

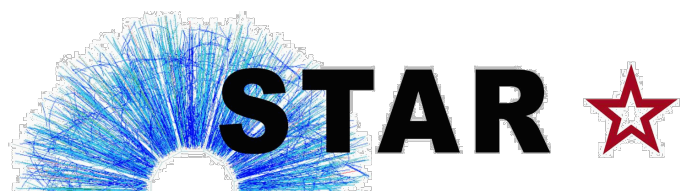
Studies of three-particle correlations and reaction-plane correlators from STAR

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(for the STAR Collaboration)

BROOKHAVEN
NATIONAL LABORATORY

XLVI International Symposium on Multiparticle Dynamics (ISMD2016)

Jeju island, South Korea August 29 – September 2, 2016



Outline

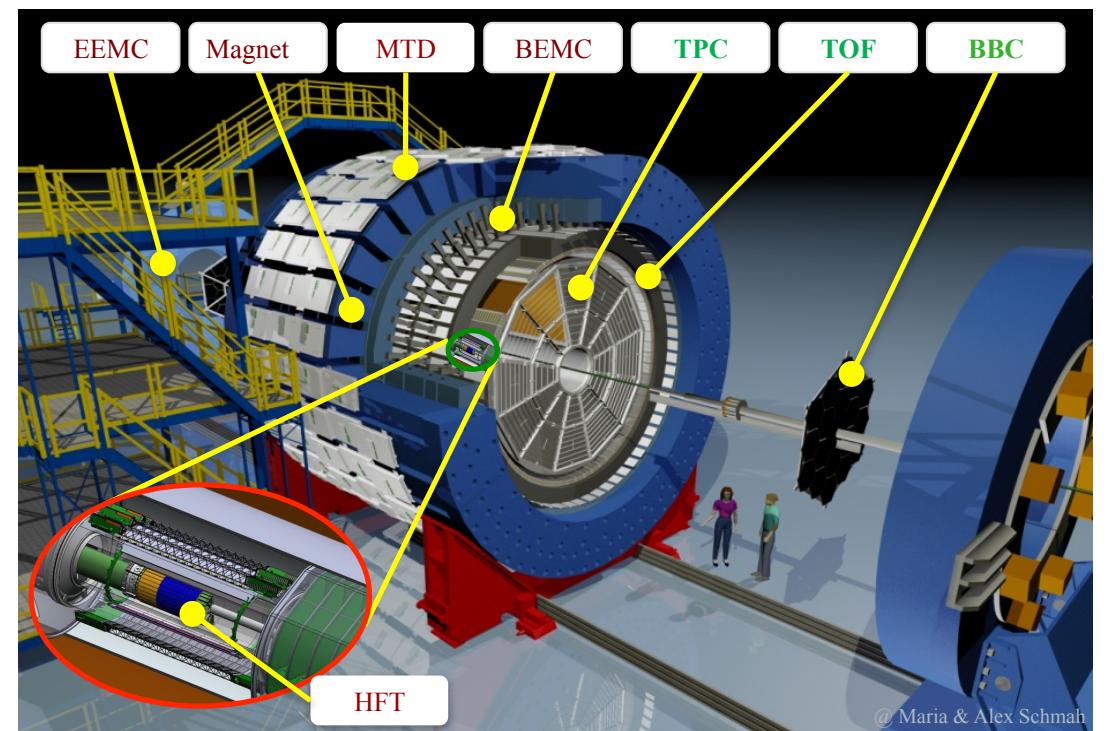
- Introduction
- Measurement of 3-particle correlations from STAR
- Comparison to models & possible interpretations

Goal is to :

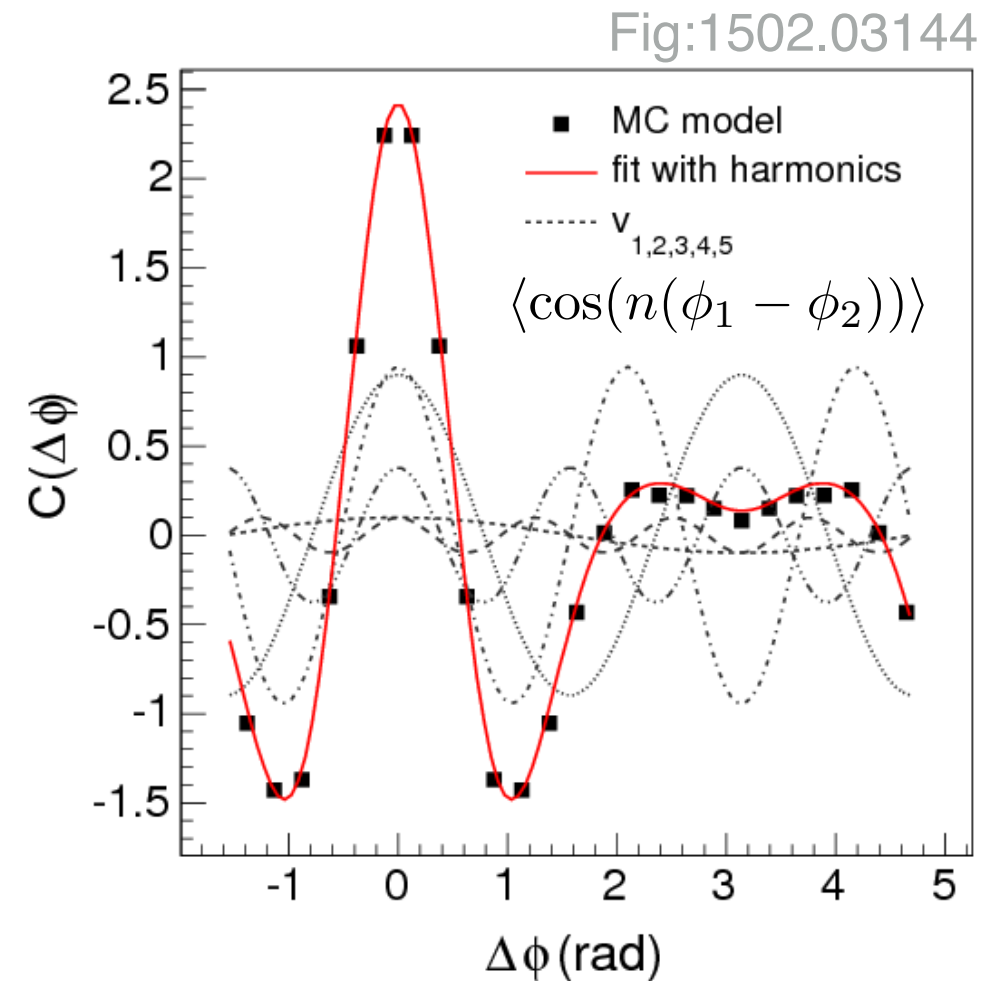
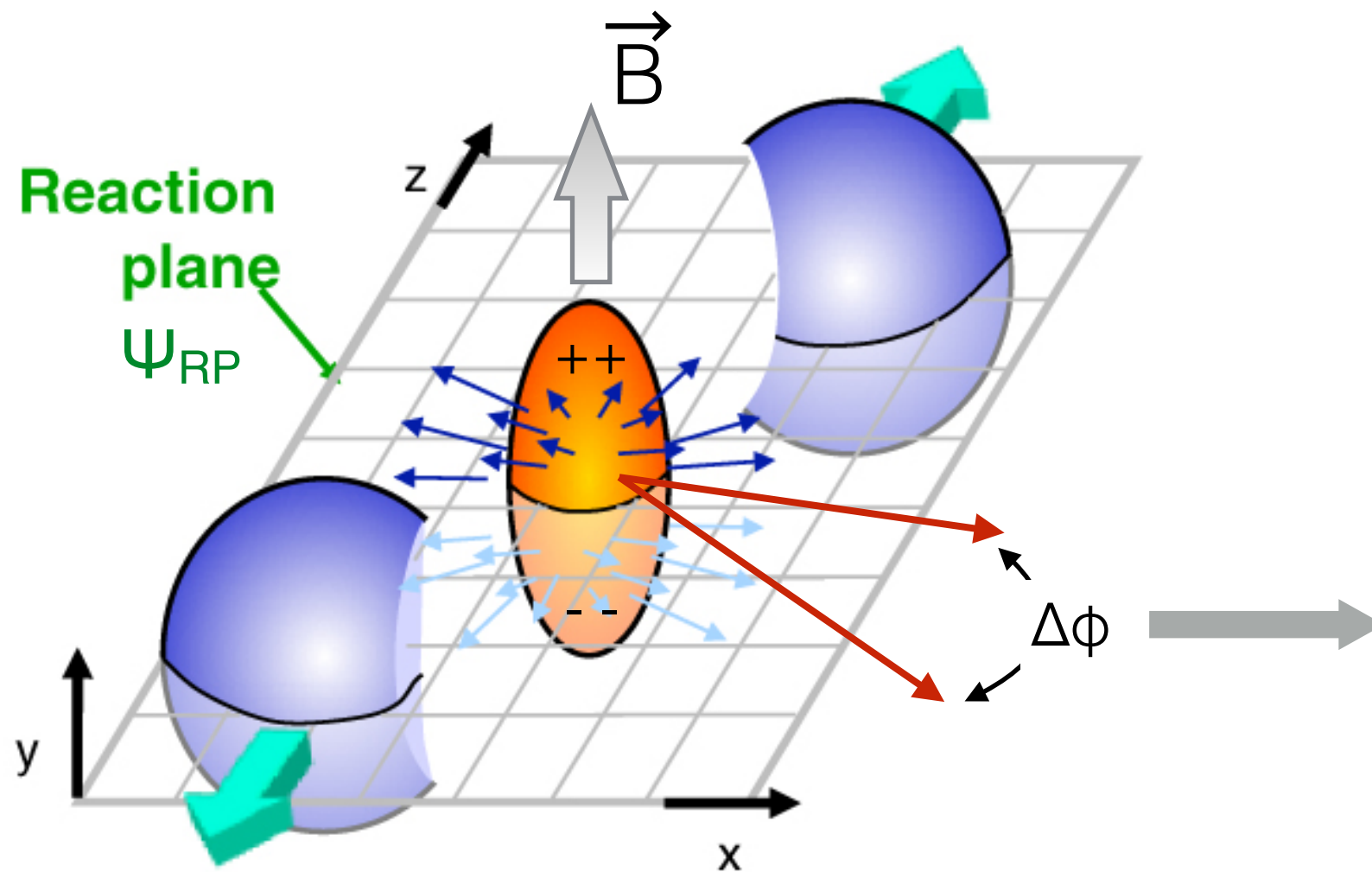
Map out 3D structure of HIC

Constrain η/s with more precision

Provide baseline for CME



Azimuthal correlations in Relativistic Heavy Ion collisions



Conventional measurement \rightarrow two-particle correlations : $\langle \cos(n(\phi_1 - \phi_2)) \rangle$

This measurement \rightarrow three-particle correlations : $\langle \cos(m\phi_1 + n\phi_2 - (m + n)\phi_3) \rangle$

Definition of the observables

- General (3-particle) correlator :

$$C_{m,n,m+n} = \langle \langle \cos(m\phi_1 + n\phi_2 - (m+n)\phi_3) \rangle \rangle$$

- Connection to event-plane correlator (based on flow interpretation)

$$C_{m,n,m+n} = \langle v_m v_n v_{m+n} \cos(m\Psi_m + n\Psi_n - (m+n)\Psi_{m+n}) \rangle$$

Different harmonic of $C_{m,n,m+n} \rightarrow$ sensitive to different physics

$$C_{112} = \langle \cos((\phi_1^\pm + \phi_2^\mp - 2\phi_3)) \rangle \rightarrow \text{charge separation w.r.to event plane driven by chiral magnetic effect}$$

Why study three-particle correlations ?

Teany, Yan 1010.1876

Bhalerao, Luzum, Ollitrault 1106.4940

Heinz, Qiu 1208.1200

ATLAS 1408.4342

- **Two particle correlation w.r.to RP :**
More freedom to map out both transverse and longitudinal structure of the fireball
- **Connection to flow harmonic & event-plane correlations :**
Non-linear hydrodynamic response more sensitive to viscosity
- **Baseline for Chiral Magnetic Effects (CME) :**
Essential to understand components driven by initial-state, magnetohydrodynamics

Going beyond conventional measurements of flow harmonics

Motivation-I (3D structure of HIC)

Initial-state fluctuations

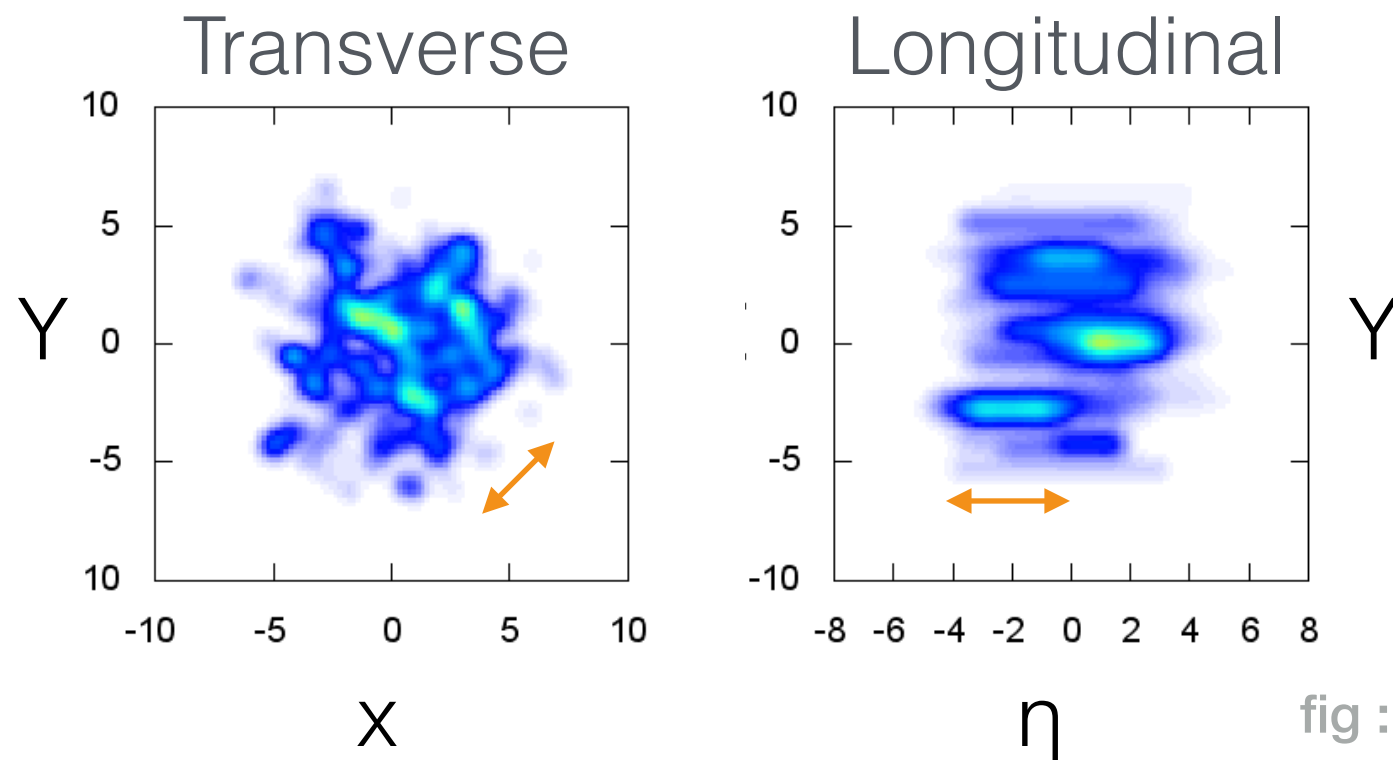


fig : Schenke
QM'15

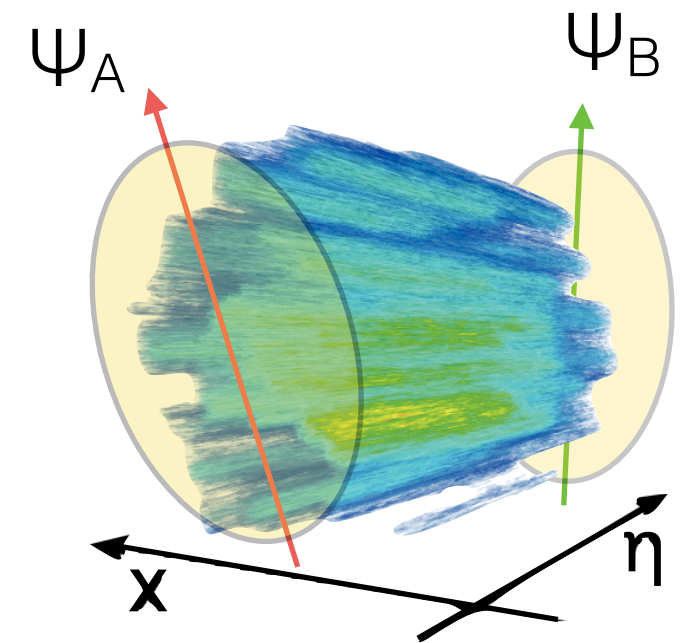


fig : 1605.07158

Bozek *et al* 1011.3354
Jia *et al* 1403.6077
Pang *et al* 1511.04131

Breaking of **boost-invariance** → due to longitudinal fluctuations

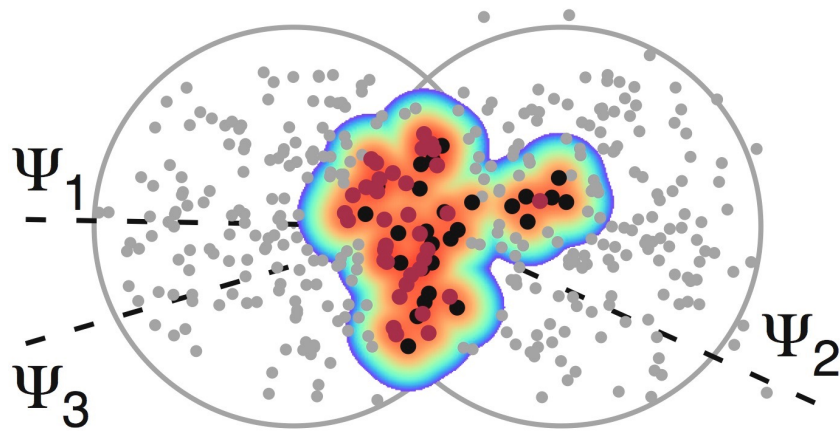
These effects → referred as **twist, torque, event-plane decorrelation**

