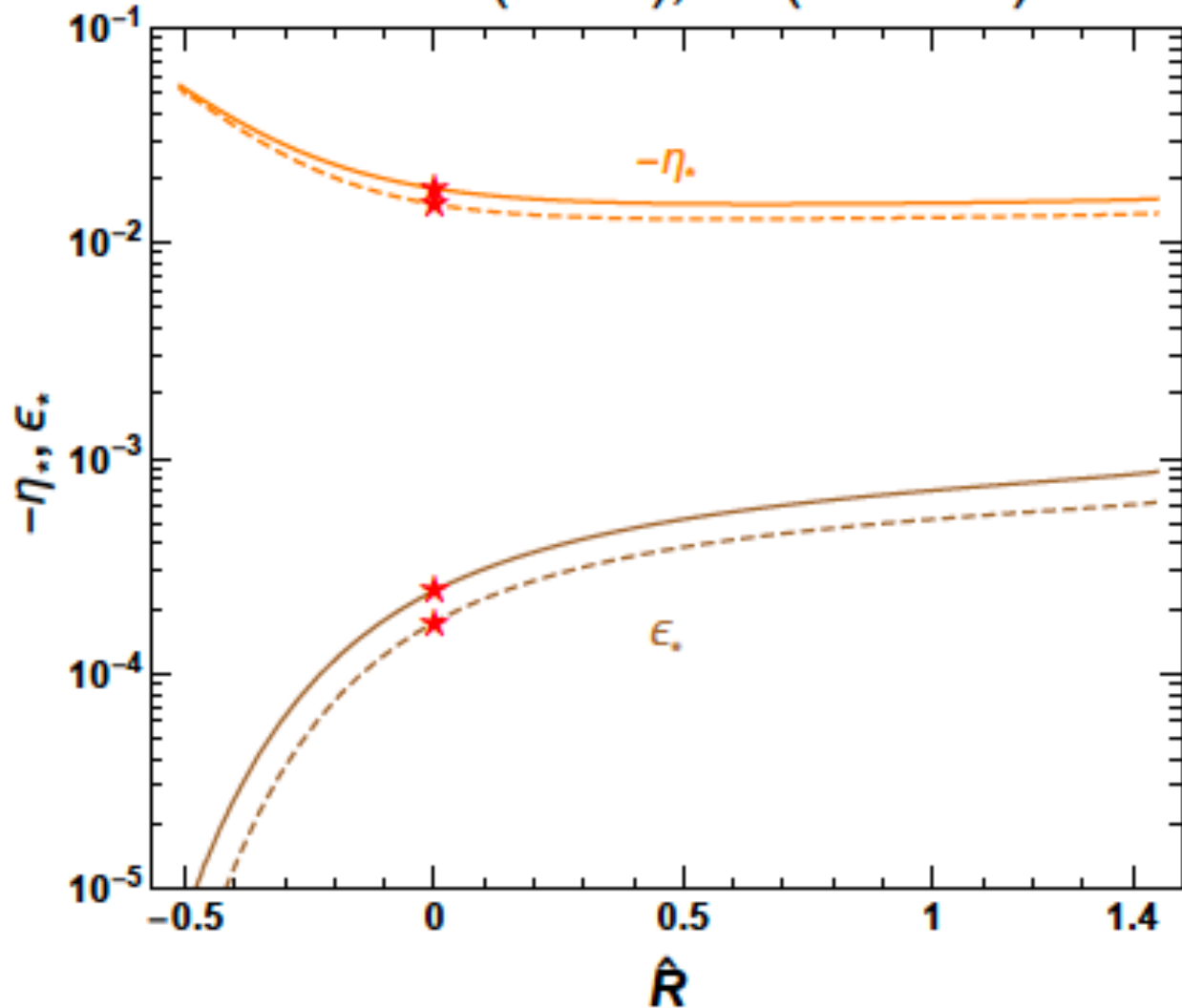
Higgs-sigma mixed or pure sigma inflation.

$$\frac{\mathcal{L}_E}{\sqrt{-g_E}} = -\frac{1}{2}R(g_E) + \frac{1}{2}(\partial_\mu\chi)^2 - V_I(\tau) \left(1 - 2\hat{R}e^{-\frac{1}{\sqrt{6}}\chi} - 2(1 - \hat{R}^2)e^{-\frac{2}{\sqrt{6}}\chi} \right).$$

Inflaton = radial component: $m_\tau \sim \sqrt{\xi_2 V_I} \gg m_\chi \sim \sqrt{|\eta| V_I}$

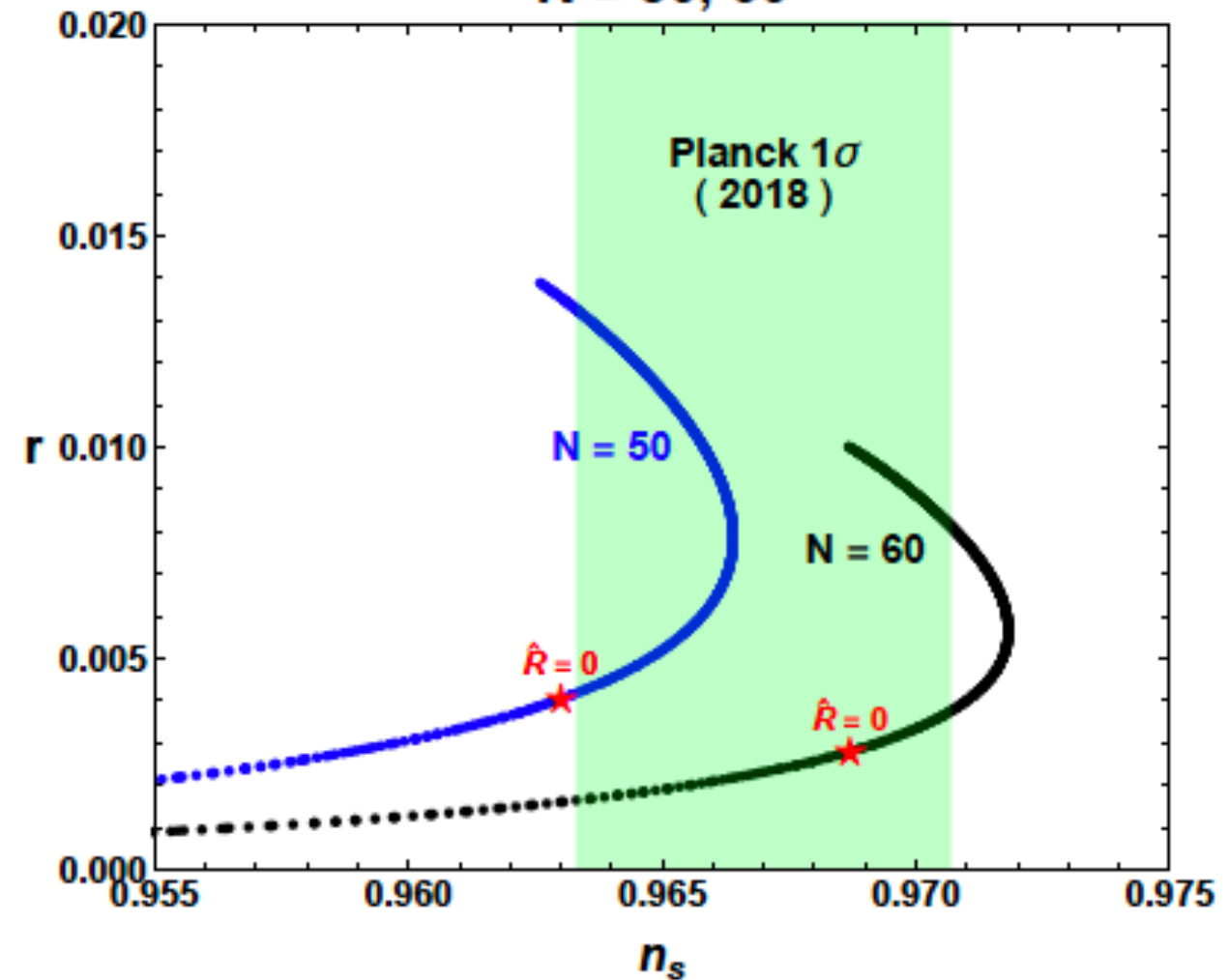
Tensor mode scales up!

