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on Multiparticle Dynamics
ISMD2016**

**Jeju Island, South Korea
August 29 – September 2
2016**



**Top-Quark p_T -Spectra at LHC
and Flavor Independence of z -Scaling**

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*JINR, Dubna, Russia

** NPI Řež, Czech Republic



Contents

- Introduction (motivation & goals)
- z -Scaling (principles, ideas, definitions,...)
- Properties of z -Scaling
 - Flavor independence of $\Psi(z)$
- Self-similarity:
 - Top-quark production at Tevatron & LHC
- Conclusions



Fundamental principles and symmetries



"Fundamental symmetry principles dictate the basic laws of physics, control the structure of matter, and define the fundamental forces in Nature."

Leon M. Lederman

Self-similarity is a property of physical phenomena and the principle to construct theories.

Top flavor is a fundamental property of quark and has relevance to the structure of the momentum space at small scales.

Top physics is a pillar of the current research program in HEP and provide stringent tests of SM.



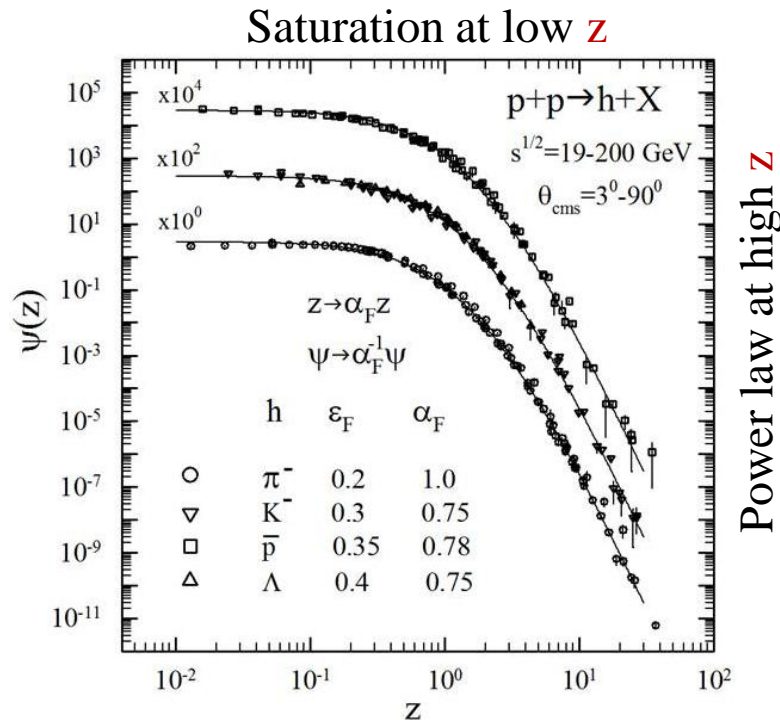
z-Scaling - Universality & Saturation

Inclusive cross sections of $\pi^-, K^-, \bar{p}, \Lambda$ in pp collisions

FNAL:
PRD 75 (1979) 764

ISR:
NPB 100 (1975) 237
PLB 64 (1976) 111
NPB 116 (1976) 77
(low p_T)
NPB 56 (1973) 333
(small angles)

STAR:
PLB 616 (2005) 8
PLB 637 (2006) 161
PRC 75 (2007) 064901



Energy scan of spectra at U70, ISR, S \bar{p} pS, SPS, HERA, FNAL(fixed target), Tevatron, RHIC, LHC

MT & I.Zborovsky
T.Dedovich

Phys.Rev.D75,094008(2007)
Int.J.Mod.Phys.A24,1417(2009)
J. Phys.G: Nucl.Part.Phys.
37,085008(2010)
Int.J.Mod.Phys.A27,1250115(2012)
J.Mod.Phys.3,815(2012)

- Energy & angular independence
- Flavor independence (π, K, \bar{p}, Λ)
- Saturation for $z < 0.1$
- Power law $\Psi(z) \sim z^{-\beta}$ for high $z > 4$

Scaling – “collapse” of data points onto a single curve.



Motivation & Goals

Development of **z-scaling** approach for description of **hadron**, **direct photon** and **jet** production in inclusive reactions to search for signatures of new physics (phase transitions, quark compositeness, extra dimensions, black holes, fractality of space-time, **complementary restrictions for theory**,...)

