

1 Studies of three-particle correlations and reaction-plane correla- 2 tors from STAR

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5

6 **Abstract.** We present STAR measurements of various harmonics of three-particle corre-
7 lations in $\sqrt{s_{NN}} = 200$ GeV Au+Au collisions at RHIC. The quantity $\langle \cos(m\phi_1 + n\phi_2 -$
8 $(m + n)\phi_3) \rangle$ is measured for inclusive charged particles for different harmonics m and n
9 as a function of collision centrality, transverse momentum p_T and relative pseudorapid-
10 ity $\Delta\eta$. These observables provide detailed information on global event properties like
11 correlations between event planes of different harmonics and are particularly sensitive
12 to the expansion dynamics of the matter produced in the collisions. We compare our
13 measurements to different viscous hydrodynamic models. We argue that these measure-
14 ments probe the three dimensional structure of the initial state and provide unique ways
15 to constrain the transport parameters involved in hydrodynamic modeling of heavy-ion
16 collisions.

17 1 Introduction

18 By now it has been established that relativistic heavy-ion collisions produce a strongly correlated
19 Quark Gluon Plasma (sQGP). Recent experimental studies have focused on studying the properties of
20 such sQGP. One of the striking properties of such a phase of matter is that it exhibits nearly perfect
21 fluidity characterized by the smallest viscosity-to-entropy-density ratio η/s amongst all known fluids
22 in the nature. Over the past years, combined insights from both experiment through measurements
23 of anisotropic flow coefficients v_n and from theory through viscous hydrodynamic simulations, have
24 made precise extraction of η/s possible. However a very intrinsic characteristic about such transport
25 parameter, i.e. its temperature dependence is not yet fully constrained by experimental measurements.
26 A primary goal of the current measurements at RHIC is therefore to go beyond conventional measure-
27 ments of flow coefficients and provide new observables that can be useful to constrain $\eta/s(T)$.

28 In this work we present the measurements of three particle correlations from the STAR experi-
29 ment using the observable $C_{m,n,m+n} = \langle \langle \cos(m\phi_1 + n\phi_2 - (m + n)\phi_3) \rangle \rangle$, where m, n defines the har-
30 monic coefficients and $\phi_{1,2,3}$, the azimuthal angles of three particles [1]. The inner and the outer
31 averages are taken over all triplets and events respectively. The observable $C_{m,n,m+n}$ can be ap-
32 proximated as correlations of flow harmonics, v_n , and corresponding event plane angles, Ψ_n s, as
33 $\langle v_m v_n v_{m+n} \cos(m\Psi_m + n\Psi_n - (m + n)\Psi_{m+n}) \rangle$. Theoretical studies show that such an observable can
34 probe non-linear hydrodynamic response and therefore become more sensitive to viscosity than in-
35 dividual flow harmonics v_n [1–10]. Better sensitivity to viscous effects can be very useful towards

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36 more precise extraction of different transport parameters and possibly their temperature dependence
 37 by comparison to hydrodynamic simulations [11, 12]. Measurements of event plane and flow har-
 38 monic correlations have been performed at LHC by ATLAS collaboration [13] and recently by ALICE
 39 collaboration[14]. However measurements at a single energy is not sufficient to constrain $\eta/s(T)$.
 40 LHC measurements are sensitive to the η/s at higher temperatures, meanwhile full constraint on
 41 $\eta/s(T)$ can only be achieved with complementary measurements of $C_{m,n,m+n}$ at RHIC [11, 12, 15, 16].
 42 In fact, measurements over the entire range of energy available under the Beam Energy Scan (BES)
 43 program at RHIC will be most preferable in this context. Measurements at RHIC have additional
 44 advantages. Since the beam rapidity is smaller one expects stronger variation of initial geometry,
 45 fluctuations, energy density, temperature, baryon density etc. over a relatively smaller window of
 46 rapidity as compared to LHC. In this context, measurements of $C_{m,n,m+n}$ on the pseudorapidity separation
 47 between particles may allow us to study the breaking of longitudinal invariance, three dimension
 48 structure of the initial state [3, 17–20] over relatively smaller window of acceptance available for mea-
 49 surements at RHIC than LHC. In addition to constraining initial state and transport parameters, the
 50 charge dependence of three particle correlation can be used to search for the signals of the chiral
 51 magnetic effect (CME) [21–24]. In this work we will not study such charge dependence, however, we
 52 expect that the results presented here for inclusive charged particles will provide important baseline
 53 for CME measurements.