N = 50 (Solid), 60 (Dashed)



$$\hat{R} \equiv \xi_1 / (\xi_2 + \xi_H \tau^2)^{1/2}$$

N = 50, 60



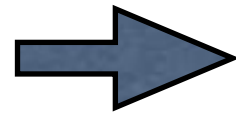
★ Higgs inflation

The higher unitarity scale, the more deviation up to $r=0.01$.

Tensor-to-scalar ratio testable at future CMB experiments.

Inflaton dark matter

Approximate Z_2



Sigma inflaton = dark matter

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2}\Omega(\sigma, H)R + \frac{1}{2}(\partial_\mu\sigma)^2 + |D_\mu H|^2 - V(\sigma, H)$$

Z_2 symmetric in particle physics:

$$V(\sigma, H) = V_0 + \frac{1}{2}m_\sigma^2\sigma^2 + \frac{1}{4}\lambda_\sigma\sigma^4 + \frac{1}{2}\lambda_{\sigma H}\sigma^2|H|^2 + m_H^2|H|^2 + \lambda_H|H|^4.$$

Z_2 broken in gravity: $\Omega(\sigma, H) = 1 + \boxed{\xi_1\sigma} + \xi_2\sigma^2 + 2\xi_H|H|^2,$

Inflaton decays only by the trace of EM tensor:

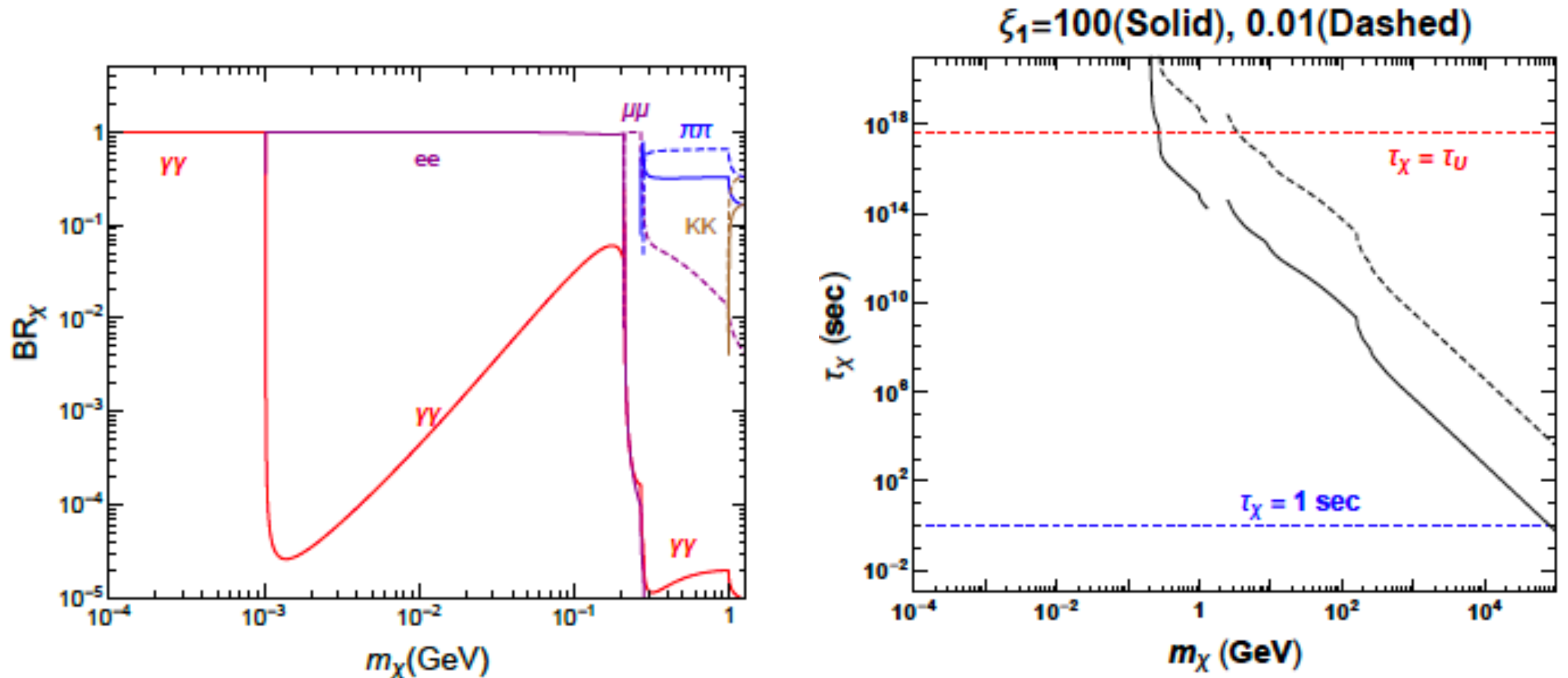
$$\mathcal{L}_\sigma = \frac{1}{2}\xi_1\sigma T_\mu^\mu \approx \frac{1}{2}\frac{\xi_1}{\sqrt{1 + \frac{3}{2}\xi_1^2}}\frac{\chi}{M_P} T_\mu^\mu,$$

[Ibarra et al (2016);
Choi, Kang, HML, Yamashita (2019)]

$$T_\mu^\mu = -(\partial_\mu\phi)^2 + 4V + \frac{m_f}{v}\phi\bar{f}f - \delta_V\frac{m_V^2}{v^2}\phi^2 V_\mu V^\mu + \delta T_\mu^\mu,$$

massless particles: $\delta T_\mu^\mu = \frac{\beta_S(\alpha_S)}{4\alpha_S} G_{\mu\nu}^a G^{a\mu\nu} + \frac{\beta_{EM}(\alpha)}{4\alpha} F_{\mu\nu} F^{\mu\nu} + \dots$

Long-lived inflaton



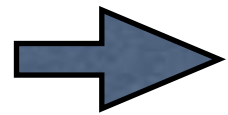
[Ibarra et al (2016, 2017); Choi, Kang, HML, Yamashita (2019)]

Inflaton can live longer than age of Universe for $m_\chi \lesssim 2m_\pi = 270$ MeV.

No CMB bound on inflaton for $m_\chi \lesssim 2$ MeV.