Analysis of new experimental data on **p_T-spectra** of **top-quark** production in **p \bar{p}** and **pp** collisions obtained at **Tevatron** and **LHC** to verify properties of **z-scaling**.

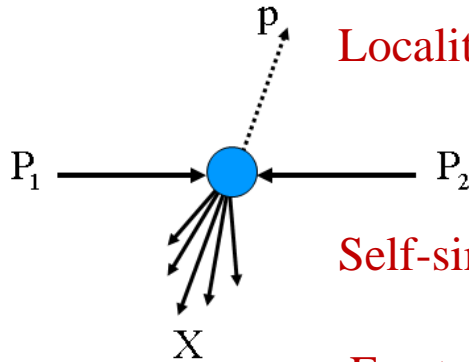
It concerns to

- Properties of sub-structure of the colliding objects, interactions of their constituents, and fragmentation process at small scales.
- Fractal properties of flavor (u,d,s,c,b,t)
- Fundamental principles (self-similarity, scale relativity, fractality, Lorentz invariance,...)
- Origin of mass, spin, charge,...., fractal topology of space-time,....



z-Scaling

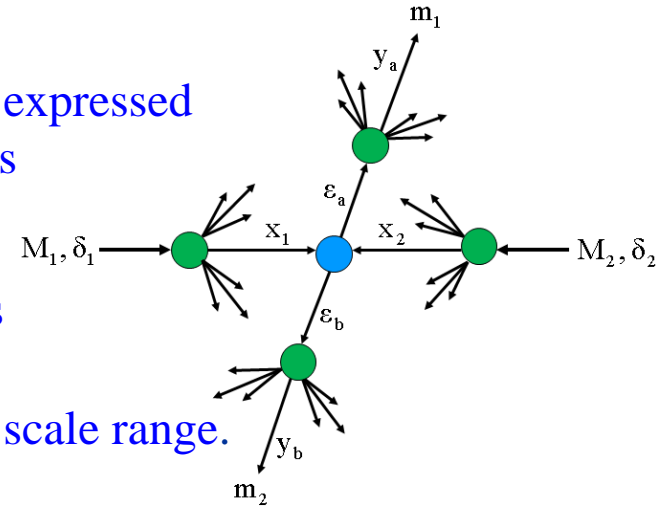
Principles: locality, self-similarity, fractality



Locality: collisions of hadrons and nuclei are expressed via interactions of their constituents (partons, quarks and gluons,...).

Self-similarity: interactions of the constituents are mutually similar.

Fractality: self-similarity is valid over a wide scale range.



Hypothesis of **z**-scaling :

$s^{1/2}, p_T, \theta_{\text{cms}}$ Inclusive particle distributions can be described in terms of constituent sub-processes and parameters characterizing bulk properties of the system.

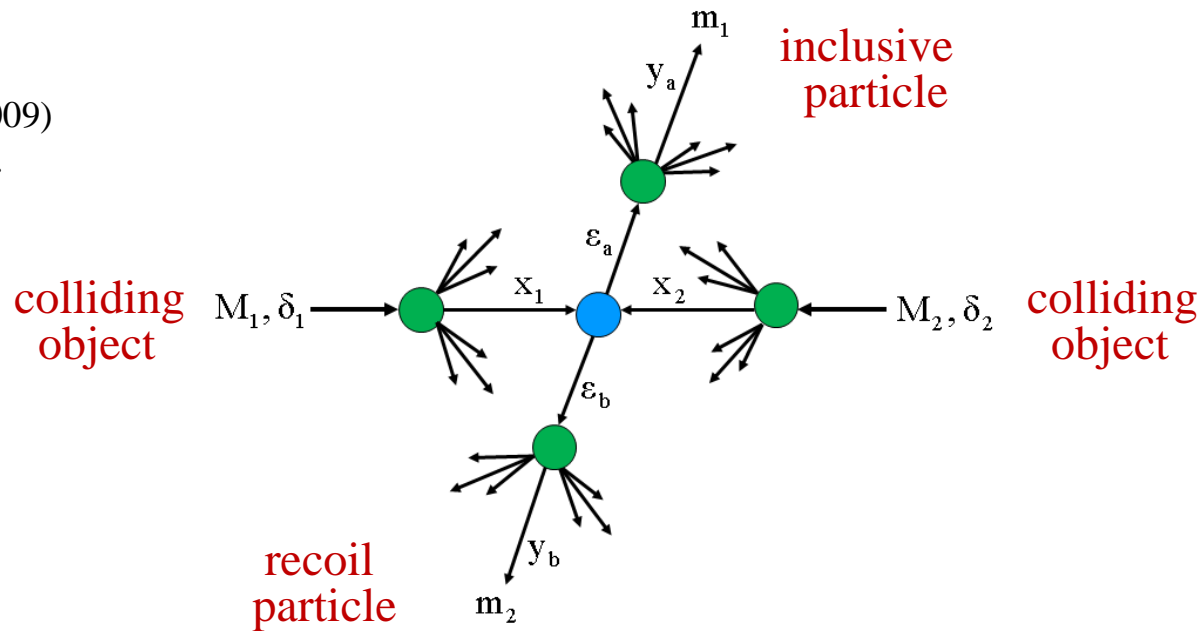
x_1, x_2, y_a, y_b
 $\delta_1, \delta_2, \epsilon_a, \epsilon_b, c$