3D initial state → can be probed by $C_{m,n,m+n}$ & its $\Delta\eta$ dependence

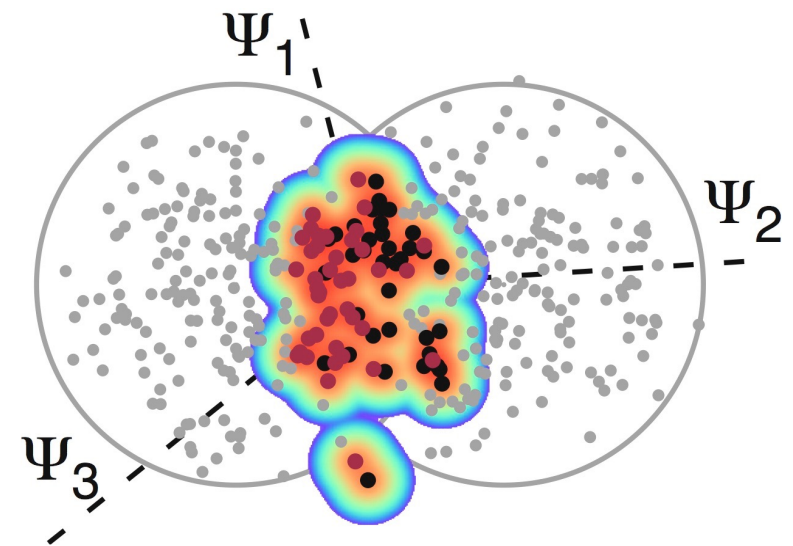
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v_3 is driven by both geometry + fluctuation

Teany, Yan 1010.1876



In-plane fluctuations



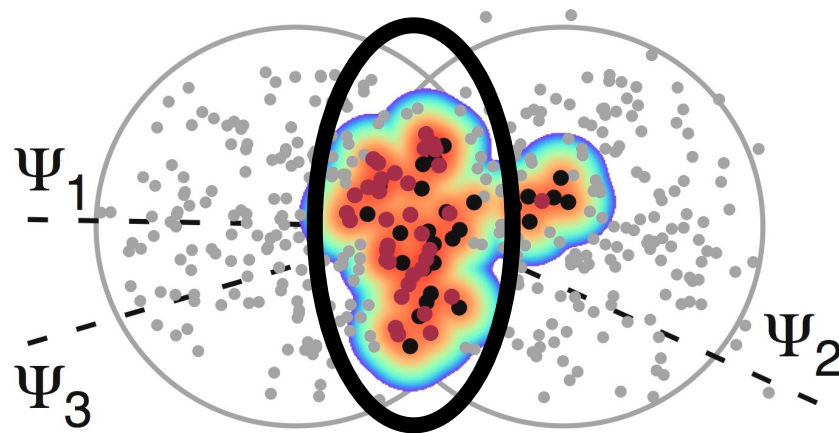
Out-of-plane fluctuations

v_1 drives v_3 in mid-central collisions \rightarrow can be probed by C_{123}

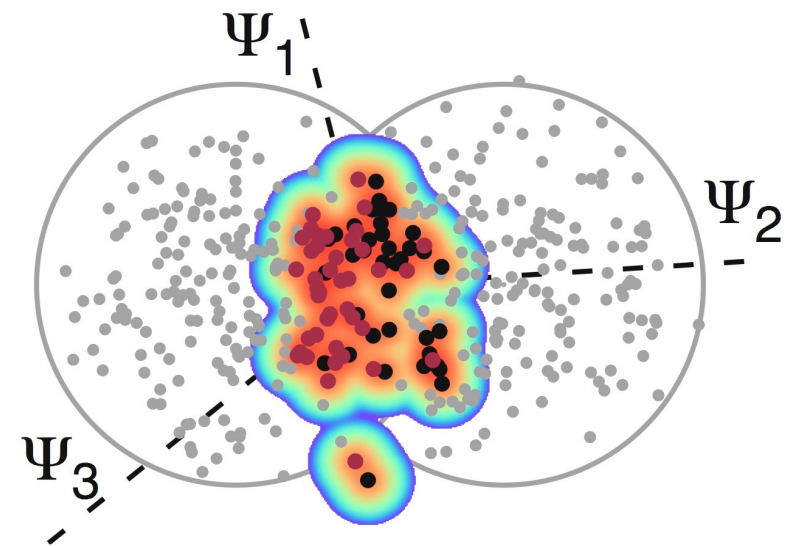
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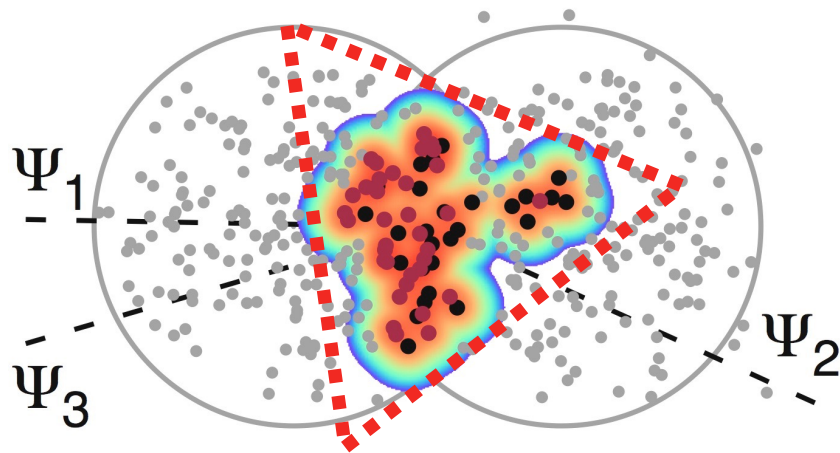
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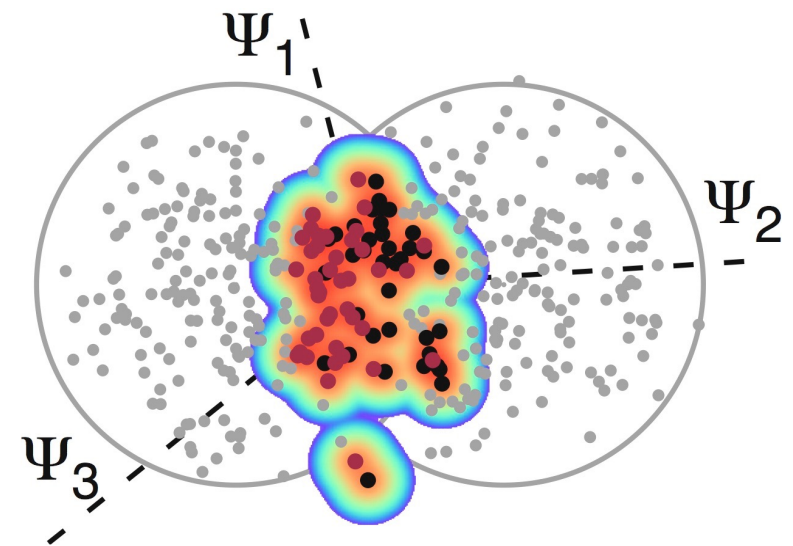
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Motivation-II (Non-linear hydro response)

Teany, Yan 1010.1876
Heinz, Qiu 1208.1200

Better probe for transport properties of QGP

- More sensitivity due to **non-linear** hydro response

$$C_{235} = \langle v_2 v_3 v_5 \cos(2\Psi_2 + 3\Psi_3 - 5\Psi_5) \rangle$$

Initial geometry



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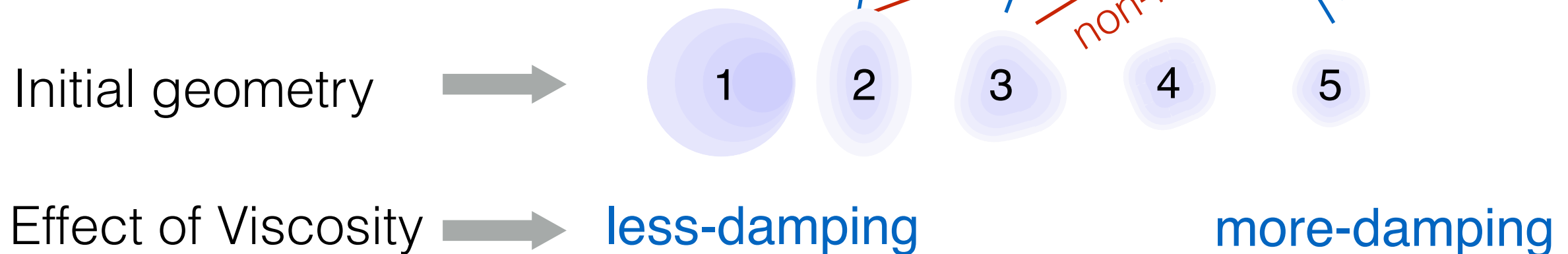
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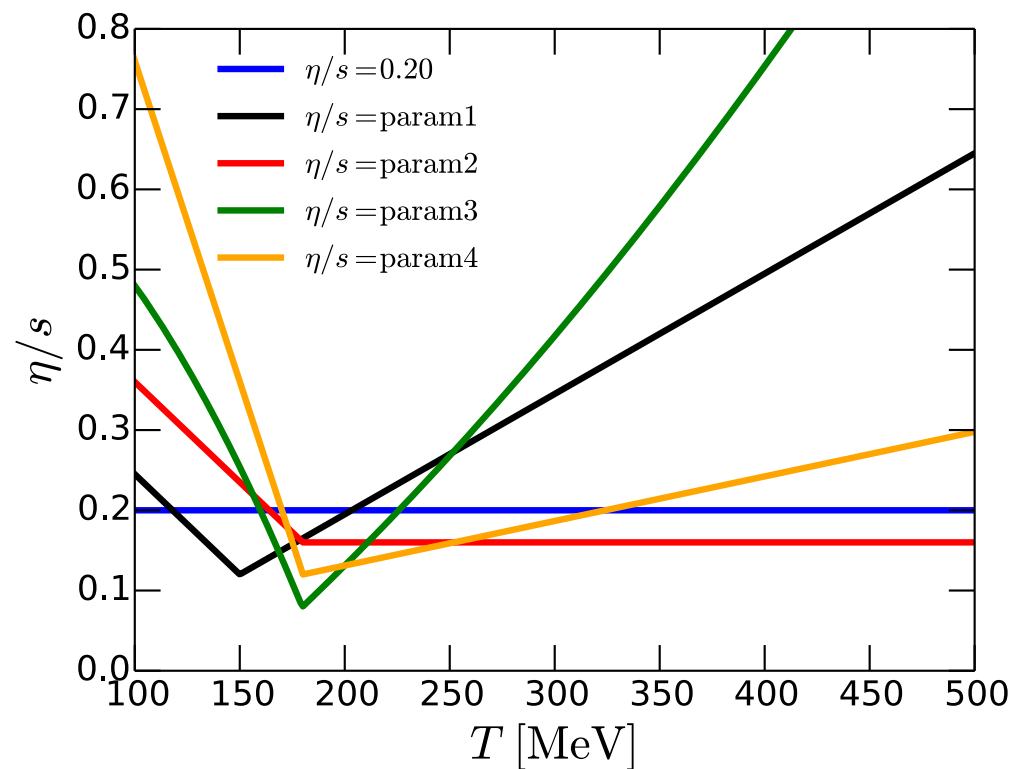


$\Psi_5 \rightarrow$ more correlated to Ψ_2 & Ψ_3 due to viscous damping

Non-linear response \rightarrow can be probed by sign change of $C_{m,n,m+n}$

Motivation-III (Towards constraining $\eta/s(T)$)

Niemi *et al*
1505.02677



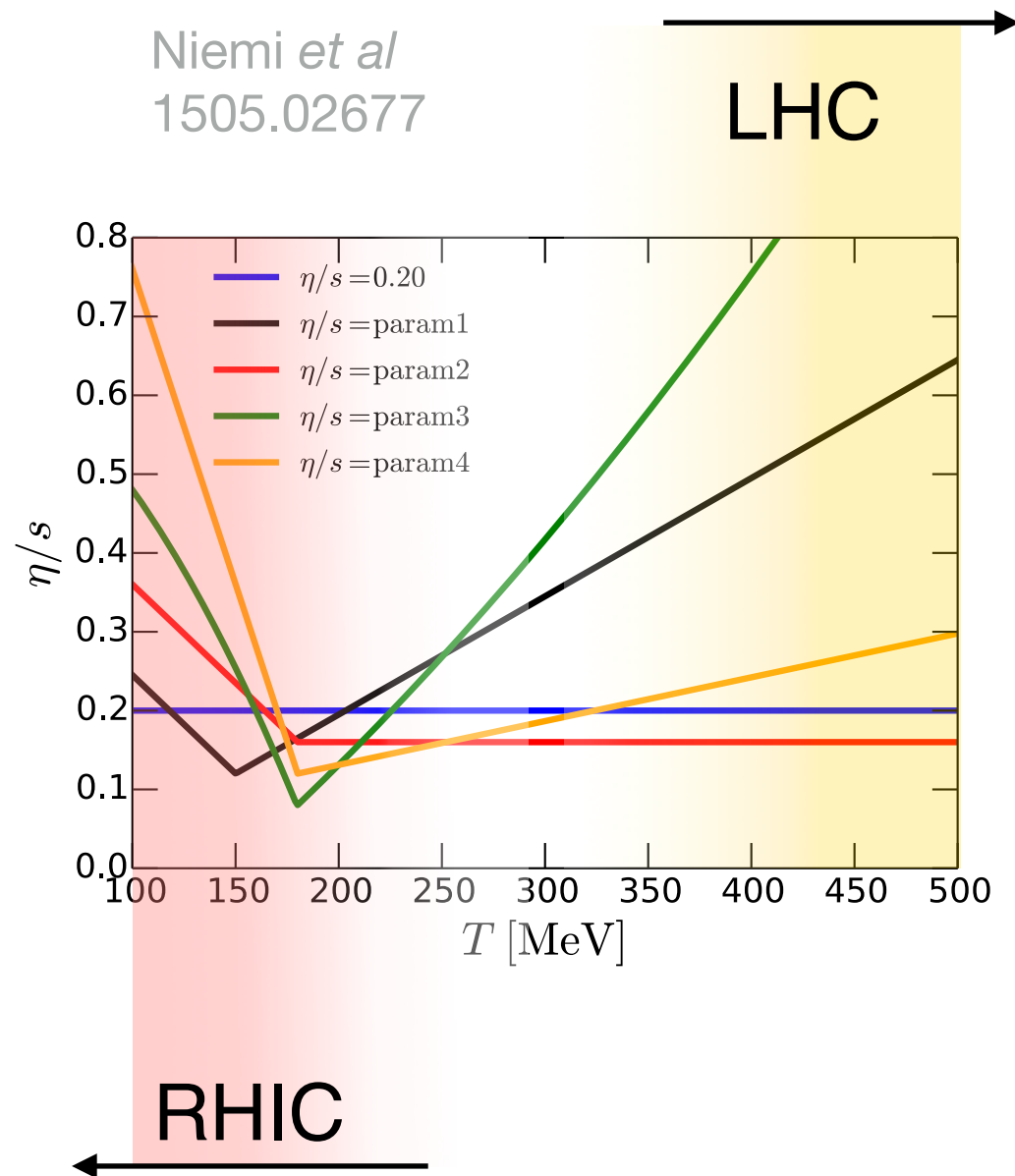
Viscosity has temperature dependence

$\eta/s(T) \rightarrow$ not yet fully constrained

Models assume parametrization

Niemi et al 1101.2442
Lacey et al 1305.3341
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Denicol et al 1512.01538