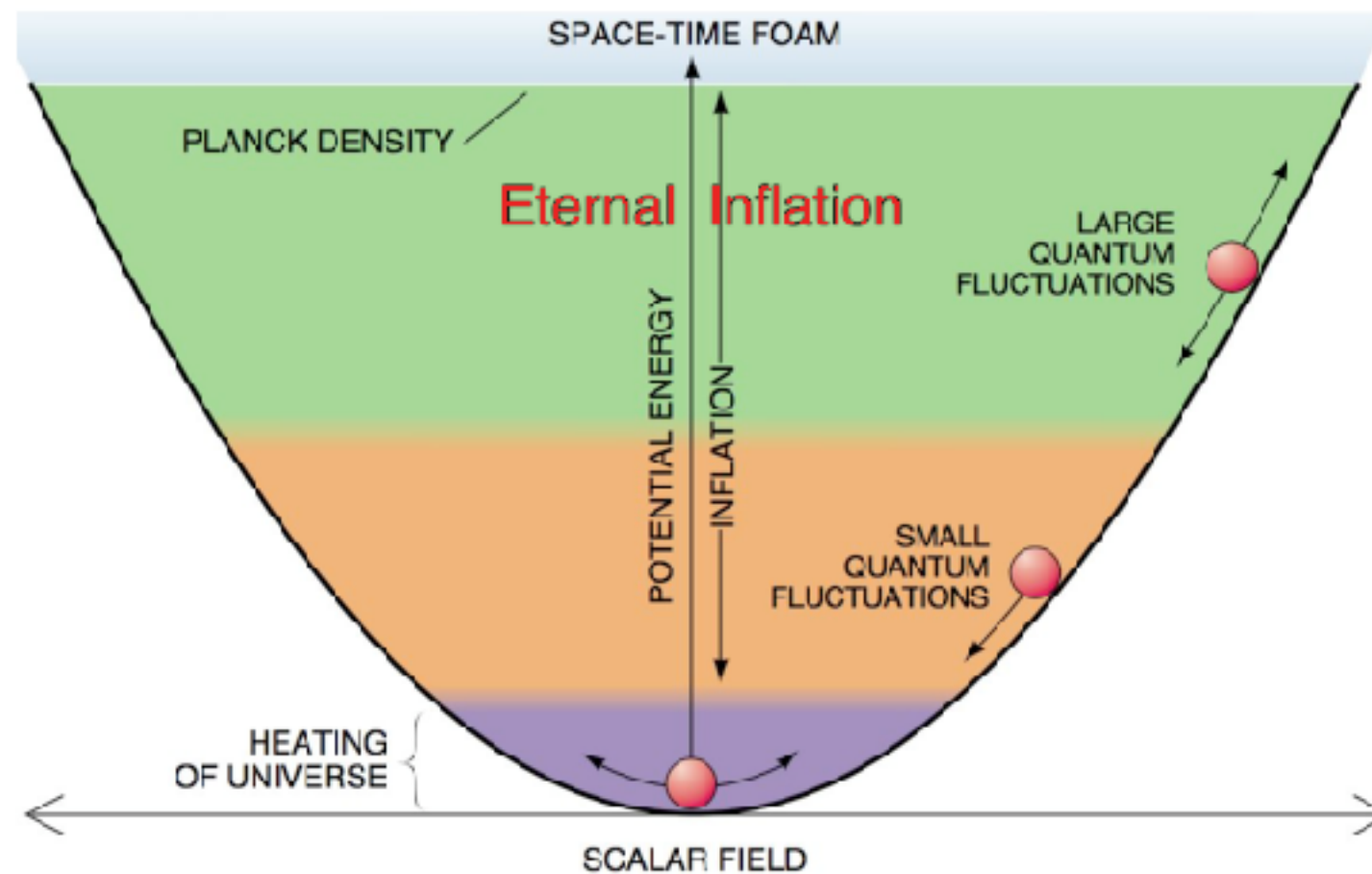
Reheating

- After inflation, the Universe is almost at zero temperature.



Reheating mechanism is required!