54 2 Experiment and analysis

55 We analyze the data on Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV collected by the STAR detector [25]
 56 during 2011 year running of RHIC. For the measurements of $C_{m,n,m+n}$ we use charged particles within
 57 the pseudorapidity range of $|\eta| < 1$ and transverse momentum of $p_T > 0.2$ GeV/c detected by the
 58 Time Projection Chamber (TPC), the primary tracking systems of STAR situated inside a 0.5 Tesla
 59 solenoidal magnetic field [26]. We use algebra based on Q-vectors and in order to account for imper-
 60 fections in the detector acceptance we apply track-by-track weights [27, 28]. We also apply momen-
 61 tum dependent tracking efficiency. In such estimation, we correct for the track-merging artifacts by
 62 measuring the relative pseudo rapidity separation between any two tracks and correcting for missing
 63 pairs apparent at $\Delta\eta \approx 0$. We estimate systematic uncertainties in our measurements by analyzing
 64 datasets of different time periods, from different years, with different tracking algorithms, with differ-
 65 ent efficiency estimates, by varying z-vertex position of the collision, and by varying track selection
 66 criteria. In addition we also quantify the effects of short-range quantum and Coulomb correlations
 67 in the systematic uncertainties by studying $\Delta\eta$ dependence of $C_{m,n,m+n}$. Finally for data-model com-
 68 parison we estimate the number of participant nucleons N_{part} using a Monte-Carlo Glauber model for
 69 different centrality intervals (0 – 5%, 5 – 10%, 10 – 20%, ..., 70 – 80%) used in this analysis [29, 30].
 70 For selection of such centrality bins we use the distribution of minimum bias uncorrected multiplicity
 71 of charged particles in the pseudorapidity region $|\eta| < 0.5$ measured by the TPC.

72 3 Results and discussion

73 In this conference proceedings we present results for correlators $C_{1,1,2}, C_{1,2,3}, C_{2,2,4}, C_{2,3,5}$. We first
 74 present differential measurements such as $\Delta\eta$ and p_T dependence of these correlators, the goal of such
 75 study is to understand how different physical scenarios effect these observables. We later on present
 76 integrated measurements i.e. the centrality dependence of $C_{m,n,m+n}$ and make comparisons to viscous
 77 hydrodynamic model calculations with different assumptions of $\eta/s(T)$.

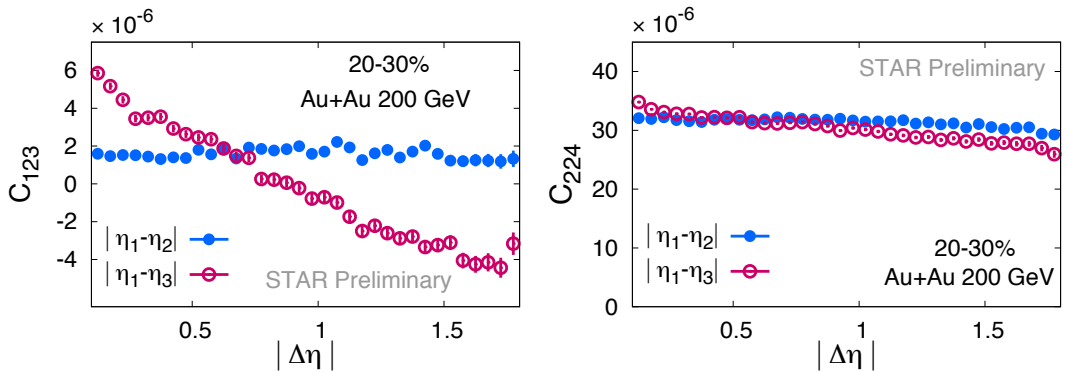


Figure 1. Relative pseudo rapidity dependence of the three particle correlator $C_{1,2,3}$ and $C_{2,2,4}$.