$Ed^3\sigma/dp^3$ Scaled inclusive cross section of particles depends in a self-similar way on a single scaling variable z .

$\Psi(z)$

Locality of hadron interactions

M.T. & I.Zborovský
 Part.Nucl.Lett.312(2006)
 PRD75,094008(2007)
 Int.J.Mod.Phys.A24,1417(2009)
 J.Phys.G: Nucl.Part.Phys.
 37,085008(2010)



Constituent subprocess

$$(\mathbf{x}_1 M_1) + (\mathbf{x}_2 M_2) \Rightarrow (m_1/y_a) + (\mathbf{x}_1 M_1 + \mathbf{x}_2 M_2 + m_2/y_b)$$

Kinematical condition (4-momentum conservation law):

$$(\mathbf{x}_1 P_1 + \mathbf{x}_2 P_2 - p/y_a)^2 = M_X^2$$

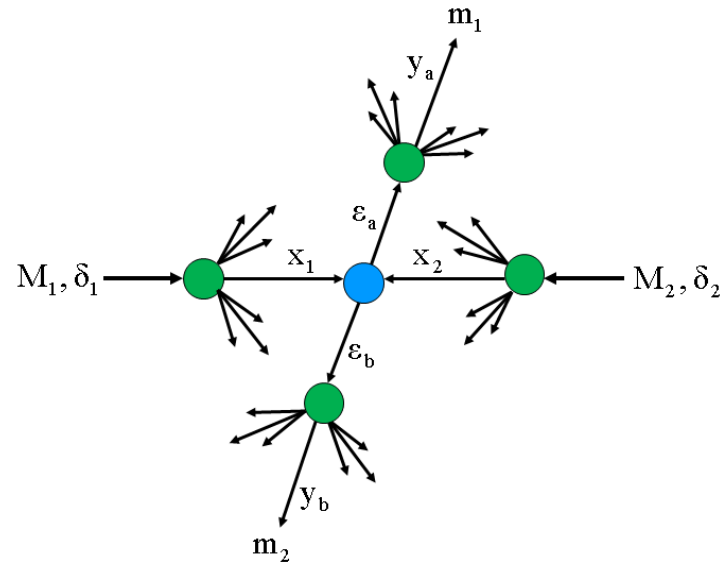
Recoil mass: $M_X = \mathbf{x}_1 M_1 + \mathbf{x}_2 M_2 + m_2/y_b$



Z as self-similarity parameter

$$Z = z_0 \cdot \Omega^{-1}$$

$$z_0 = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m}$$



- Ω^{-1} is the minimal resolution at which a constituent subprocess can be singled out of the inclusive reaction
- $s_{\perp}^{1/2}$ is the transverse kinetic energy of the subprocess consumed on production of m_1 & m_2
- $dN_{ch}/d\eta|_0$ is the multiplicity density of charged particles at $\eta = 0$
- c is a parameter interpreted as a “specific heat” of created medium
- m is an arbitrary constant (fixed at the value of nucleon mass)