$$V(\phi) = \frac{m^2}{2}\phi^2$$



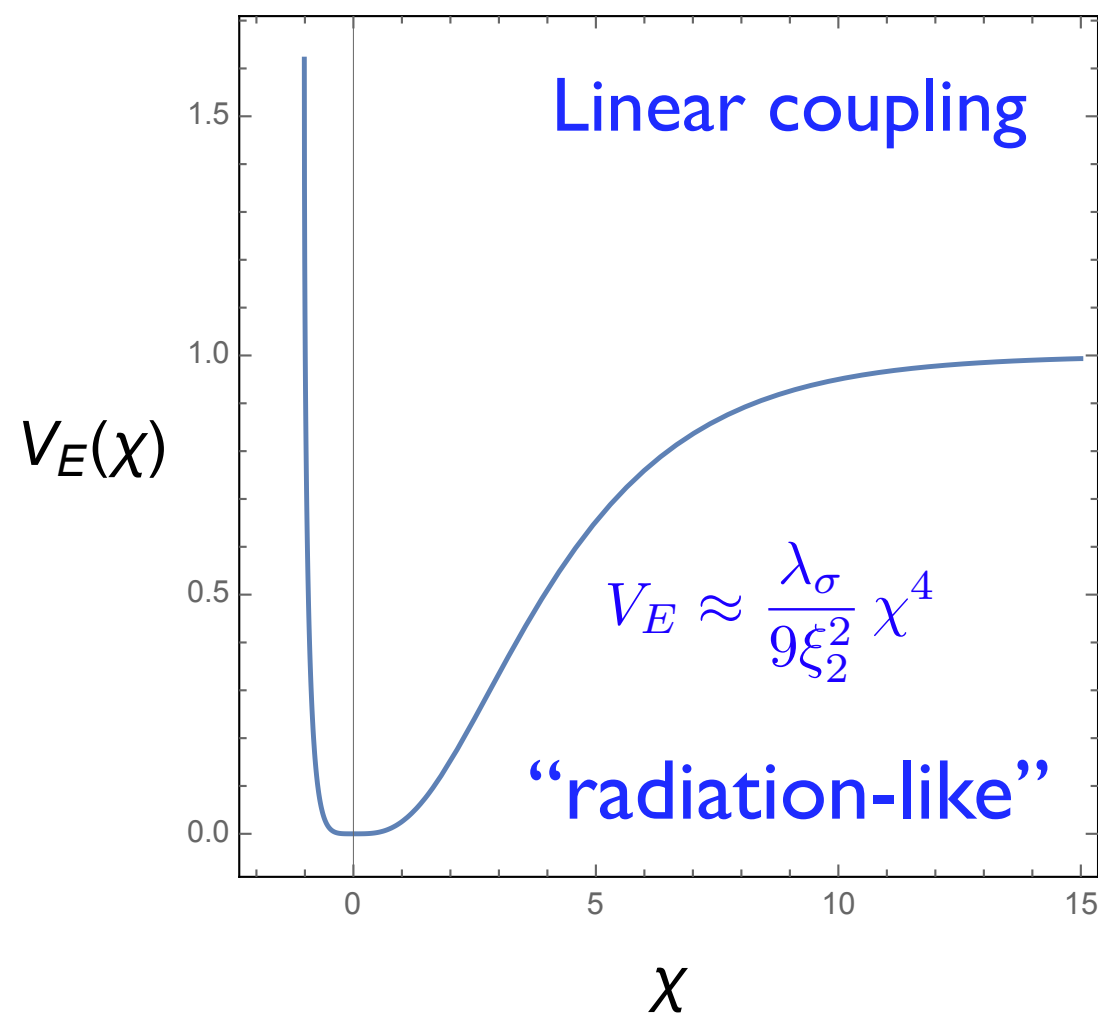
Reheating from sigma field

“Quartic potential” during reheating

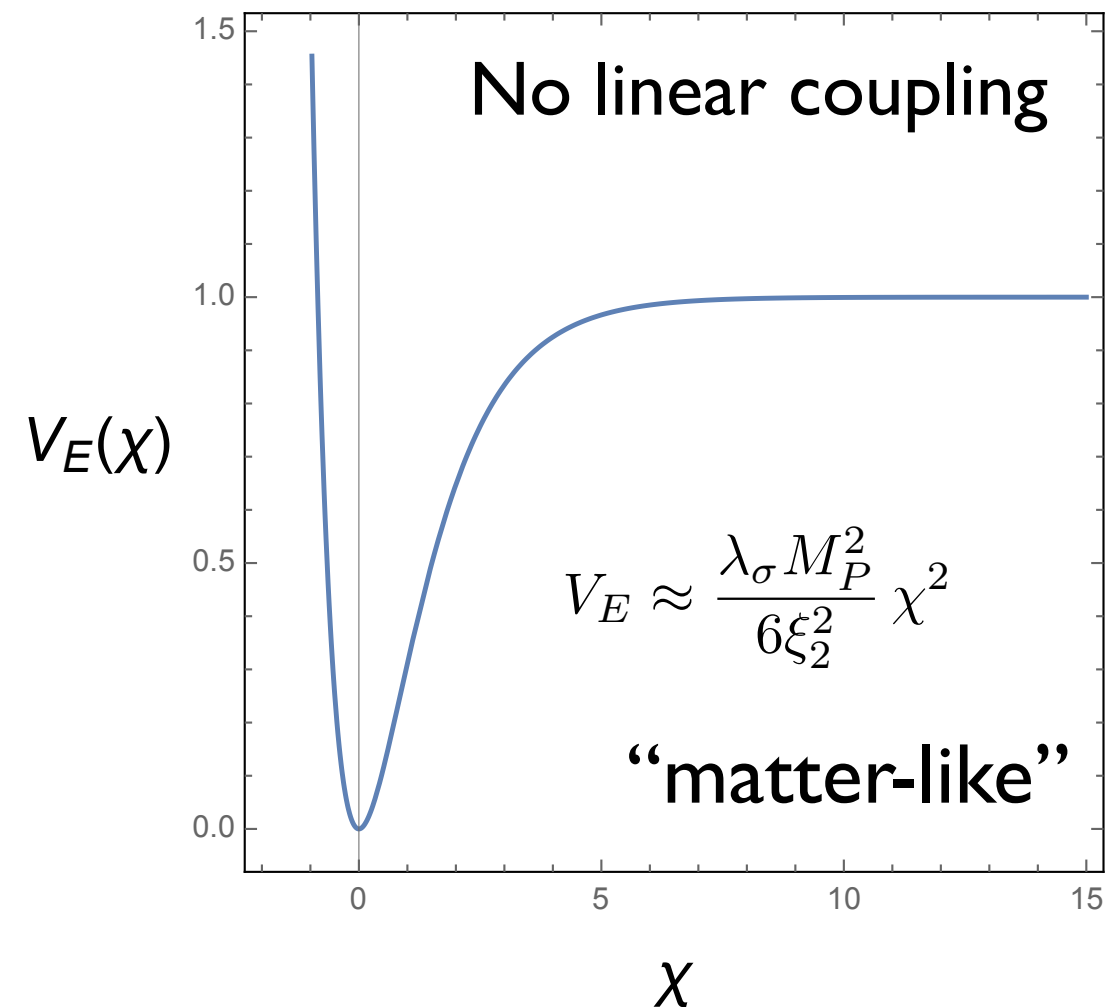
$$\chi \approx \sqrt{\frac{3}{2}} \ln \Omega = \sqrt{\frac{3}{2}} \ln(1 + \xi_1 \sigma + \xi_2 \sigma^2) \quad [\text{Choi, Kang, HML, Yamashita (2019)}]$$

$$\chi \lesssim 1: \quad V_E \approx \frac{\lambda_\chi}{4} \chi^4, \quad \lambda_\chi \equiv \frac{4\lambda_\sigma}{9\xi_2^2} = (5.3 \times 10^{-10}) R^{-4} \left(\frac{r}{0.01} \right)$$

R=1.5



R=0



Inflaton condensate

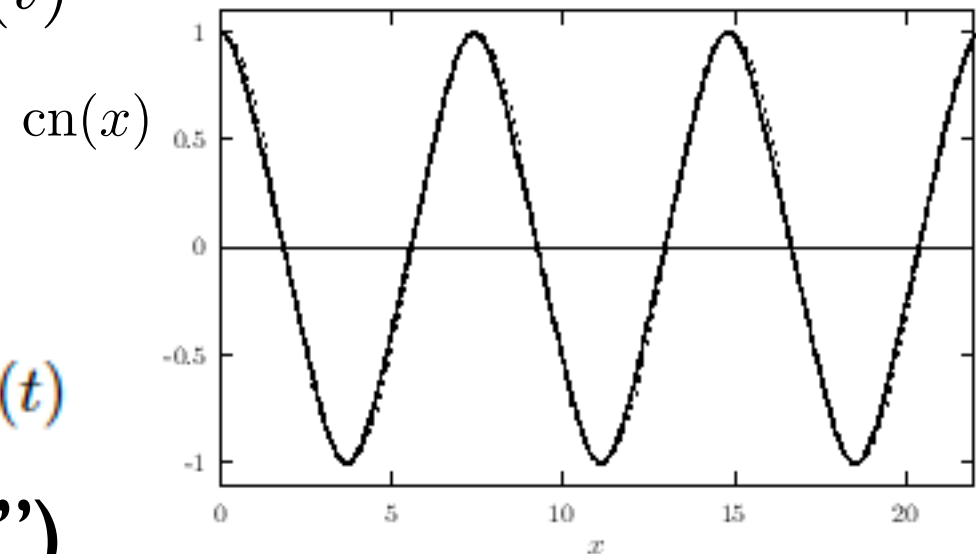
Inflaton condensate:

[P. Green et al, 1997; Tenkanen, 2016; Choi, Kang, HML, Yamashita (2019)]

$$H^2 = \frac{\rho_{\chi_c}(t)}{3M_P^2} = \left(\frac{1}{2t}\right)^2, \quad \rho_{\chi_c} = \frac{1}{4}\lambda_\chi \chi_c^4(t)$$

➔ $\chi_c(t) = \chi_0(t) \operatorname{cn}\left(\omega(t)t, \frac{1}{\sqrt{2}}\right),$

$$\chi_0 = \chi_{\text{end}} \sqrt{t_{\text{end}}/t} \quad \omega(t) = 0.85 \lambda_\chi^{1/2} \chi_0(t)$$



1) Jacobi cosine form (“unharmonic”)

2) Amplitude decreases due to expansion.

cf. matter-like: constant freq. $\chi_c(t) = \chi_0(t) \cos(mt), \quad H = \frac{2}{3t}.$

Particle production or decay from inflaton reheat!

“Preheating”

“Perturbative reheating”

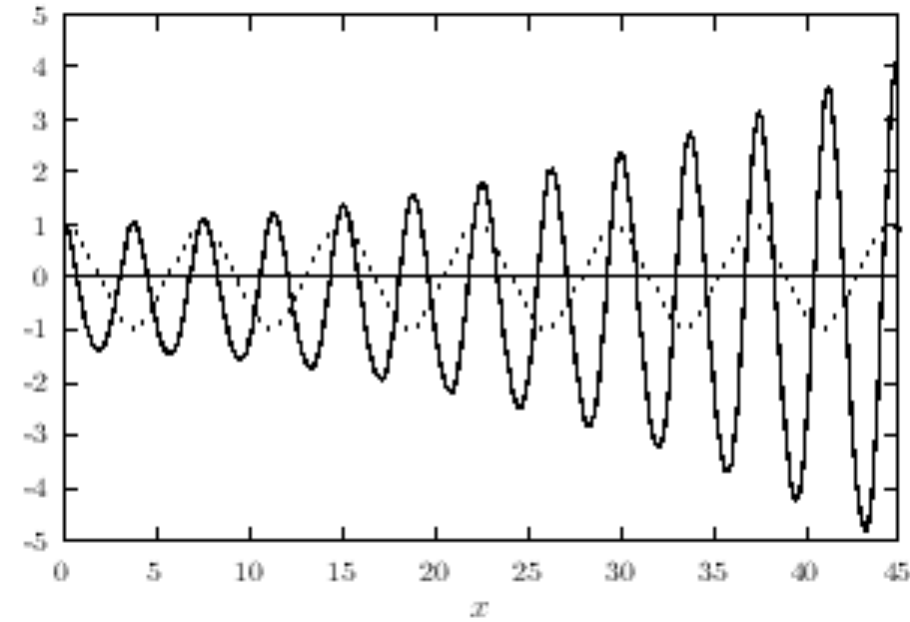
Preheating

Lame equations for Higgs perturbation

$$H_k(t) = a(t)h_k(t) : \quad [\text{P. Green et al, 1997}] \quad H_k$$

$$H_k'' + \left(\kappa^2 + \frac{\lambda_{\chi H}}{2\lambda_{\chi}} \text{cn}^2\left(x, \frac{1}{\sqrt{2}}\right) \right) H_k = 0$$