78 3.1 $\Delta\eta$ dependence

79 In Fig. 1 we show the $\Delta\eta$ dependence of $C_{1,2,3}$ and $C_{2,2,4}$. A similar measurement for $C_{1,1,2}$ was
80 previously presented by STAR in Ref [22]¹. One can clearly see in Fig. 1(left) that $C_{1,2,3}$ correlator
81 shows a very strong dependence on $\Delta\eta_{1,3}$ (i.e. between the first and third order harmonics) but a very
82 weak dependence on $\Delta\eta_{1,2}$ (i.e. between first and second order harmonics). We omit the curve for
83 the variation of $C_{1,2,3}$ with $\Delta\eta_{2,3}$ for clarity which looks very similar to the curve shown for $\Delta\eta_{1,2}$.
84 A strong dependence of $C_{1,1,2}$ correlator for $\Delta\eta_{1,2}$ (i.e. between two first order harmonics) was also
85 observed in the previous STAR measurement in Ref [22]. In contrast, the similar measurement shown
86 in Fig.1 (right) for the correlator $C_{2,2,4}$ with two possible combinations of $\Delta\eta$ shows a much weaker
87 dependence compared to its absolute magnitude. These observations indicate a very specific pattern
88 for three particle correlations. The relative rapidity dependence between either “first-first” or “first-
89 third” harmonics show strong variations and even change of sign, whereas between second and any
90 other harmonics the correlations show much weaker variation in relative rapidity.

91 Variations of $C_{m,n,m+n}$ with $\Delta\eta$ can come from hydrodynamic response to the three-dimensional
92 structure of initial state [3, 17–20]. They can also arise from artifacts such as short-range correlations,
93 non-flow and resonance decays [21], etc., that give rise to two-particle correlations that are correlated
94 to an event plane (determined by the third particle) and do not vanish after averaging over many
95 events. However, if such a variation persist up to large $\Delta\eta$, e.g. as shown in Fig.1 for $C_{1,2,3}$ vs $\Delta\eta_{1,3}$,
96 they can not be driven by short range correlations. In a flow scenario, strong variation in $\Delta\eta$ can come
97 from de-correlation in initial state geometry, e.g. driven by a breaking of longitudinal invariance
98 through a forward-backward rapidity dependence of harmonic planes particularly between Ψ_1 and
99 Ψ_3 [3]. In case of Ψ_2 , one do not expect strong variation with rapidity due to geometry of collisions.
100 In a non-flow scenario, in case of $C_{1,2,3}$ one possible source of $\Delta\eta_{1,3}$ dependence could be momentum
101 conservation that leads to back-to-back correlations between two particles from jets that are correlated
102 to second order event plane. We discuss such scenario in the next section.

103 3.2 p_T dependence

104 The effect of momenta conservation is expected to be dominant at higher transverse momentum and
105 for low multiplicity events. Therefore, measurements performed in peripheral events can be a good

¹The $\Delta\eta$ dependence for all other harmonics of $C_{m,n,m+n}$ will be presented in a future publication.