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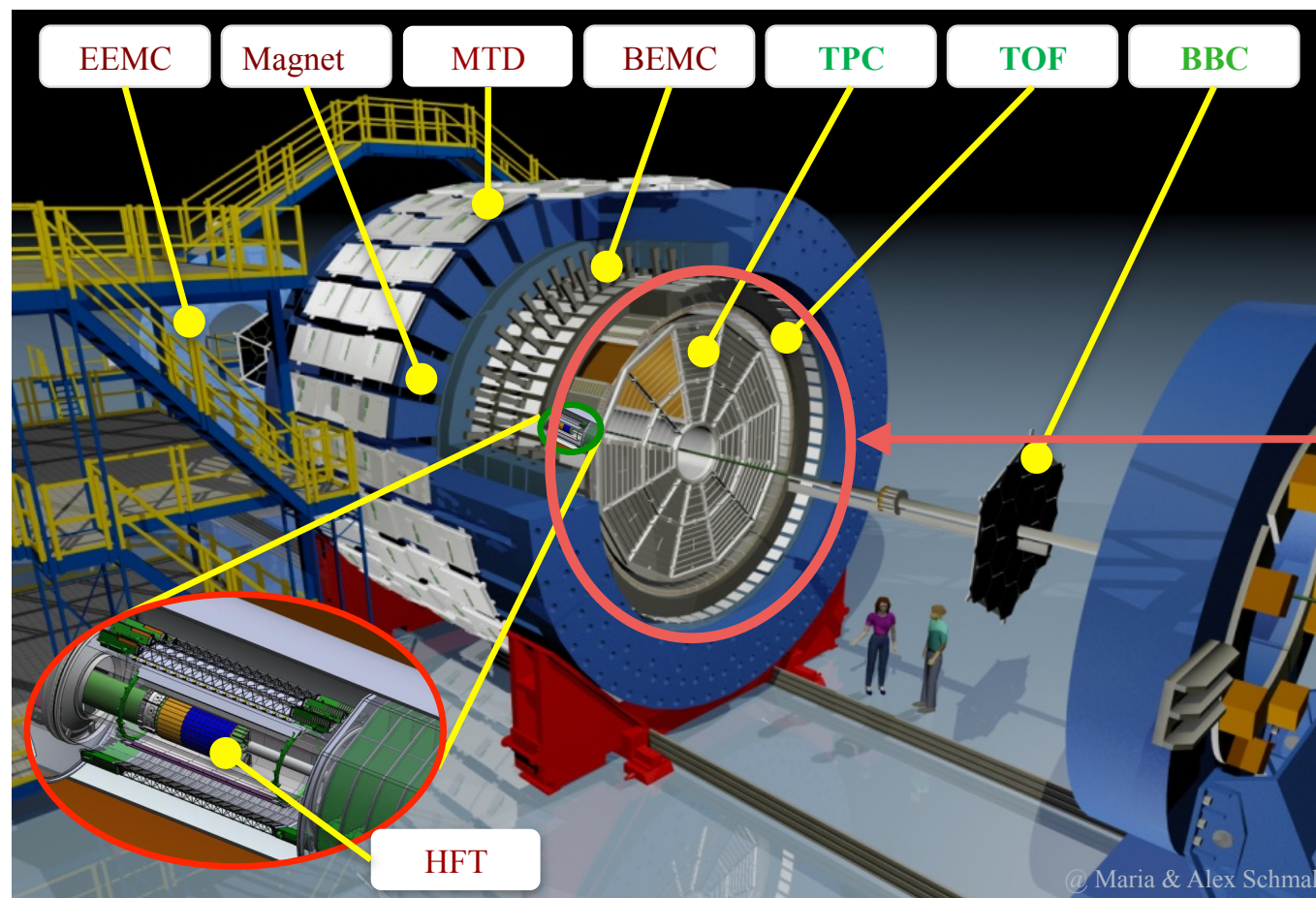
$\eta/s(T) \rightarrow$ not yet fully constrained

Models assume parametrization

Measurements at RHIC are essential
to constrain $\eta/s(T)$ at low temperatures

Niemi *et al* 1101.2442
Lacey *et al* 1305.3341
Niemi *et al* 1505.02677
Denicol *et al* 1512.01538

STAR detector system



This analysis uses inclusive charged particles detected by the Time-Projection Chamber

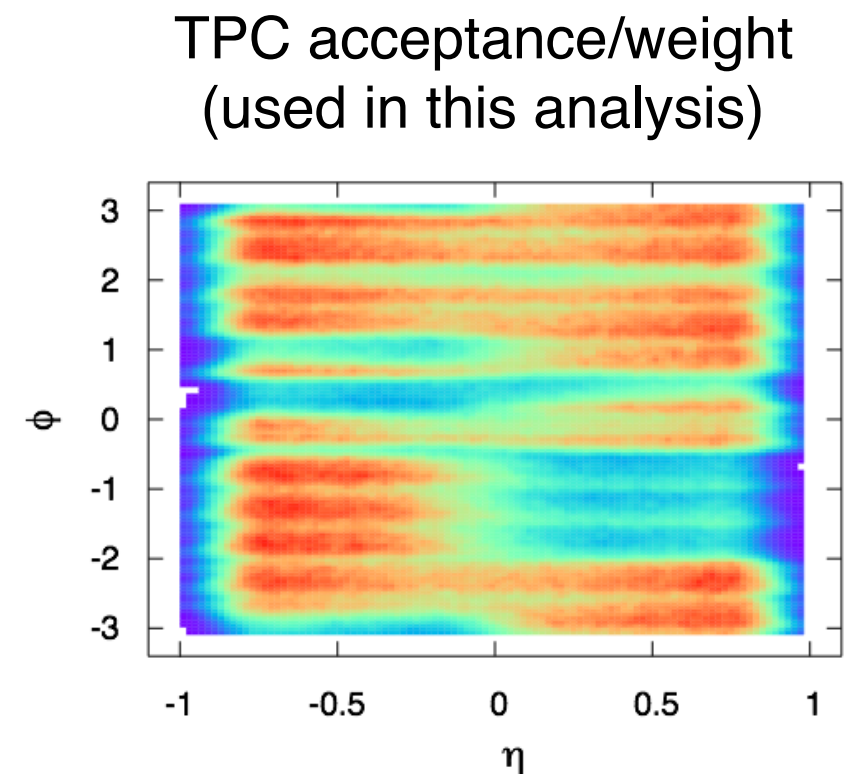
Data sets used are from year 2004, 2010-12, & 2014 :
Au+Au collisions at $\sqrt{s_{NN}} = 200, 62.4, 39, 27, 19.6, 14.5, 11.5, 7.7$ GeV

Details of the cuts & methods

- **Centrality selection:** Uncorrected multiplicity in $|\eta| < 0.5$
- **Acceptance cuts:** $0 < \phi < 2\pi$, $|\eta| < 1$, $p_T > 0.2$ GeV/c

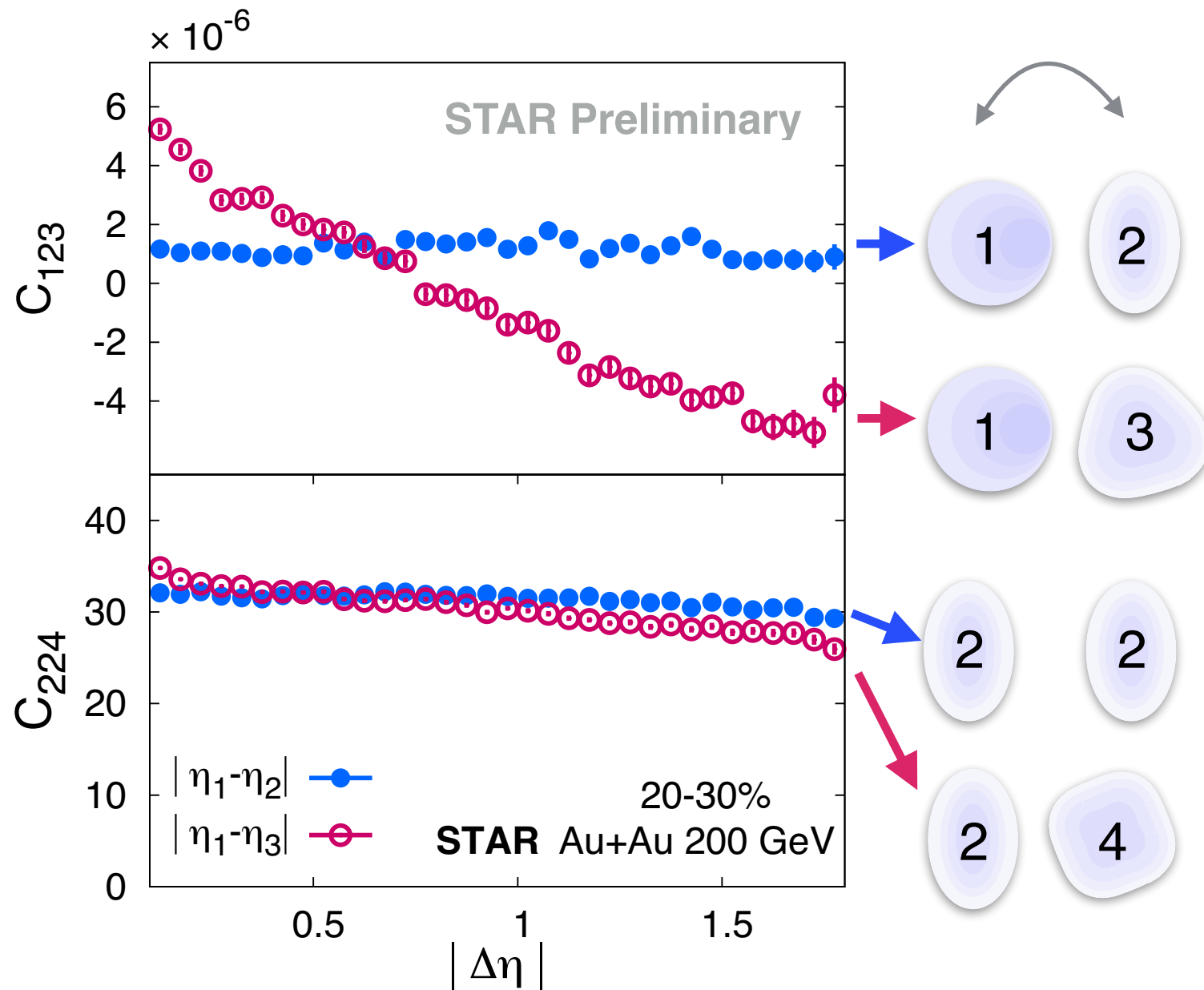
We use Q-Cumulant method & estimate :

$$C_{m,n,m+n} = \left\langle \frac{\sum_{i,j,k} \omega_i \omega_j \omega_k \cos(m\phi_i + n\phi_j - (m+n)\phi_k)}{\sum_{i,j,k} \omega_i \omega_j \omega_k} \right\rangle$$

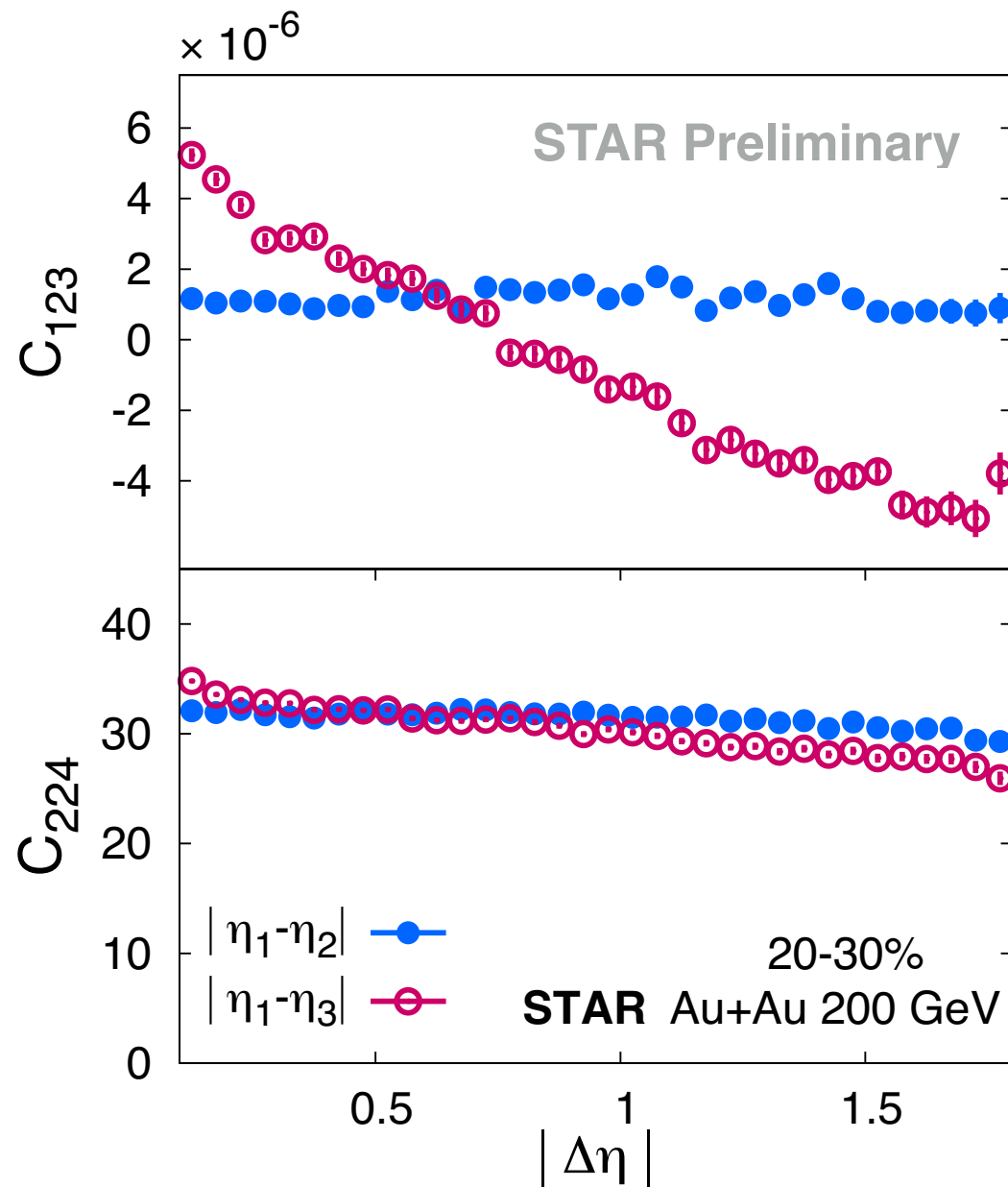


$\omega_{i,j,k} \rightarrow$ Weight estimated in bins of sagitta, η - ϕ of tracks