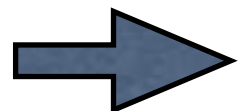
$$\kappa^2 \equiv \frac{k^2}{\lambda_{\chi} \chi_0^2 a(t)^2} \quad \text{k: comoving momentum.}$$



Growth of particle # with Higgs energy, $\omega_k^2 = \kappa^2 + \frac{\lambda_{\chi H}}{2\lambda_{\chi}} \text{cn}^2\left(x, \frac{1}{\sqrt{2}}\right)$,

$$n_k = \frac{\omega_k}{2} \left(|H_k|^2 + \frac{|\dot{H}_k|^2}{\omega_k^2} \right) - \frac{1}{2} \quad \longrightarrow \quad n_k \sim e^{\mu_k x}, \quad x = (48\lambda_{\chi})^{1/5} \sqrt{t}.$$

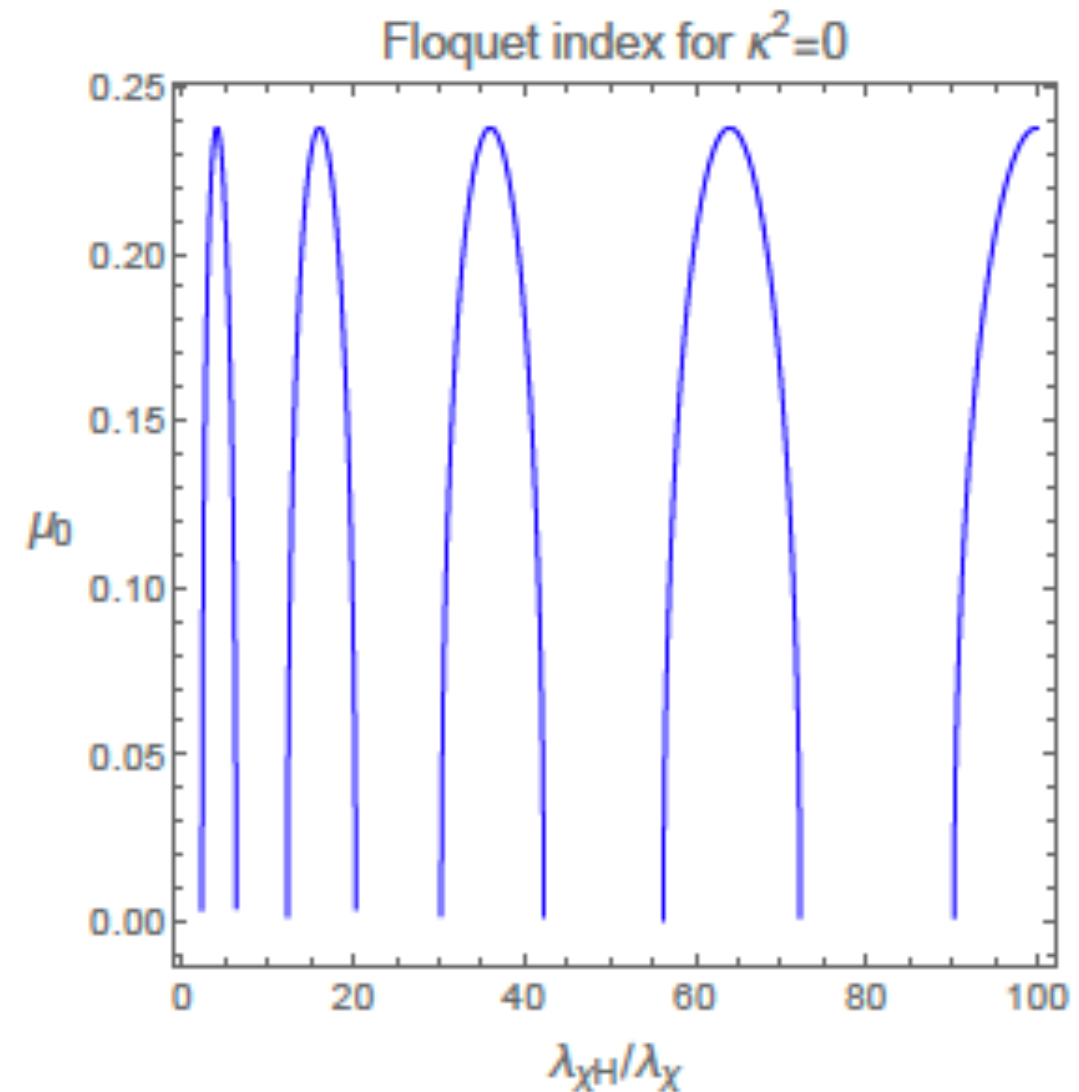
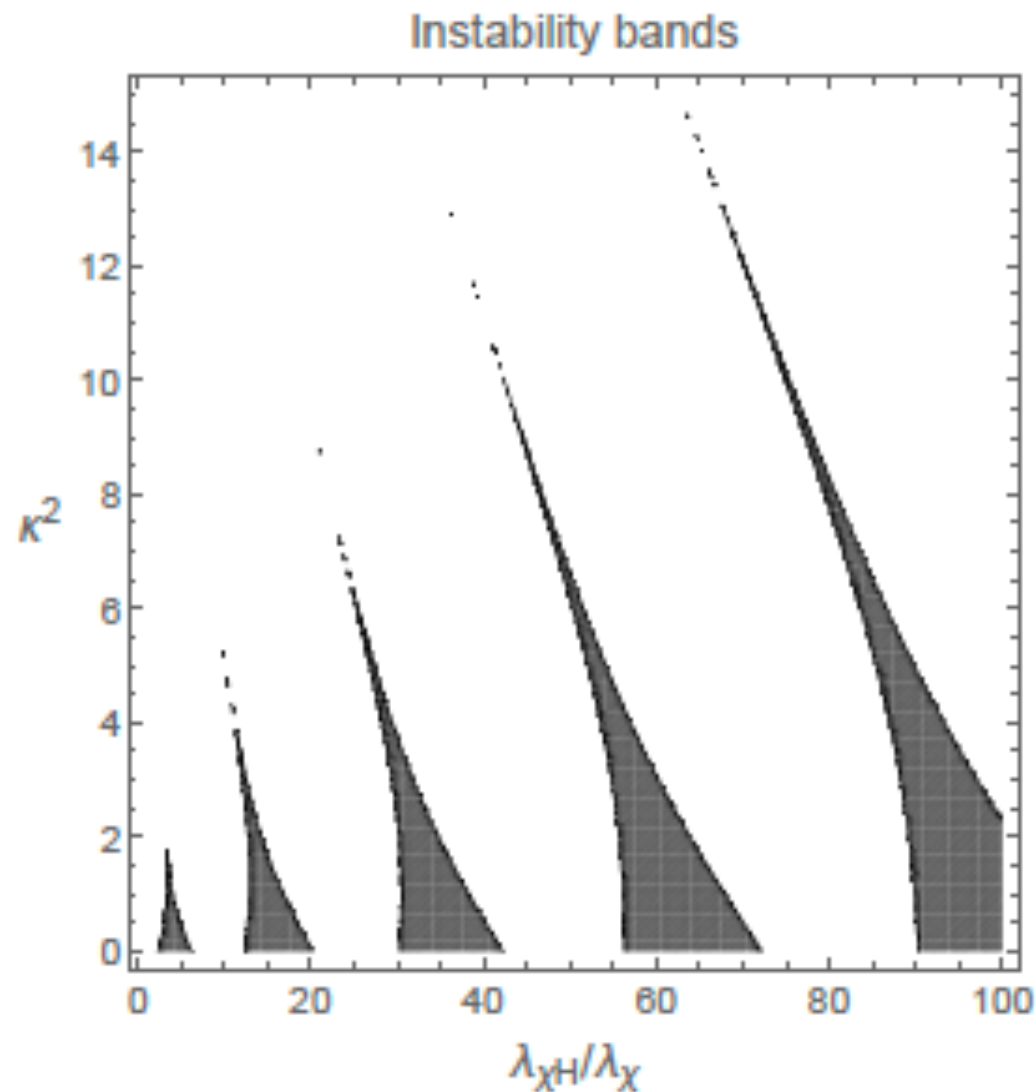
Preheating condition: $\frac{\dot{n}_k}{n_k} \sim 2\mu_k \dot{x} \gtrsim \Gamma_{\chi e} \approx \Gamma_{\chi e \rightarrow hh}$



$$\mu_k \gtrsim 2 \times 10^{-7} \left(\frac{\lambda_{\chi H}}{10^{-7}} \right)^2 \left(\frac{10^{-10}}{\lambda_{\chi}} \right)$$

[Choi, Kang, HML, Yamashita (2019v2, to appear)]

Preheating



Zero momentum: Broad resonance is efficient. High reheating!