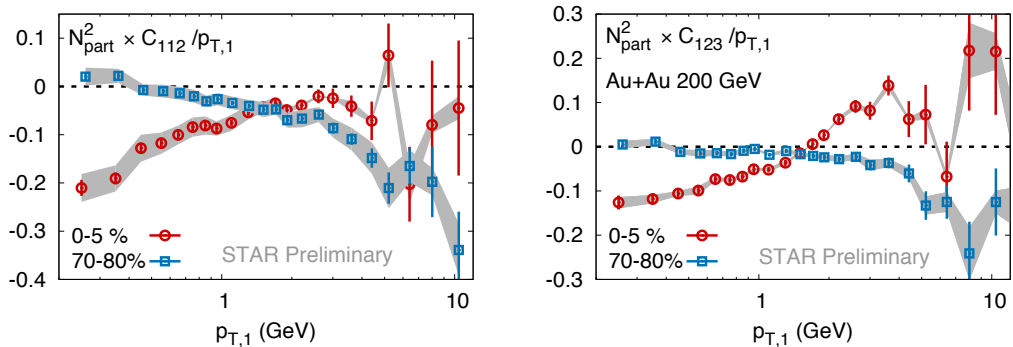


Figure 2. Transverse momentum dependence of the three particle correlator $C_{1,1,2}$ and $C_{1,2,3}$.

106 baseline for such studies. In the central events due to large number of particles, quenching of jet-like
 107 correlations etc., the effect of momentum conservation will not be dominant. It is therefore essential
 108 to perform this exercise in both central (e.g. 0–5%) and peripheral (e.g. 70–80%) and contrast
 109 the trend seen in data. From $\Delta\eta$ dependence of $C_{m,n,m+n}$ we find that the correlators involving first
 110 order harmonics can be sensitive to non-flow effects such as momentum conservations from jets etc.
 111 In Fig. 2 we therefore study the variations of the correlators $C_{1,1,2}$ and $C_{1,2,3}$ with the transverse
 112 momentum p_T of the particle corresponding to the first order harmonic, i.e. for the first particle
 113 as denoted by $p_{T,1}$. In order to remove trivial increase of first order harmonic v_1 with transverse
 114 momentum and trivial dilution of correlation while going from peripheral to central events we multiply
 115 the correlator by a factor of $N_{\text{part}}^2/p_{T,1}$. The results for 70–80% indicates that for high $p_{T,1}$ both $C_{1,1,2}$
 116 and $C_{1,2,3}$ becomes negative. Such trend is consistent with a picture of momentum conservation and
 117 can be understood as follows. If a pair of back-to-back particles gets aligned along Ψ_2 , they will lead
 118 to negative values for these correlators since then we have $C_{1,1,2} \approx \cos(\pi)$ and $C_{1,2,3} \approx \cos(\pm 3\pi)$. This
 119 might explain the decreasing trend for 70–80% events. However such a scenario can not explain the
 120 trend seen 0–5% events where one finds negative signal at small $p_{T,1}$ and nearly zero or positive
 121 signal at large $p_{T,1}$. This qualitatively different trend seen in central events can not be due to non-flow
 122 correlations from back-to-back pairs.

123 Clearly the differential measurements of these correlators can provide better insights of the relative
 124 contributions of different sources of correlations that can affect $C_{m,n,m+n}$. Model calculations that
 125 include full treatment of three-dimensional initial geometry, fluctuations and different other sources
 126 of correlations can improve our understanding in this context [31].

127 3.3 Centrality dependence

128 We measure the centrality dependence of $C_{m,n,m+n}$ and compare our results with three different vis-
 129 ous hydrodynamic model calculations. They include 1) hydrodynamic simulations by Teaney and
 130 Yan [3, 5], 2) the perturbative QCD+saturation+hydro based “EKRT” model [11] and 3) hydrody-
 131 namic simulations MUSIC [32] with IP-Glasma initial conditions [33]. In addition we also esti-
 132 mate the correlations from initial state geometry using Monte Carlo Glauber model by approximating
 133 $C_{m,n,m+n} = \langle \varepsilon_m \varepsilon_n \varepsilon_{m+n} \cos(m\Phi_m + n\Phi_n - (m+n)\Phi_{m+n}) \rangle$, where ε_n s and Φ_n s are the initial eccentrici-
 134 ties and the participant planes respectively. All of these models have been previously constrained by
 135 the measurements of v_n and other data on azimuthal correlations from RHIC and LHC, but they do