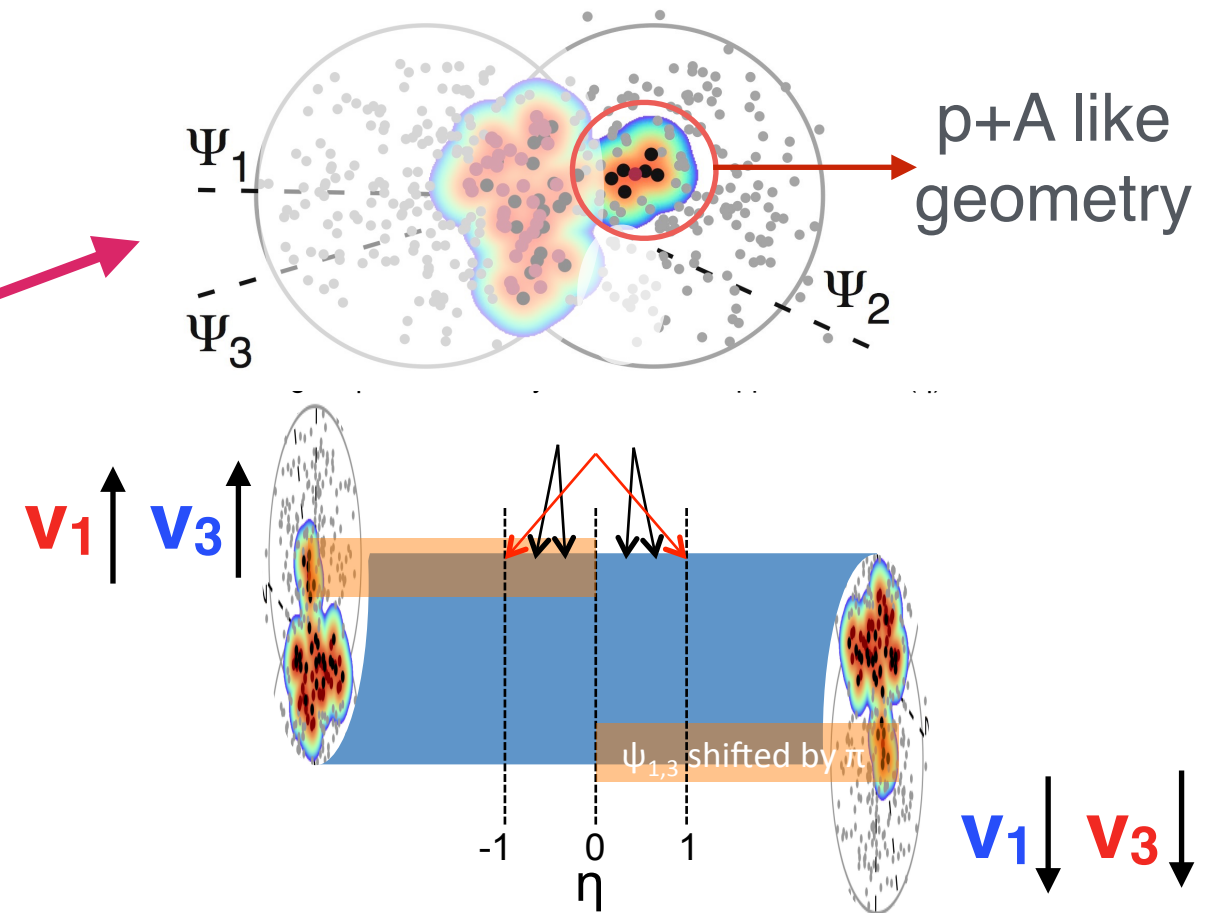
Results : $\Delta\eta$ dependence of $C_{m,n,m+n}$



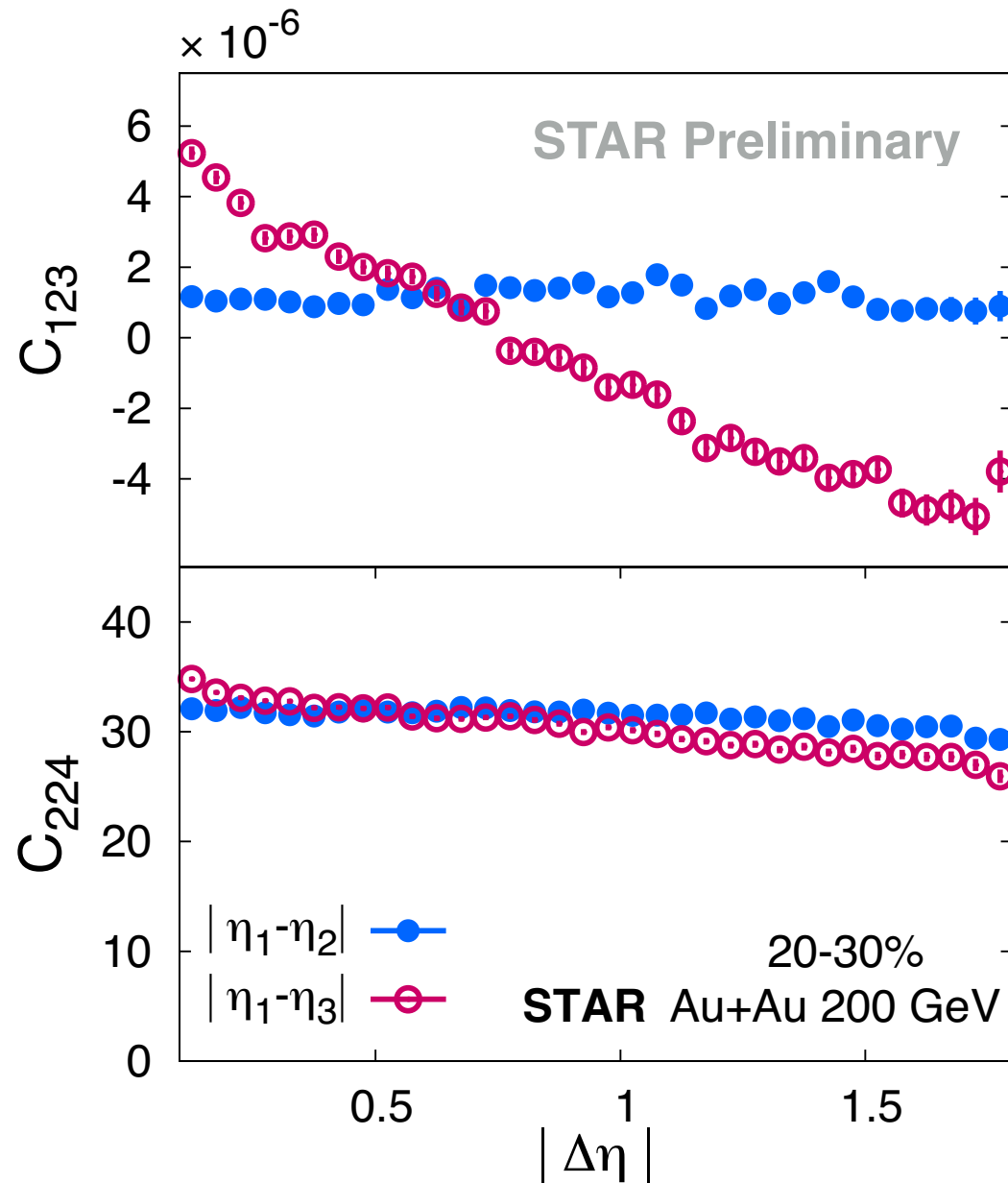
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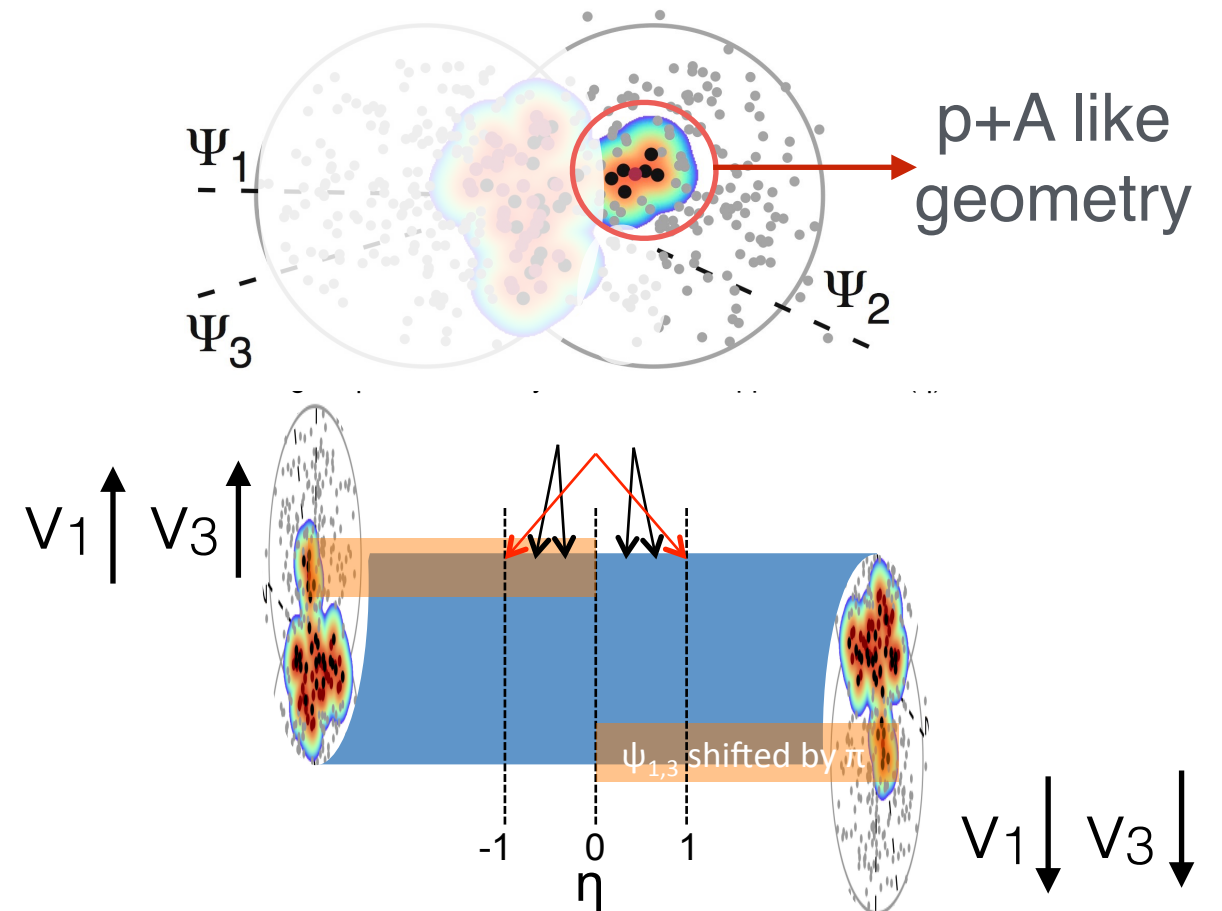
Possible scenario:
fluctuations \rightarrow η -asymmetry, $\Delta\eta$ dependence



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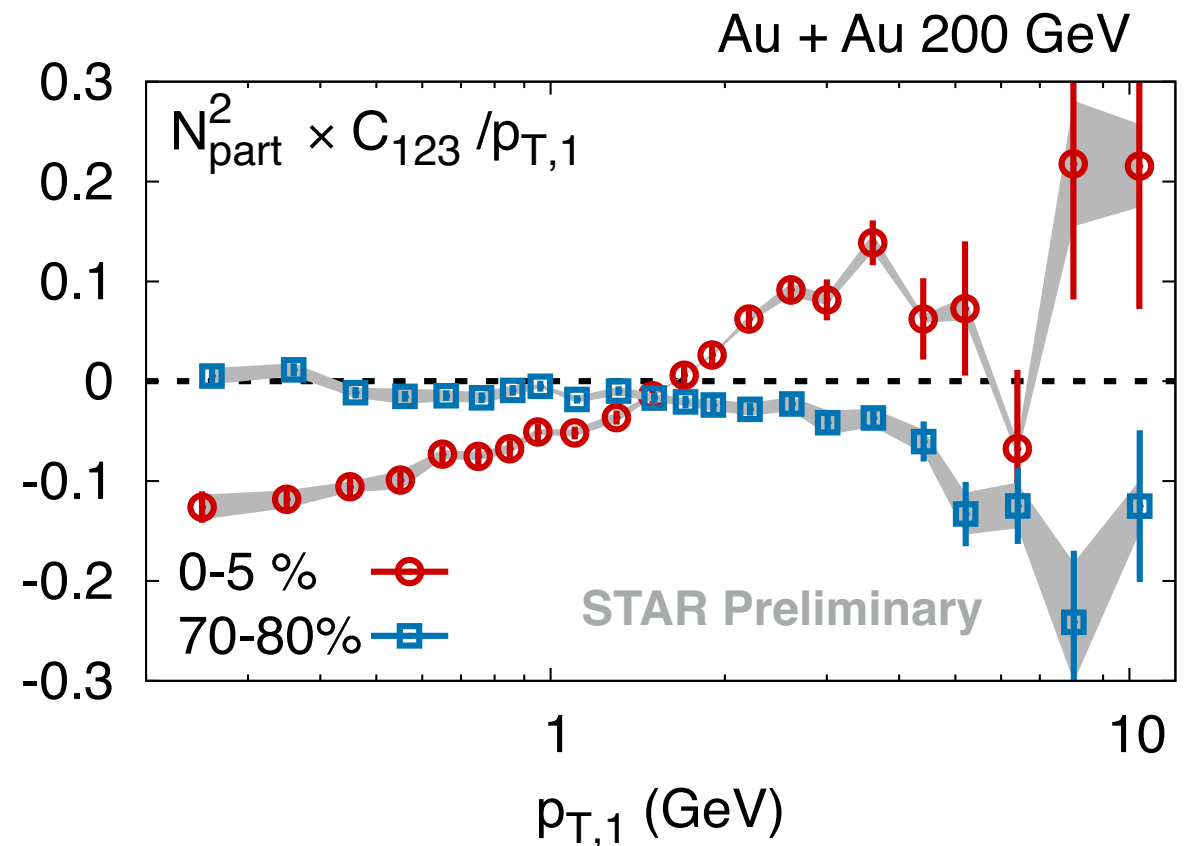
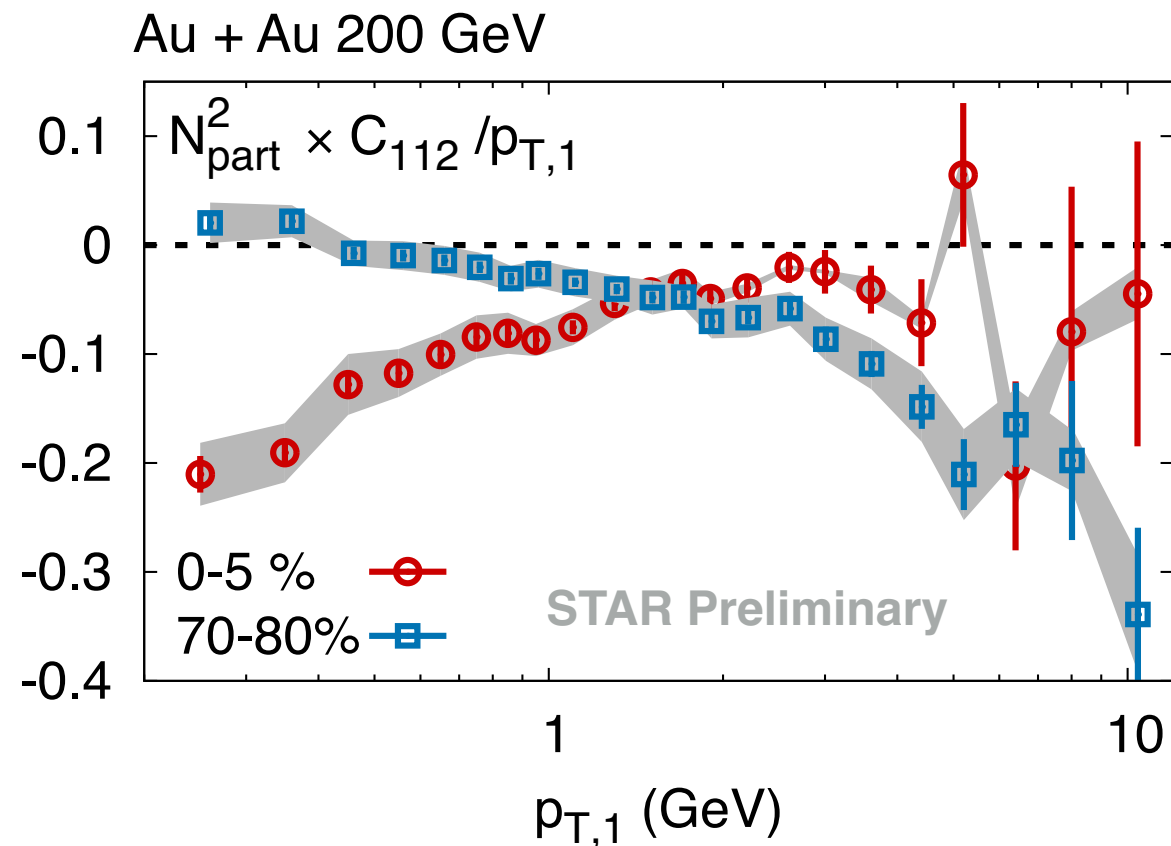
Jet correlated to Ψ_2 plane may also lead to $\Delta\eta$ dependence