Large momentum: Narrow resonance “Redshifted away”

Inefficient preheating \rightarrow perturbative reheating!

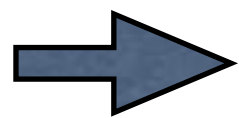
Dark matter from reheating

Reheating temperature:

[Choi, Kang, HML, Yamashita (2019)]

$$\Gamma_{\chi_c \rightarrow \chi\chi} = 0.023 \lambda_\chi^{3/2} \chi_0, \quad \Gamma_{\chi_c \rightarrow hh} = 0.002 \lambda_{\chi H}^2 \lambda_\chi^{-1/2} \chi_0. \quad \text{BR} = \frac{\Gamma_{\chi_c \rightarrow \chi\chi}}{\Gamma_{\chi_c \rightarrow \chi\chi} + \Gamma_{\chi_c \rightarrow hh}}$$

$$\Gamma_{\chi_c} = \Gamma_{\chi_c \rightarrow hh} \cdot \left(\frac{1}{1 - \text{BR}} \right) \simeq H_{\text{dec}} = \sqrt{\frac{\lambda_\chi}{12}} \frac{\chi_0^2(t_{\text{dec}})}{M_P}; \quad \frac{\pi^2 g_*(T_{\text{RH}})}{30} T_{\text{RH}}^4 = (1 - \text{BR}) \cdot \rho_{\chi_c}(t_{\text{dec}})$$



$$T_{\text{RH}} = (4.4 \times 10^6 \text{ GeV}) \left(\frac{100}{g_*(T_{\text{RH}})} \right)^{1/4} \left(\frac{\lambda_{\chi H}}{10^{-8}} \right)^2 R^3 (1 - \text{BR})^{-3/4} \left(\frac{r}{0.01} \right)^{-3/4}$$

Dark matter abundance: $\lambda_{\chi H} \sim \lambda_{\sigma H} / \xi_1^2 \lesssim 10^{-7}$ out of equilibrium

$$\Omega_\chi h^2 = (\Omega_\chi h^2)_{\text{FIMP}} + (\Omega_\chi h^2)_{\text{RH}} : \text{non-thermal production}$$

$$\text{Higgs decay: } (\Omega_\chi h^2)_{\text{FIMP}} = 0.12 \left(\frac{100}{g_*(m_h)} \right)^{3/2} \left(\frac{\lambda_{\chi H}}{4.4 \times 10^{-7}} \right)^2 \left(\frac{m_\chi}{1 \text{ eV}} \right)$$

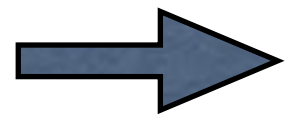
$$\text{Inflaton decay: } (\Omega_\chi h^2)_{\text{RH}} = 7.3 R \left(\frac{r}{0.01} \right)^{-1/4} \cdot \text{BR} \cdot \left(\frac{m_\chi}{1 \text{ eV}} \right)$$

DM = Dark radiation

Dark matter relativistic at production: “Dark Radiation”

DM becomes non-relativistic if $\frac{a_{\text{dec}}}{a_{\text{NR}}} \sim \frac{m_\chi}{k} \sim \frac{m_\chi}{\sqrt{3\lambda_\chi \chi_0(t_{\text{dec}})}} :$

$$\begin{aligned} \frac{T_{\text{NR}}}{T_{\text{eq}}} &= 0.77 \lambda_\chi^{-1/4} \left(\frac{m_\chi}{1 \text{ eV}} \right) \\ &= 160 R \left(\frac{r}{0.01} \right)^{-1/4} \left(\frac{m_\chi}{1 \text{ eV}} \right) \end{aligned}$$



$$m_\chi > 7.8 \text{ keV}$$

$$T_{\text{NR}} > T_{\text{BBN}}$$

before BBN

If DM remains relativistic during BBN,

Dark radiation:

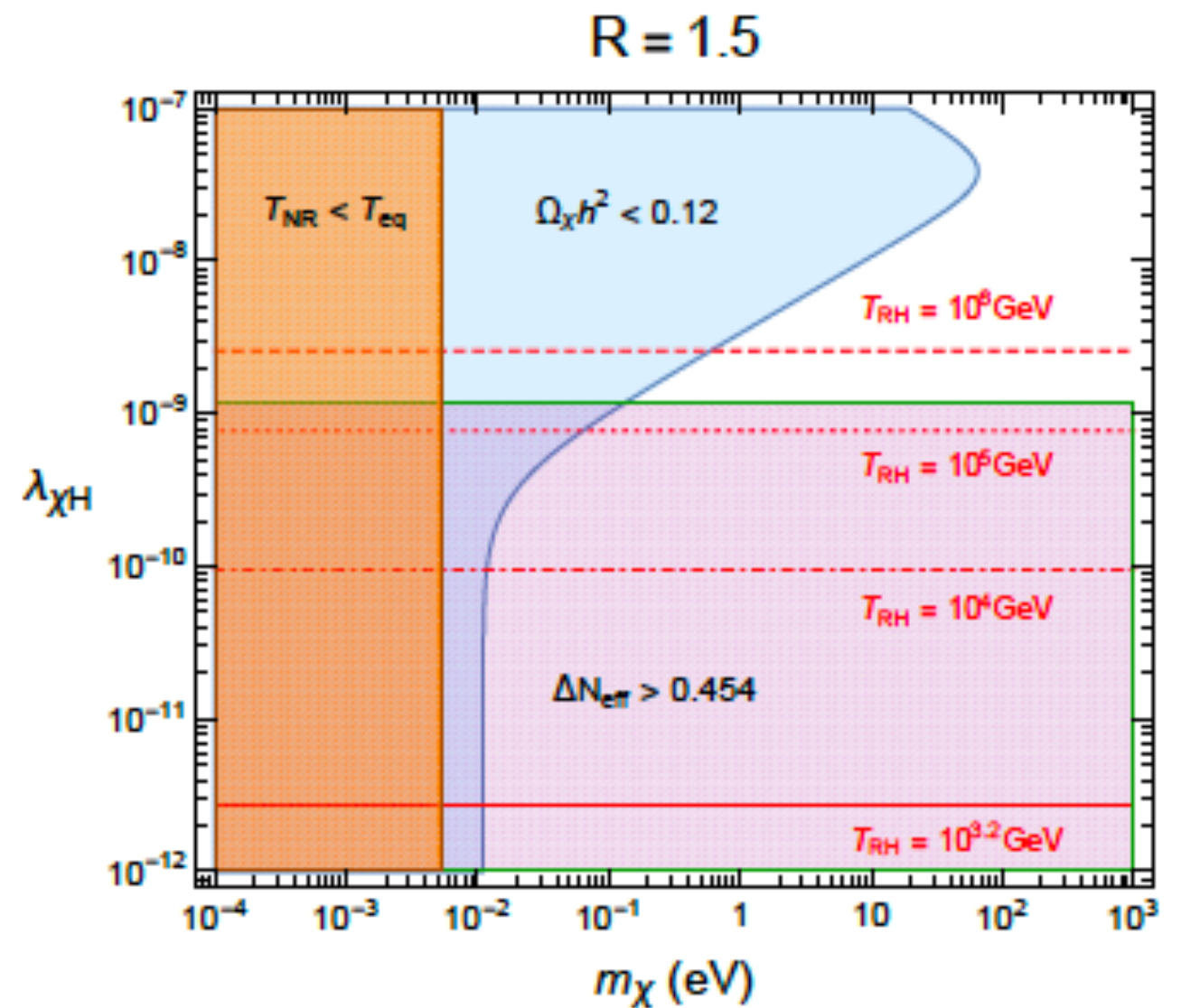
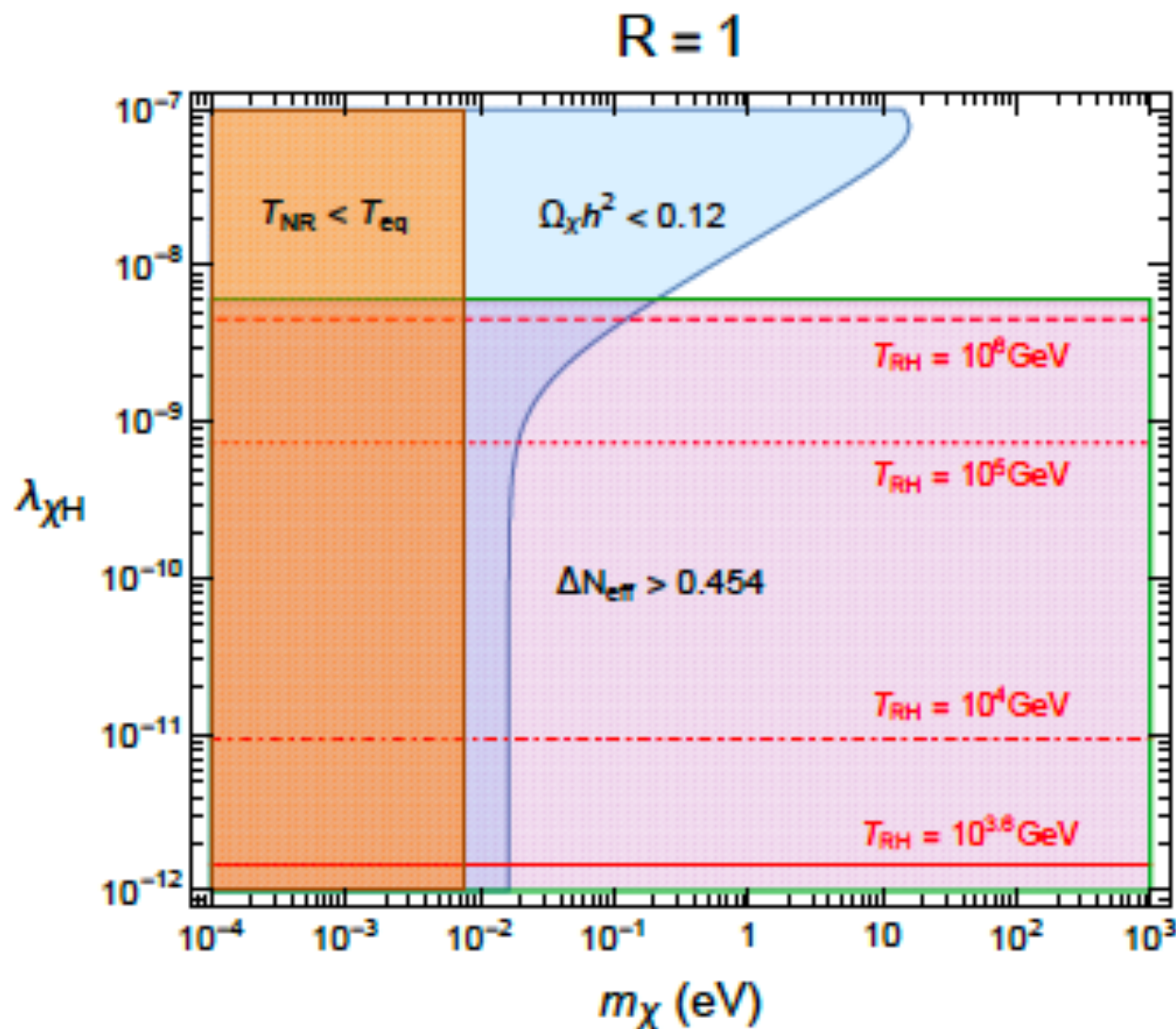
$$\begin{aligned} \Delta N_{\text{eff}} &= \frac{4}{7} \left(\frac{11}{4} \right)^{4/3} g_* \cdot \frac{\rho_\chi(a_{\text{eq}})}{\rho_R(a_{\text{eq}})} \cdot \left(\frac{a_{\text{NR}}}{a_{\text{eq}}} \right) \\ &\leq 0.0944 R^{-1} \left(\frac{r}{0.01} \right)^{1/4} \left(\frac{1 \text{ eV}}{m_\chi} \right) \end{aligned}$$

- (a) $N_{\text{eff}} = 2.93^{+0.23}_{-0.23}$
 - (b) $N_{\text{eff}} = 3.04^{+0.22}_{-0.22}$
 - (c) $N_{\text{eff}} = 3.06^{+0.22}_{-0.22}$
- 95 %, *Planck* TT,TE,EE
+lowE+BAO+Aver (2015)
+Peimbert (2016)
+Cooke (2018).

$$\text{case c) } m_\chi \gtrsim 0.208(0.139) \text{ eV within } 2\sigma$$

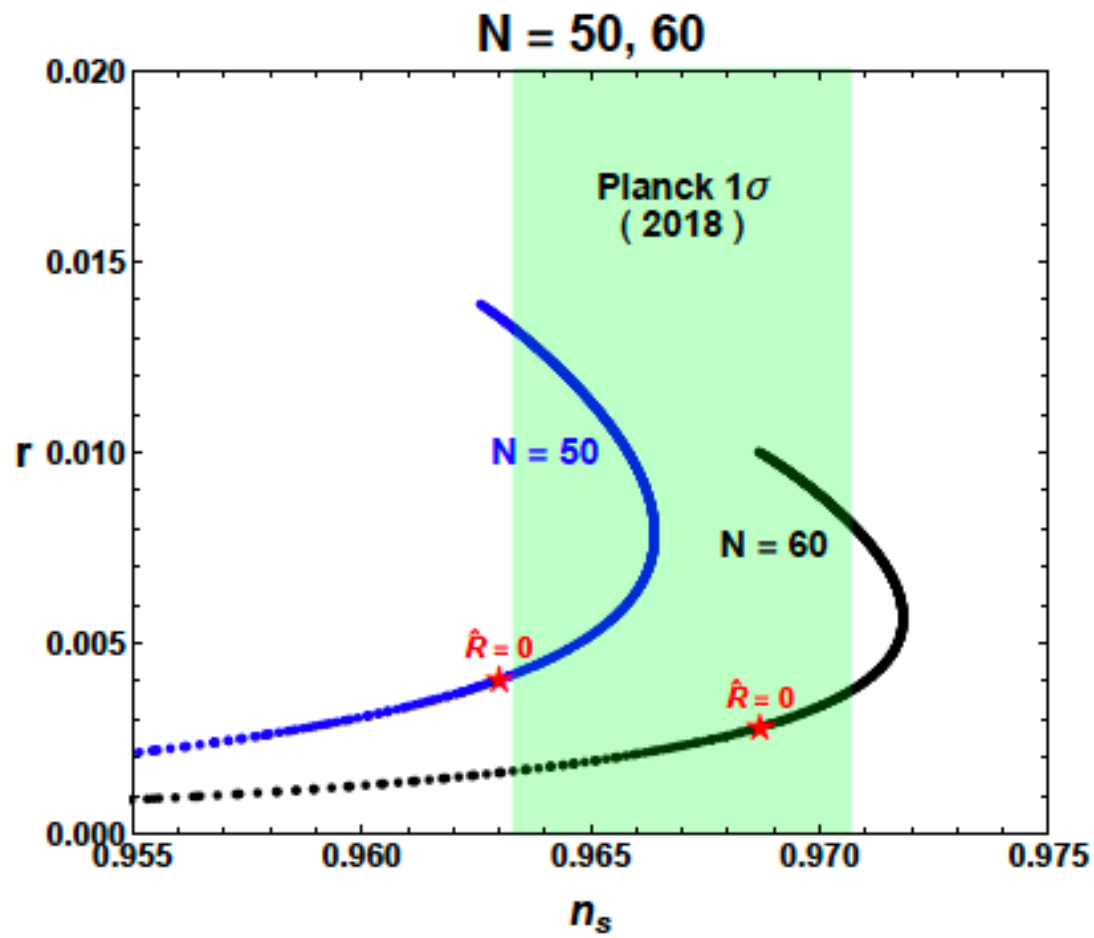
Inflaton dark matter

[Choi, Kang, HML, Yamashita (2019)]