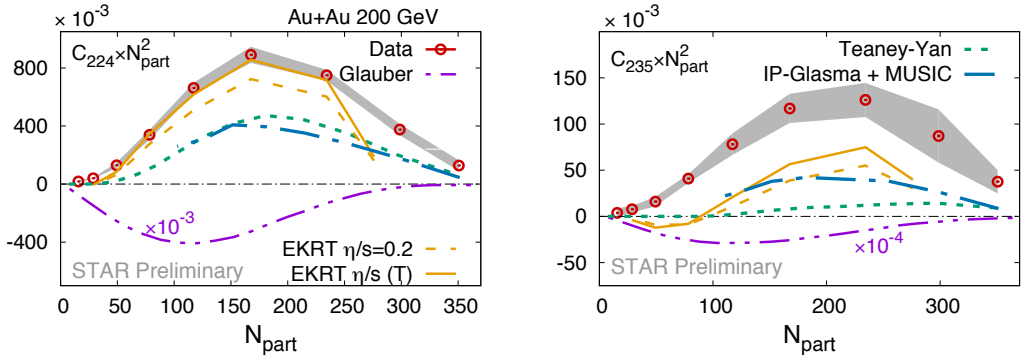


Figure 3. Centrality dependence of three particle correlator $C_{1,1,2}$ and $C_{2,2,4}$ compared to different viscous hydrodynamic model calculations.

136 not include longitudinal dependence in the initial state and assume boost invariance. From Fig.1 it is
 137 evident that the correlator $C_{2,2,4}$ has the least variation on $\Delta\eta$ and will provide the best opportunity for
 138 comparison to boost-invariant hydrodynamic simulations. We therefore present the centrality dependence
 139 of the correlator $C_{2,2,4}$ in Fig.3 (left). In Fig.3 (right) we also compare the centrality dependence
 140 of $C_{2,3,5}$. In order to scale out the trivial dilution of correlations due to increase of number of pairs
 141 while going from peripheral to central events we have multiplied the correlators by N_{part}^2 . The Glauber
 142 model calculations predict that purely initial state correlation of eccentricities and participant planes
 143 leads to negative values for all the correlators. Both $C_{2,2,4}$ and $C_{2,3,5}$ being positive in data indicate the
 144 dominance of non-linear hydrodynamic response of the medium to initial state geometry. This obser-
 145 vation is consistent to the measurement at LHC by the ATLAS collaboration in Ref [13]. We however,
 146 find that although the qualitative trends predicted by different viscous hydrodynamic simulations are
 147 similar to data, some quantitative differences exist. Particularly for $C_{2,2,4}$ one can see that the current
 148 precision of the data can very well differentiate between constant and temperature dependent viscos-
 149 ity used in the EKRT simulations. Such comparisons would be key to constrain $\eta/s(T)$. Apart from
 150 analysis at $\sqrt{s_{NN}} = 200$ GeV, our future studies will be focused on measurements for other lower
 151 energies under RHIC Beam Energy Scan program which will provide better constraints of $\eta/s(T)$.

152 Summary

153 In summary, we have presented the first measurements of three-particle correlations $C_{m,n,m+n} =$
 154 $\langle\langle \cos(m\phi_1 + n\phi_2 - (m+n)\phi_3) \rangle\rangle$ in $\sqrt{s_{NN}} = 200$ GeV Au+Au collisions at RHIC. In comparison
 155 to conventional flow harmonic measurements these correlators can provide additional information
 156 such as de-correlation of event planes driven by three dimensional structure of the initial state and
 157 non-linear hydrodynamic response of the medium. When compared to viscous hydrodynamic mod-
 158 els these measurements with the precision presented here have the potential to constrain transport
 159 parameters and their temperature dependence.

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