Strong $\Delta\eta$ dependence of $C_{123} \rightarrow$ due to η asymmetric of v_1

$C_{224} \rightarrow$ weak dependence, best for comparison to 2D hydro models

Measurement of p_T dependence of $C_{m,n,m+n}$

Different p_T regime \rightarrow sensitivity to different physics

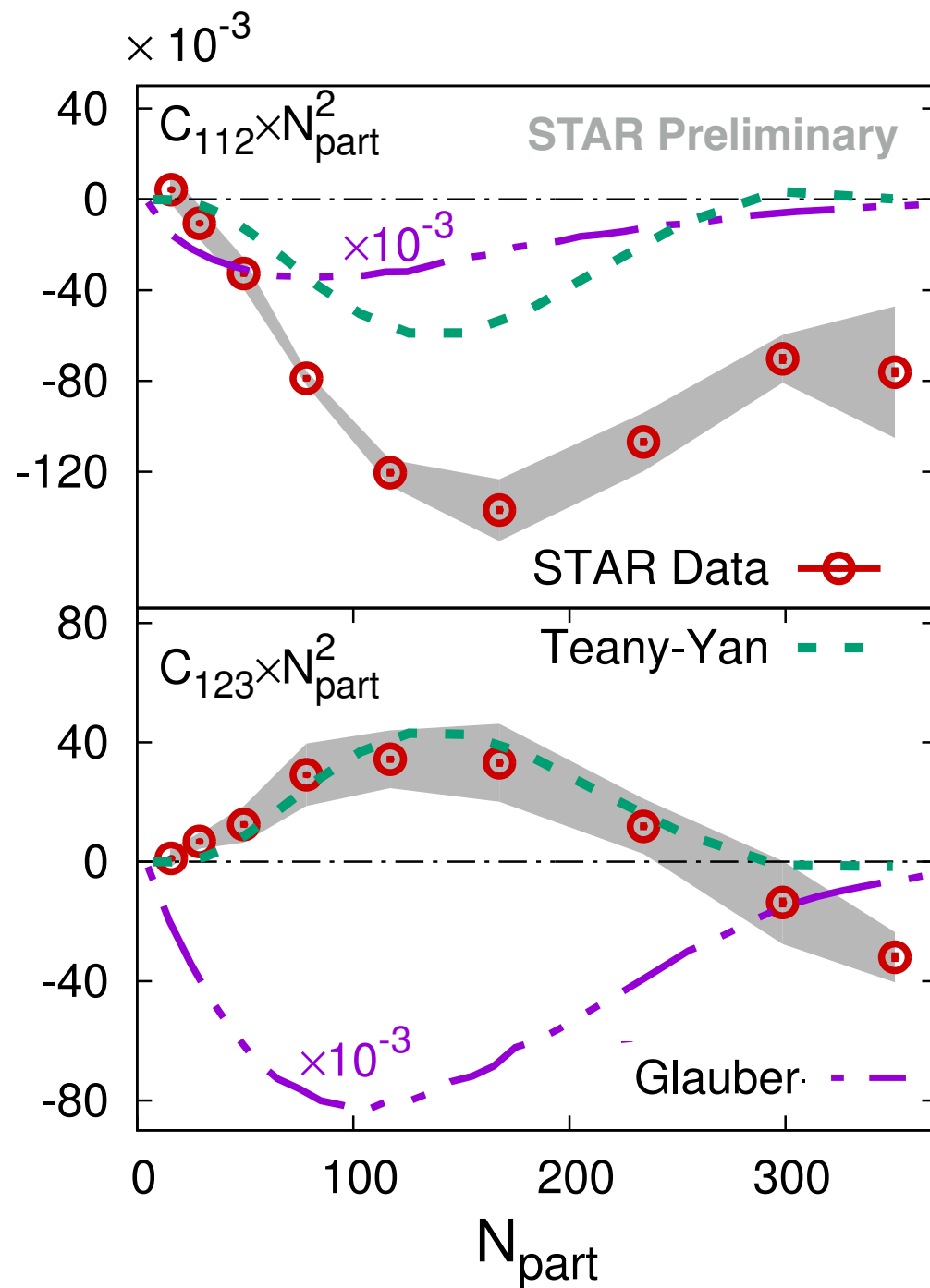


High p_T & peripheral events \rightarrow momentum conservation from jets



Correlations in central events look completely different from peripheral

Centrality dependence of $C_{m,n,m+n}$

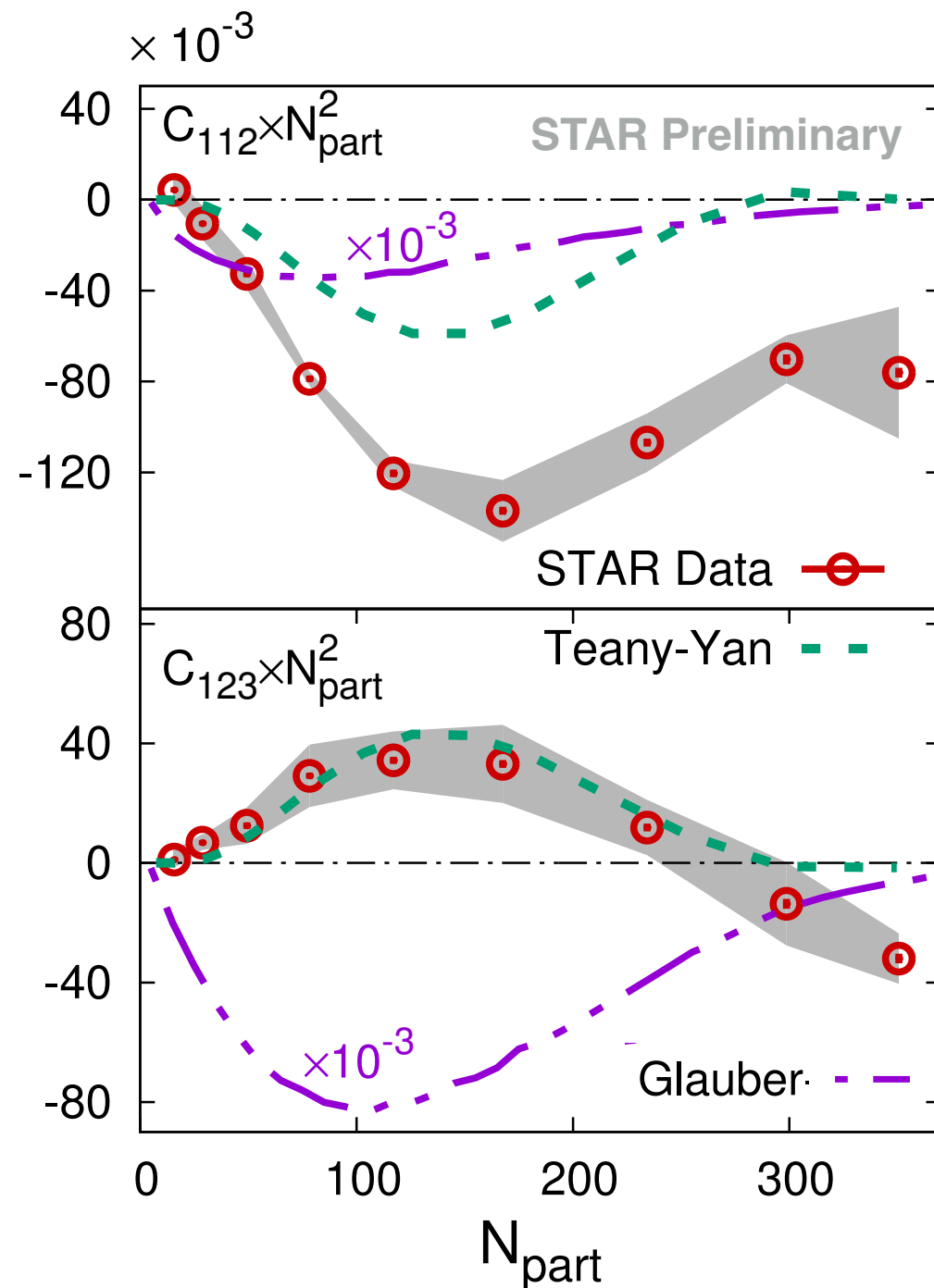


C_{112} :

- Measures baseline for CME
- Non-zero correlations for central collisions in contrast to the models

Magnitude follows initial state but sign depends on final state effects

Centrality dependence of $C_{m,n,m+n}$



C_{112} :

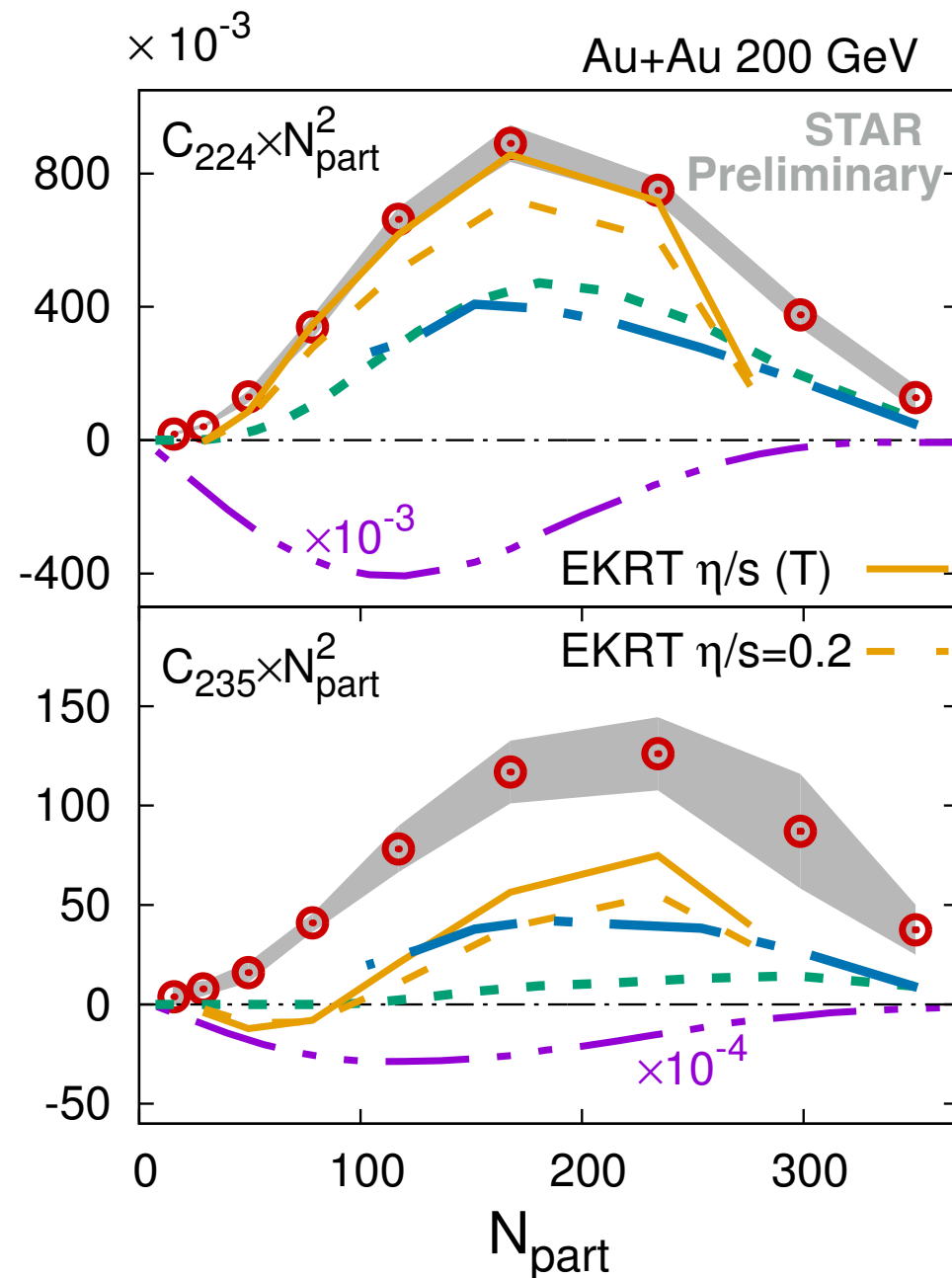
- Measures baseline for CME
- Non-zero correlations for central collisions in contrast to the models

C_{123} :

- Indicates v_1 drives v_3 (in mid-central collisions) as predicted by Teaney & Yan
- Non zero (negative) for central collisions