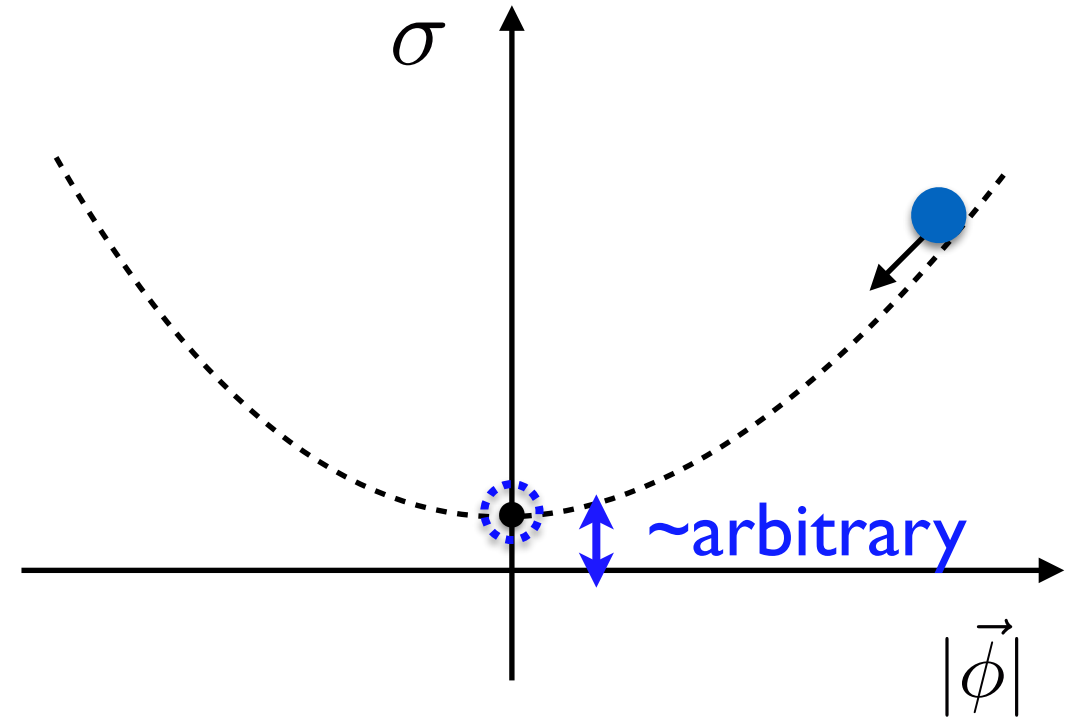


Blue: relic density, Purple: BBN, Orange: $T_{NR} < T_{eq}$

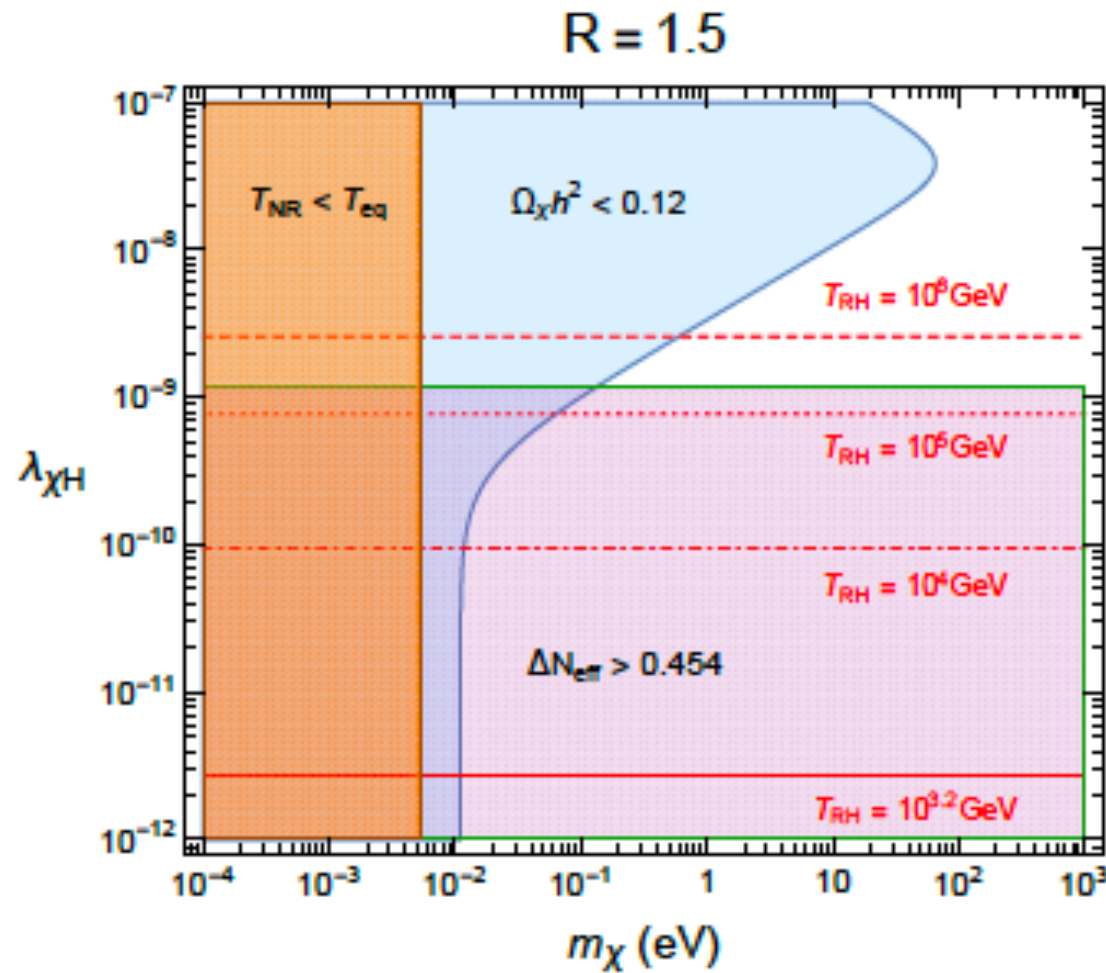
DM masses in the range of $0.1 \text{ eV} \lesssim m_\chi \lesssim 100 \text{ eV}$.



Inflation



Unitarity



Dark matter/radiation

Conclusions

- A general form of sigma models to unitarize Higgs inflation was proposed, covering various scalar-tensor theories valid below Planck scale.
- Large linear non-minimal coupling leads to sizable deviation in tensor mode up to $r=0.01$, novel reheating and small inflaton masses/parameters.
- Inflaton has suppressed couplings to the SM through the trace of energy-momentum tensor and small Higgs-portal coupling.
- Inflation is long-lived, becoming a viable candidate for decaying dark matter and dark radiation.