Magnitude follows initial state but sign depends on final state effects

Centrality dependence of higher order $C_{m,n,m+n}$



Sign change
from Glauber
expectations

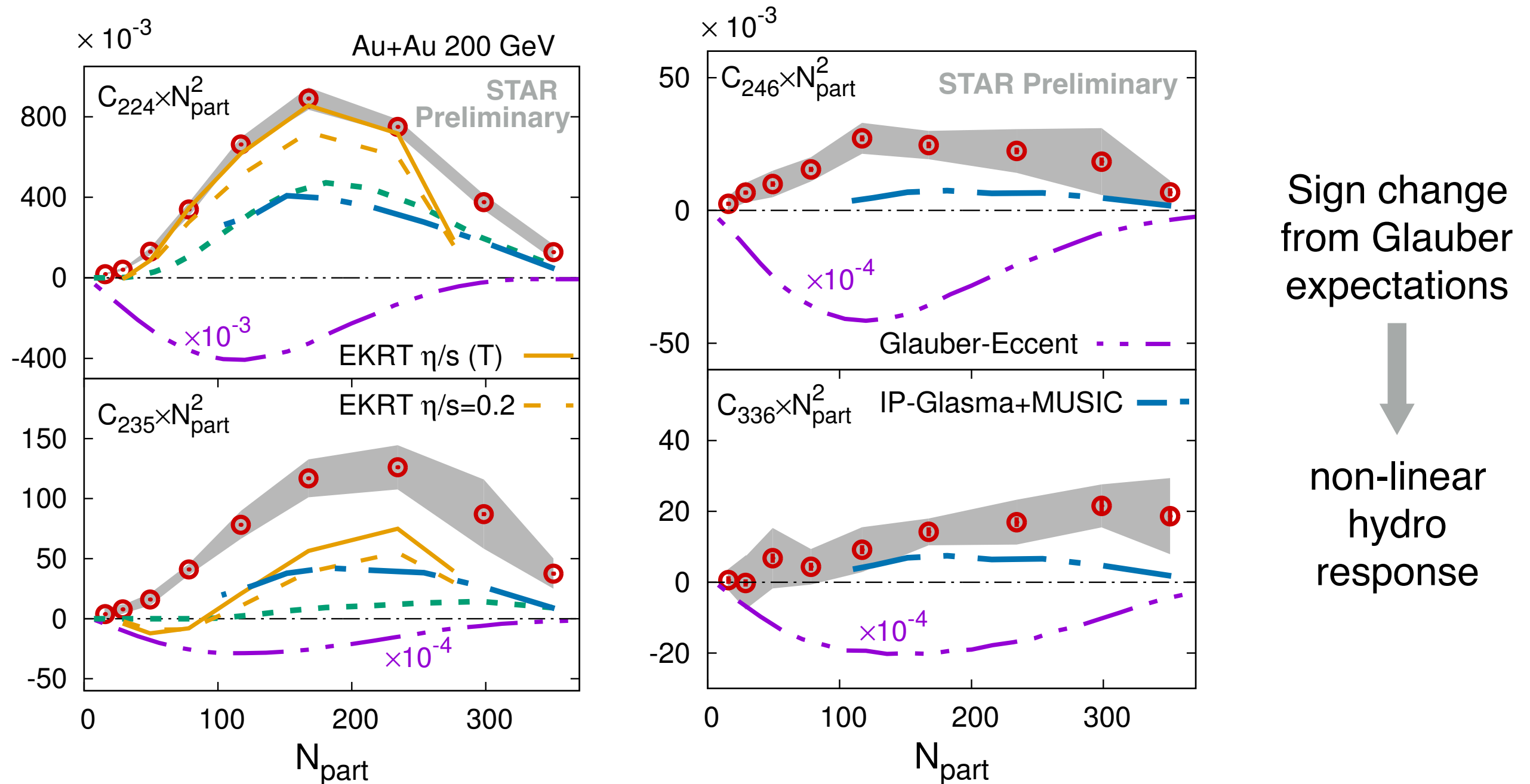


non-linear
hydro
response

Indication of strong non-linear hydro response, sensitivity to $\eta/s(T)$

2+1D hydro models describe trends but under predicts the data

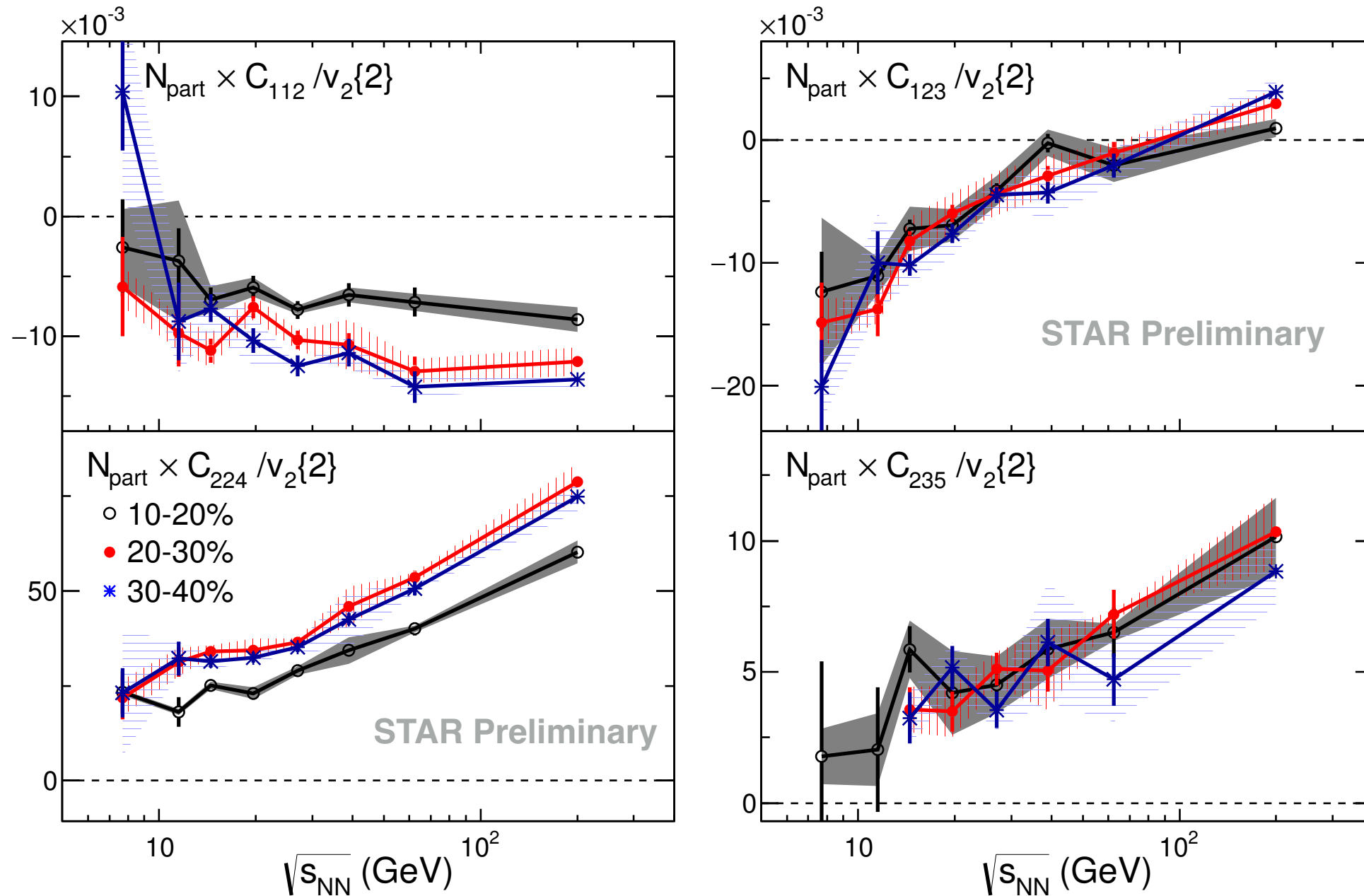
Centrality dependence of higher order $C_{m,n,m+n}$



Indication of strong non-linear hydro response, sensitivity to $\eta/s(T)$

2+1D hydro models describe trends but under predicts the data

Energy dependence of $C_{m,n,m+n}$



Monotonic dependence with C_{123} changing sign

Results will improve modeling of heavy ion collisions at low energy

Tomography of particle flow

Combining all results together can give us a picture of collisions

$$\langle \cos(1\phi_1 + 1\phi_3 - 2\phi_2) \rangle / v_2 \approx \langle \cos(1\phi'_1 + 1\phi'_2) \rangle$$

$$\langle \cos(1\phi_1 + 2\phi_3 - 3\phi_2) \rangle / v_2 \approx \langle \cos(1\phi'_1 - 3\phi'_2) \rangle$$

$$\langle \cos(2\phi_1 + 2\phi_3 - 4\phi_2) \rangle / v_2 \approx \langle \cos(2\phi'_1 - 4\phi'_2) \rangle$$

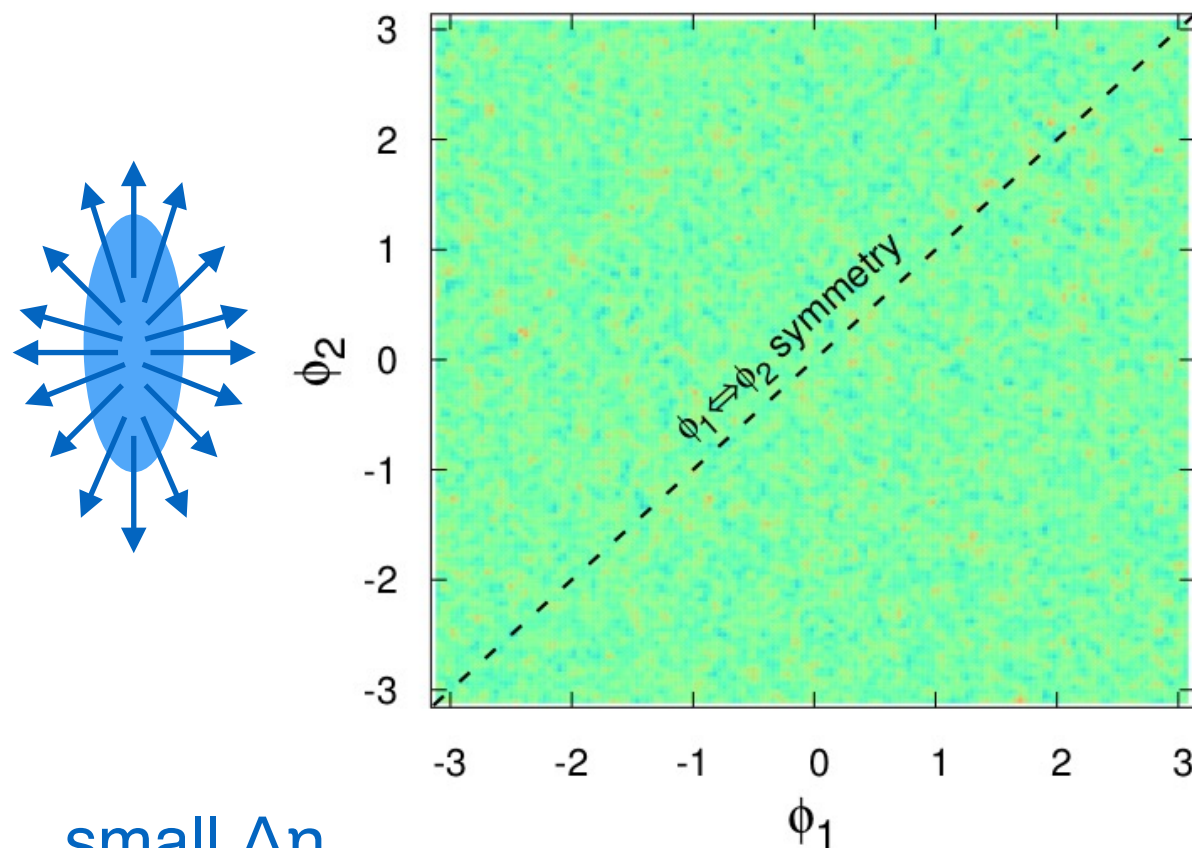
$$\langle \cos(2\phi_3 + 3\phi_1 - 5\phi_2) \rangle / v_2 \approx \langle \cos(3\phi'_1 - 5\phi'_2) \rangle$$

	(ϕ'_1, ϕ'_2) [rad]				
	$(0, 0)$	$(0, \pi)$	$(\frac{\pi}{2}, \frac{\pi}{2})$	$(\frac{\pi}{2}, -\frac{\pi}{2})$	$\pm(\frac{\pi}{3}, \frac{2\pi}{3})$
$C_{1,1,2}/v_2$	+1	-1	-1	+1	-1
$C_{1,2,3}/v_2$	+1	-1	-1	+1	$+\frac{1}{2}$
$C_{2,2,4}/v_2$	+1	+1	-1	-1	$+\frac{1}{2}$
$C_{2,3,5}/v_2$	+1	-1	-1	+1	$+\frac{1}{2}$

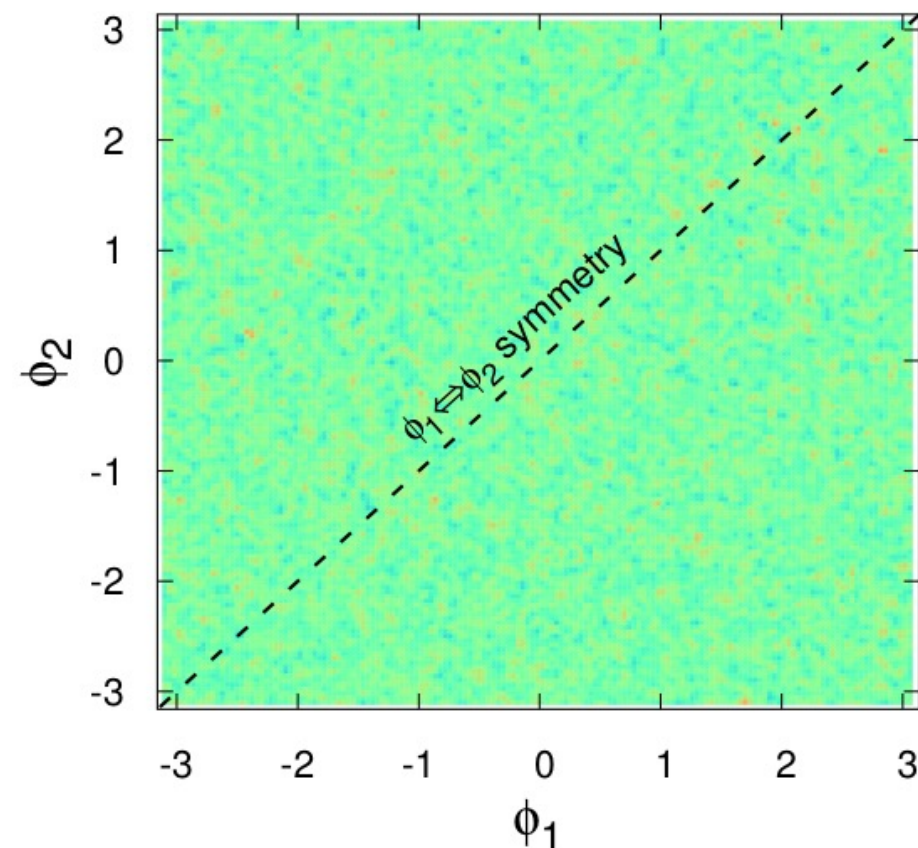
Signs of $C_{m,n,m+n}$ restrict allowed values of angles w.r.t Ψ_2

P. Sorensen
WWND'14

No restriction



No restriction



Tomography of particle flow

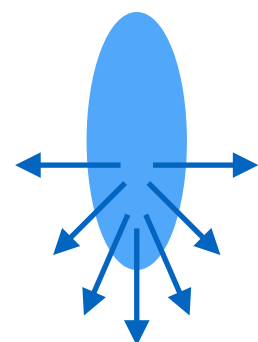
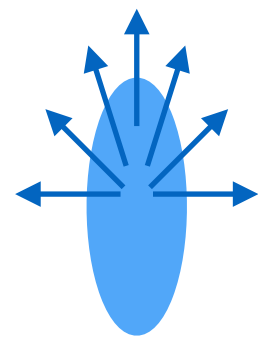
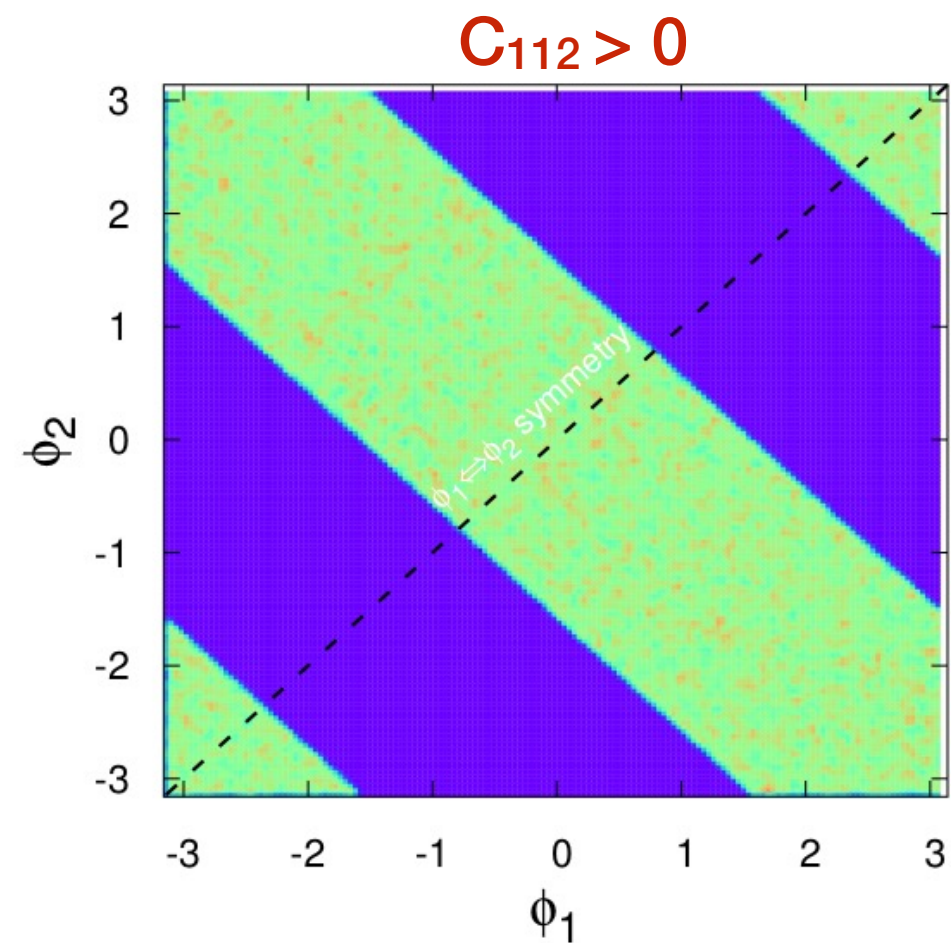
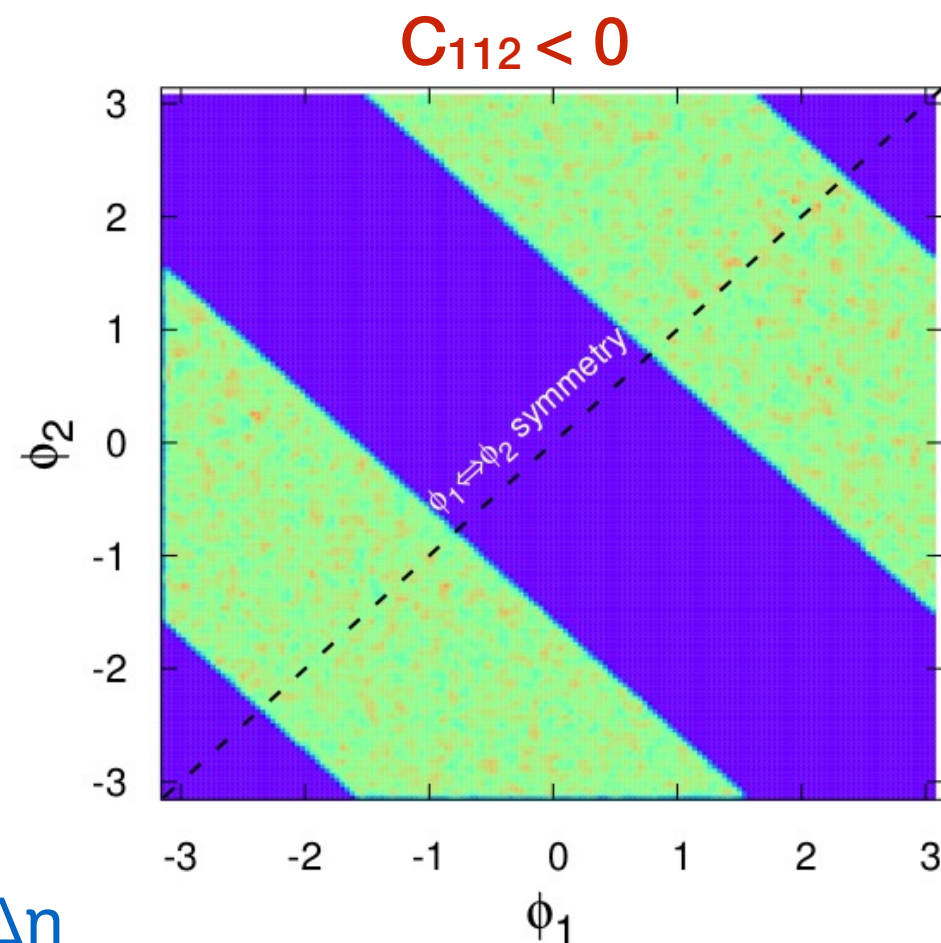
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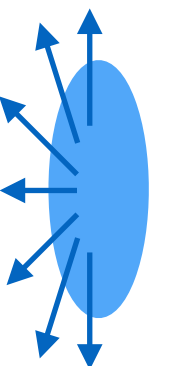
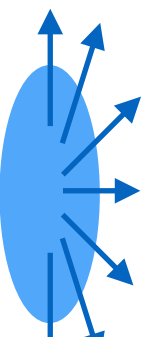
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$$\langle \cos(2\phi_1 + 2\phi_3 - 4\phi_2) \rangle / v_2 \approx \langle \cos(2\phi'_1 - 4\phi'_2) \rangle$$

$$\langle \cos(2\phi_3 + 3\phi_1 - 5\phi_2) \rangle / v_2 \approx \langle \cos(3\phi'_1 - 5\phi'_2) \rangle$$



small $\Delta\eta$

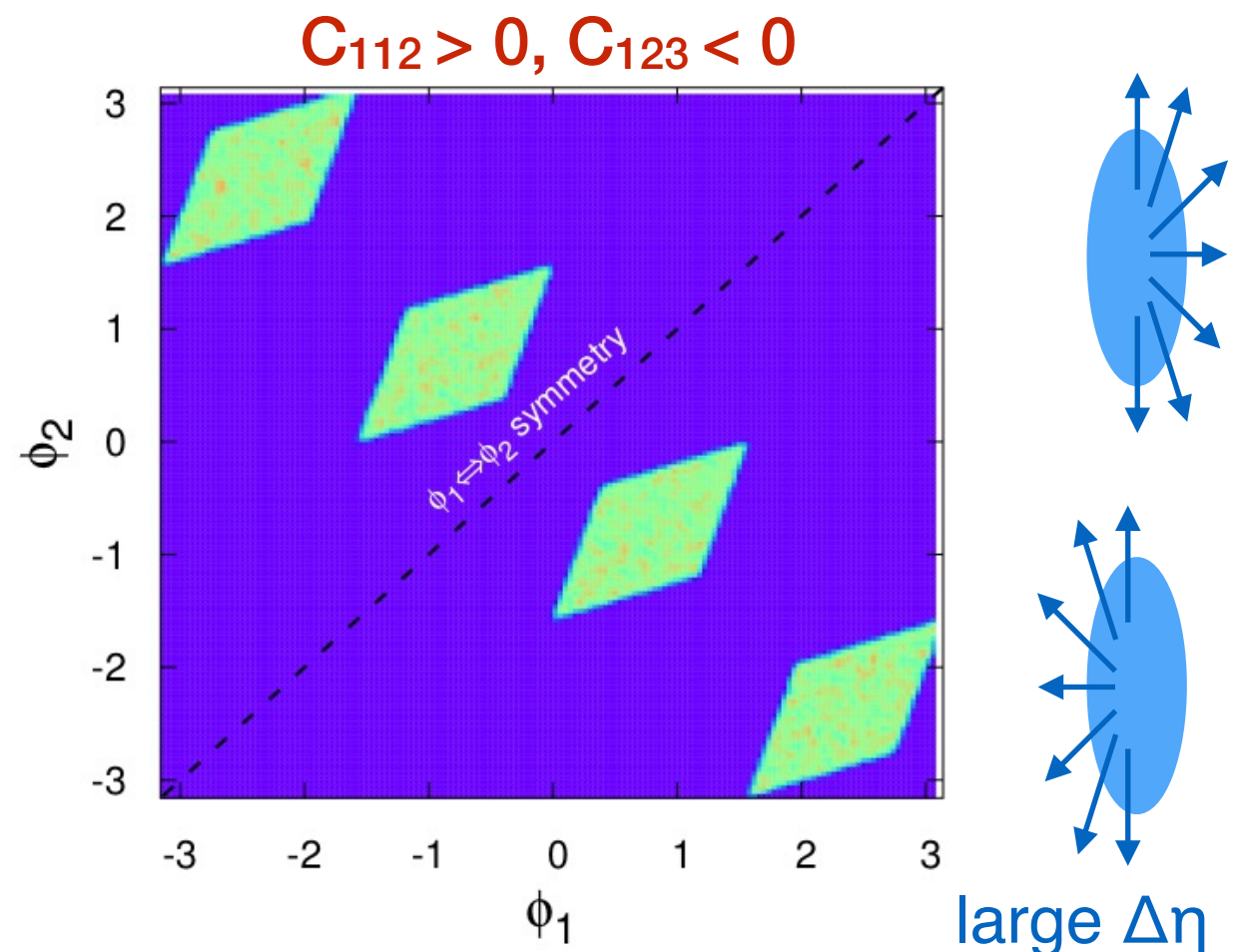
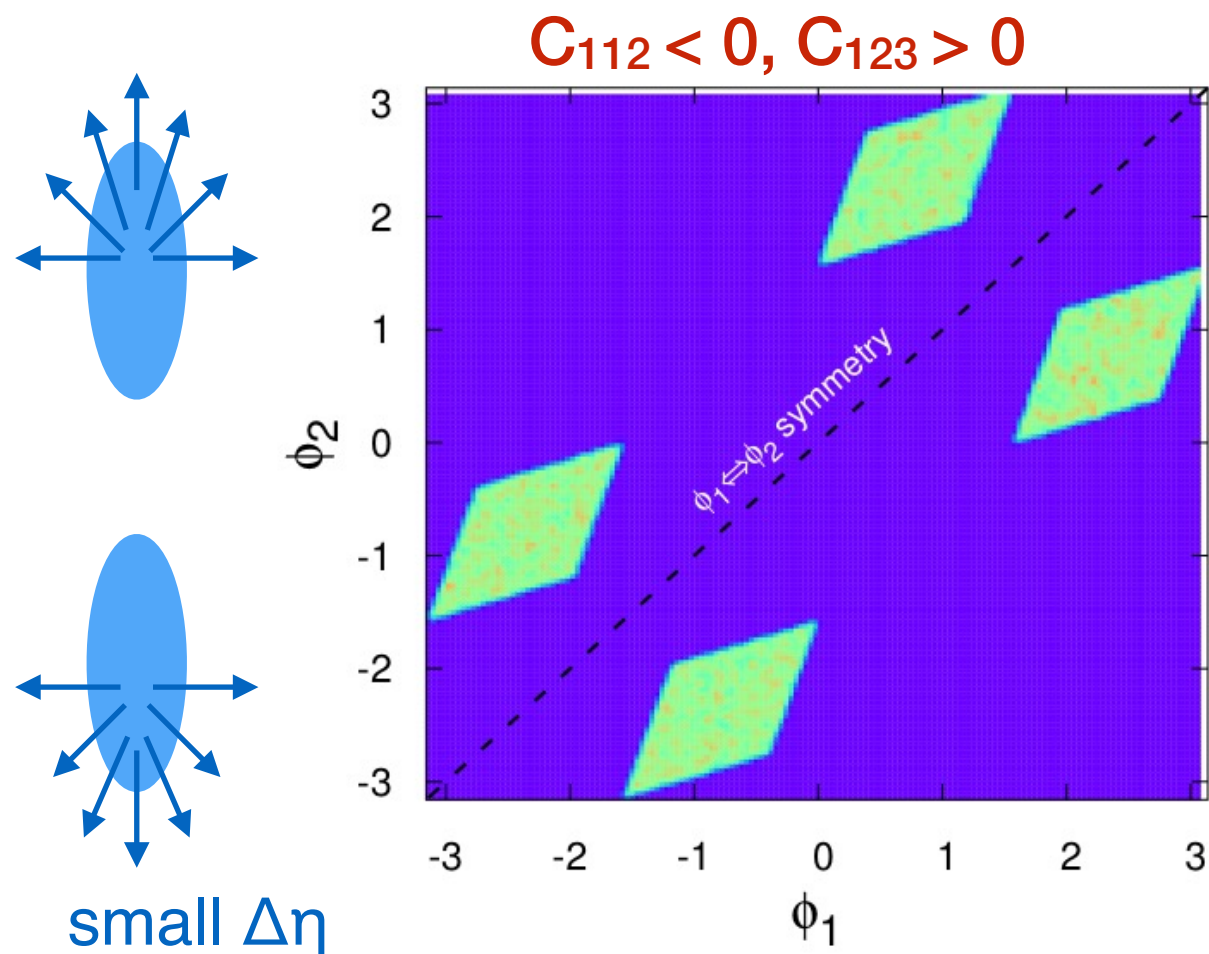


large $\Delta\eta$

Tomography of particle flow

Combining all results together can give us a picture of collisions

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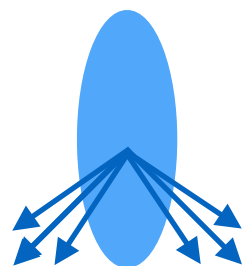
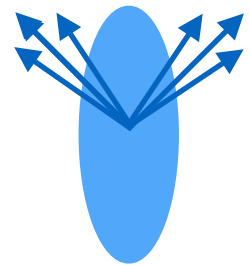
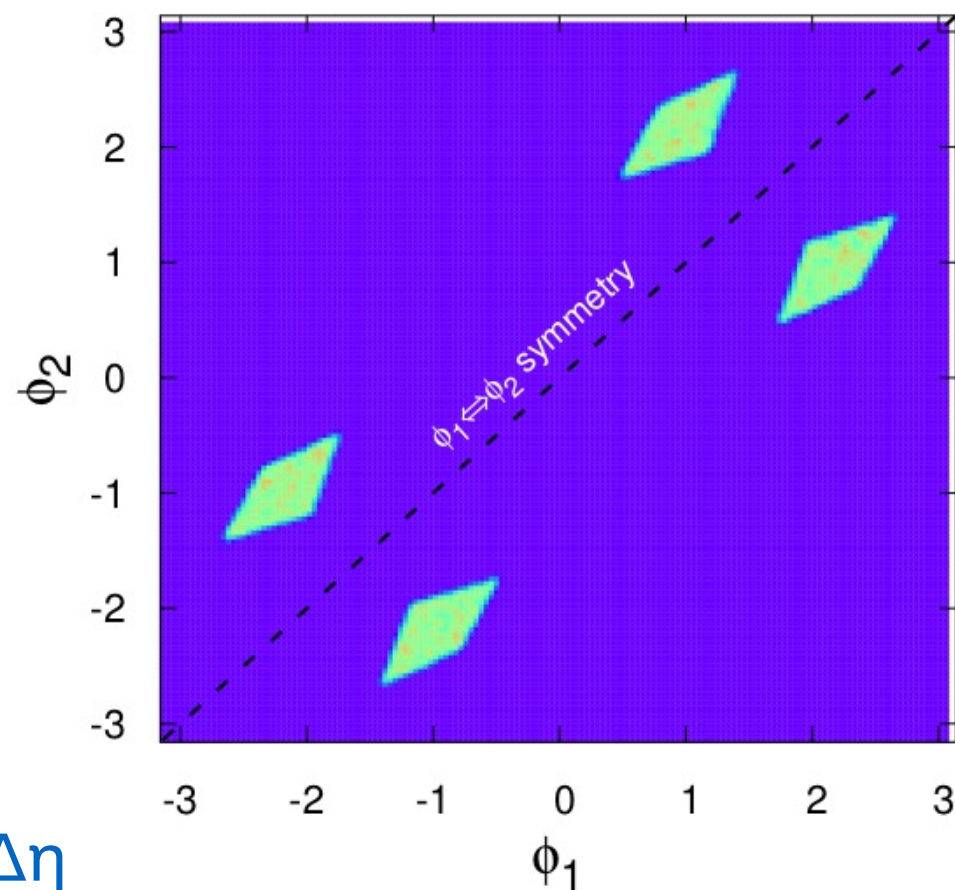


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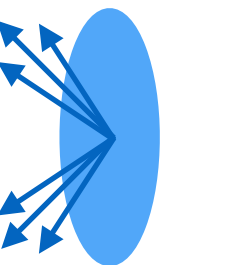
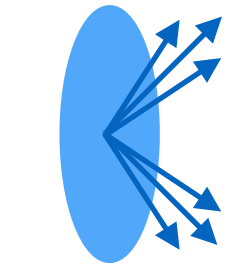
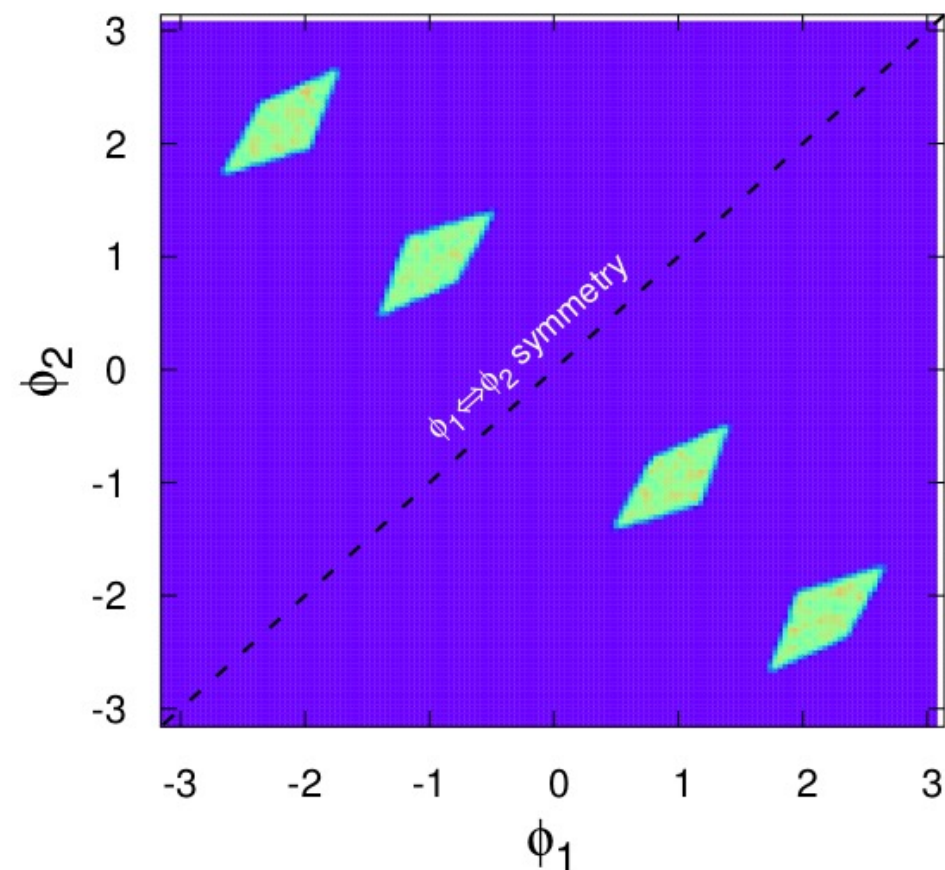
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$C_{112} < 0, C_{123} > 0, C_{224} > 0$



small $\Delta\eta$

$C_{112} > 0, C_{123} < 0, C_{224} > 0$



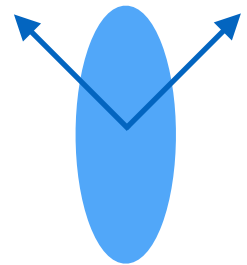
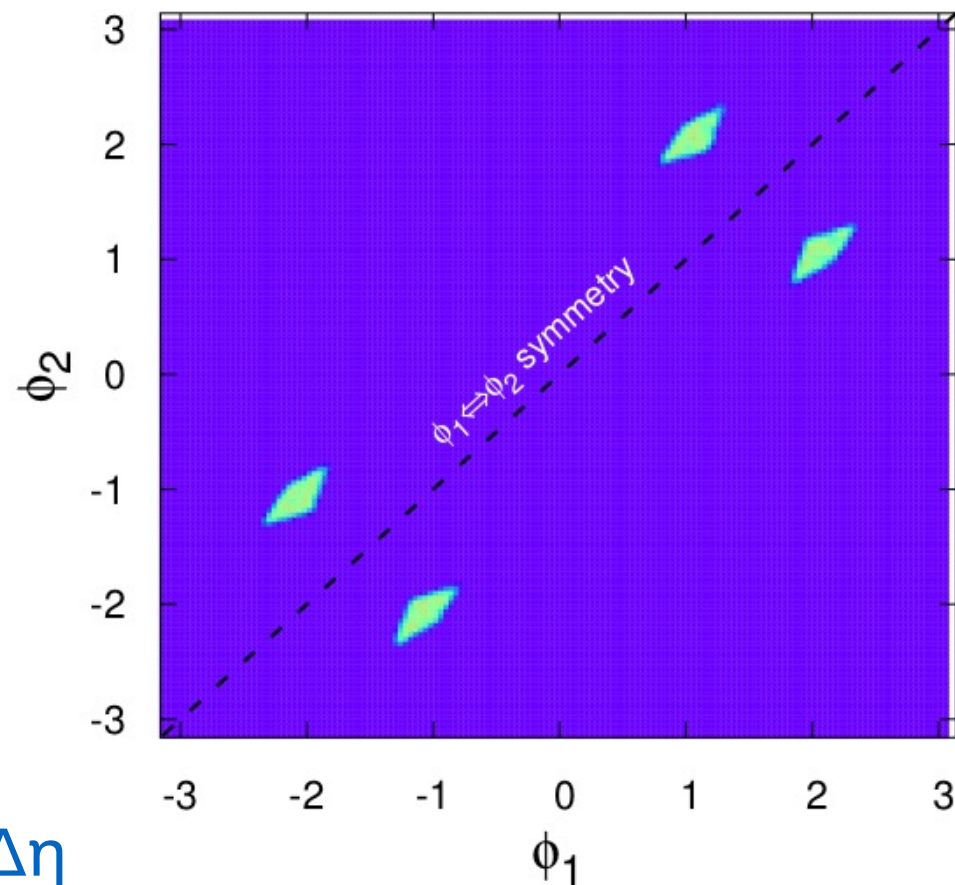
large $\Delta\eta$

Tomography of particle flow

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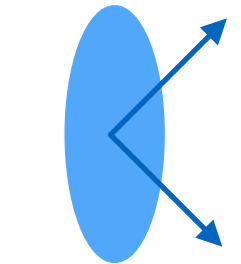
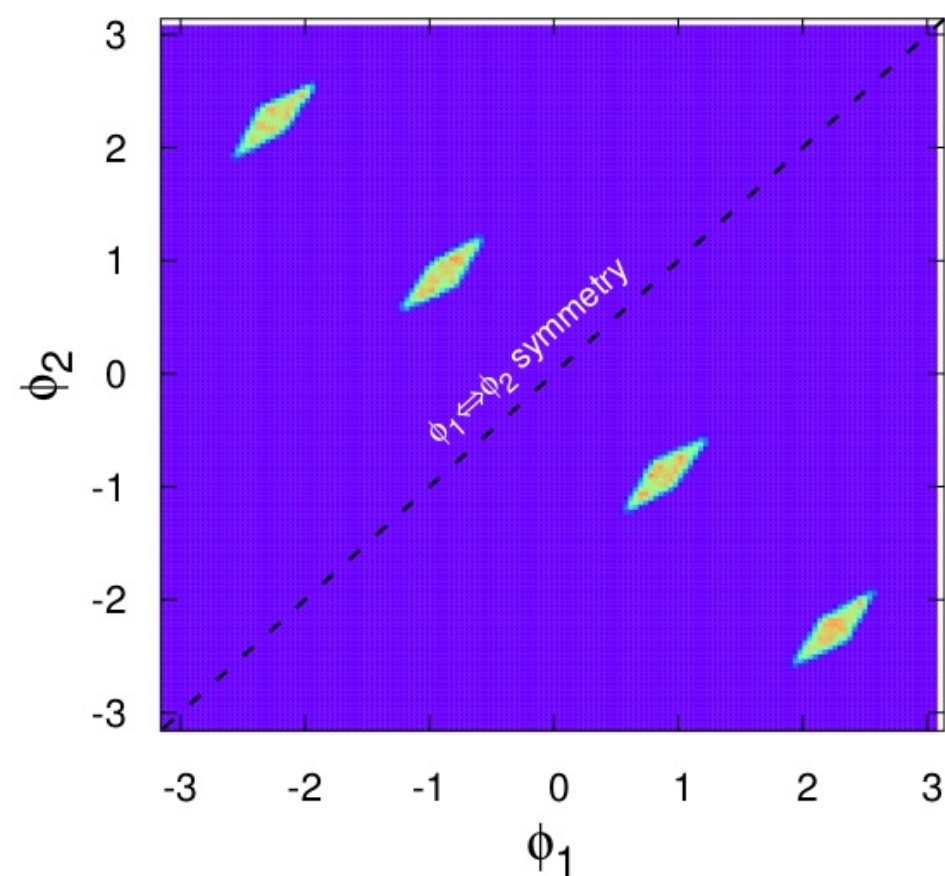
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$C_{112} < 0, C_{123} > 0, C_{224} > 0, C_{235} > 0$



small $\Delta\eta$

$C_{112} > 0, C_{123} < 0, C_{224} > 0, C_{235} > 0$



large $\Delta\eta$

Summary

Measurement of charge inclusive three particle correlations :

- Goes beyond conventional measurements of flow
- Potential for constraining η/s (T)
- Indicates presence of non-linear hydrodynamic response
- Constrains modeling of 3D-initial state and hydro evolution

Outlook

PID, charge dependence of $C_{m,n,m+n}$

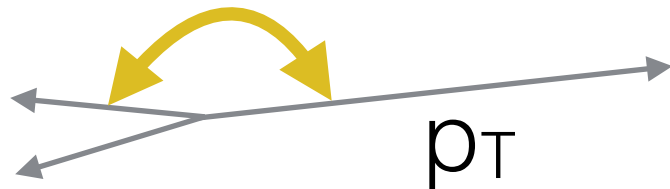
Measurement of $C_{m,n,m+n}$ over wider rapidity range with STAR upgrade

Backup

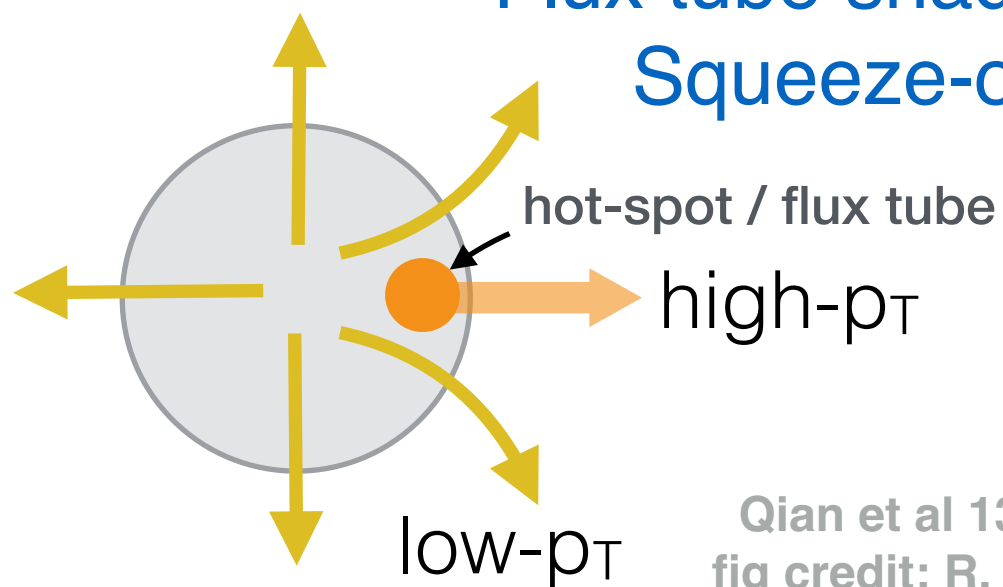
Motivation-IV (Insights beyond flow-I)

p_T dependence of $C_{m,n,m+n}$

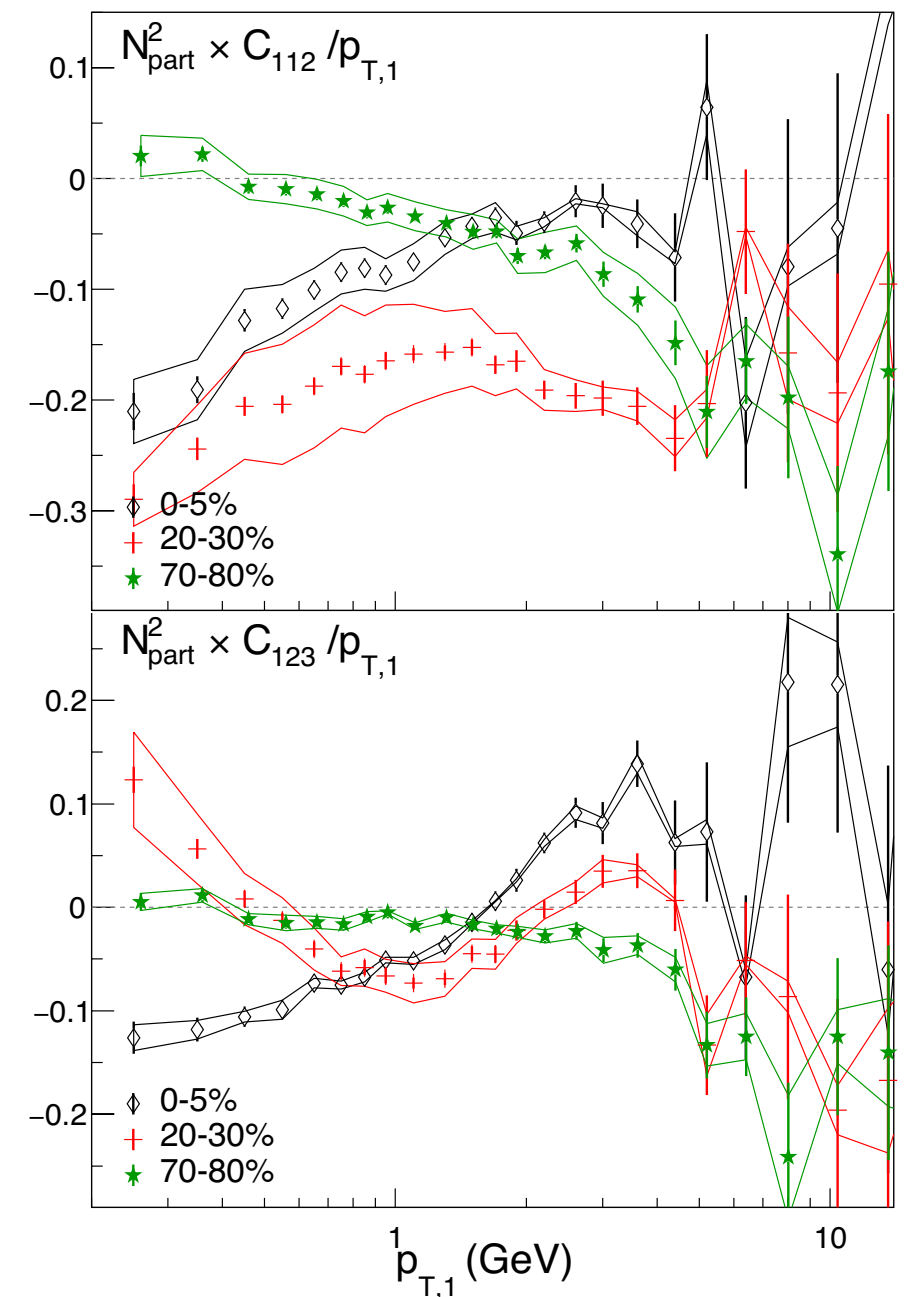
Momentum conservation



Flux tube shadowing
Squeeze-out



Qian et al 1305.4673
fig credit: R. Longacre

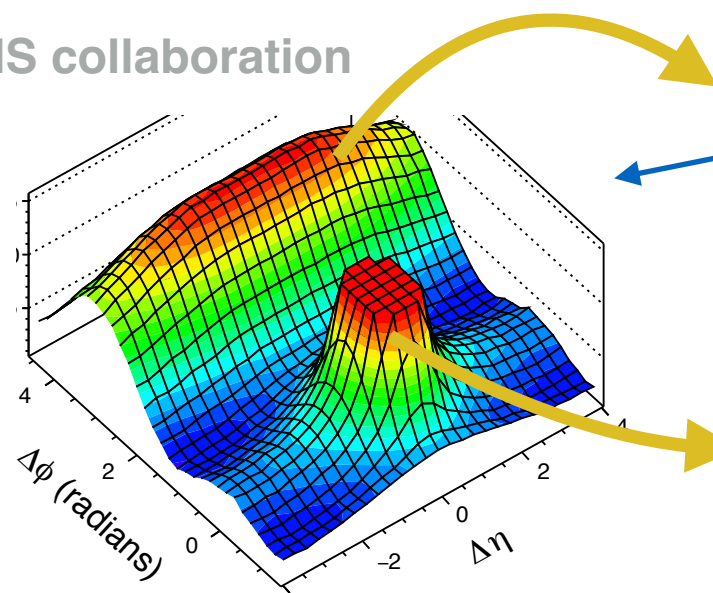


Motivation-IV (Insights beyond flow-II)

$\Delta\eta$ dependence of $C_{m,n,m+n}$

Jets/mini-jets correlated to reaction plane

fig : CMS collaboration



large $\Delta\eta_{13} \rightarrow$ forced to be back-to-back

$$C_{1\bar{2}3} \sim \cos(-3\pi), \cos(\pi) \rightarrow (-1)$$

$$C_{2\bar{2}4} \sim \cos(-4\pi), \cos(2\pi) \rightarrow (+1)$$

$$C_{1\bar{2}3} \sim (\cos(0), \cos(-2\pi)) \rightarrow (+1)$$

$$C_{2\bar{2}4} \sim (\cos(0), \cos(-2\pi)) \rightarrow (+1)$$

small $\Delta\eta_{13} \rightarrow$ no constrain, more probable to be same-sided