z as fractal measure

The fractality is reflected in definition of z

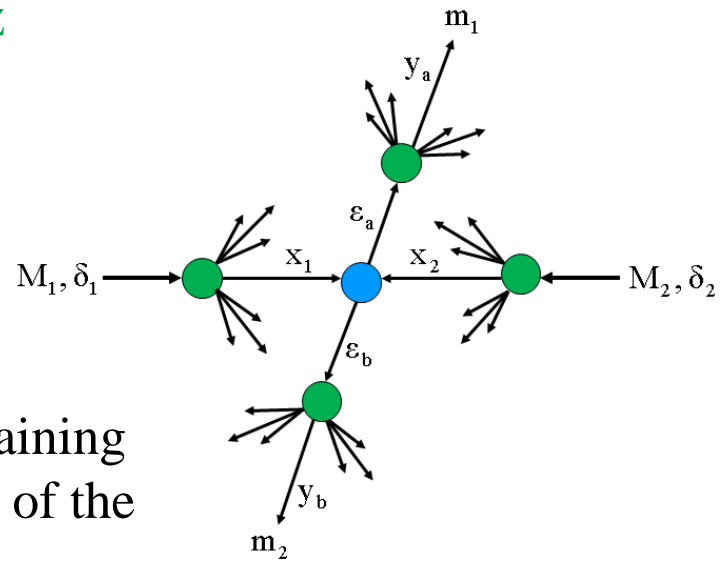
$$z = z_0 \cdot \Omega^{-1}$$

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

Ω is relative number of configurations containing a sub-process with fractions x_1, x_2, y_a, y_b of the corresponding 4-momenta

$\delta_1, \delta_2, \varepsilon_a, \varepsilon_b$ are parameters characterizing structure of the colliding objects and fragmentation process, respectively

$\Omega^{-1}(x_1, x_2, y_a, y_b)$ characterizes resolution at which a constituent sub-process can be singled out of the inclusive reaction



$$z(\Omega) \Big|_{\Omega^{-1} \rightarrow \infty} \rightarrow \infty$$

The fractal measure z diverges as the resolution Ω^{-1} increases.

Momentum fractions x_1, x_2, y_a, y_b

Principle of minimal resolution: The momentum fractions x_1, x_2 and y_a, y_b are determined in a way to minimize the resolution Ω^{-1} of the fractal measure z with respect to all constituent sub-processes taking into account 4-momentum conservation:

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

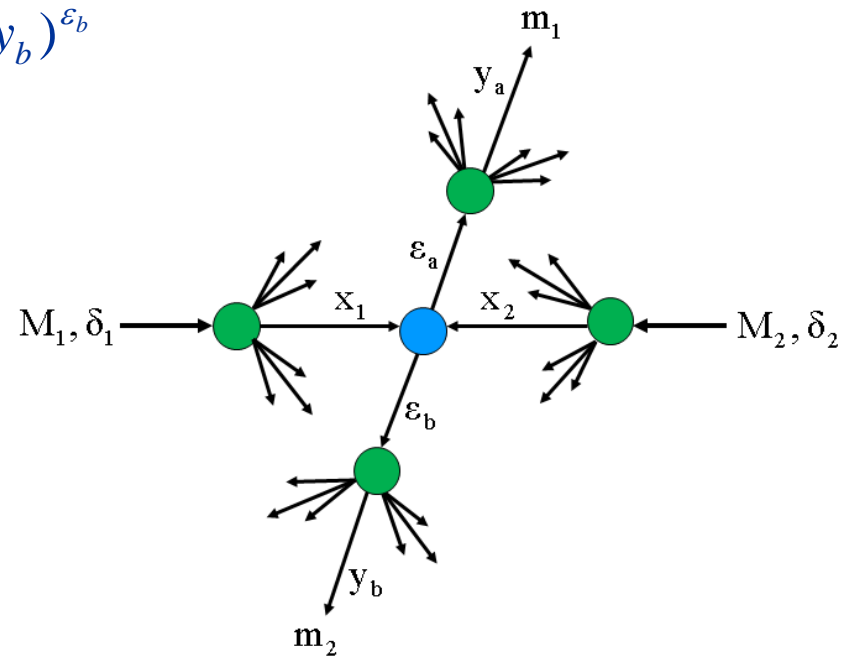
$$\begin{cases} \partial\Omega / \partial x_1 \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial x_2 \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial y_b \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \end{cases}$$

Momentum conservation law)

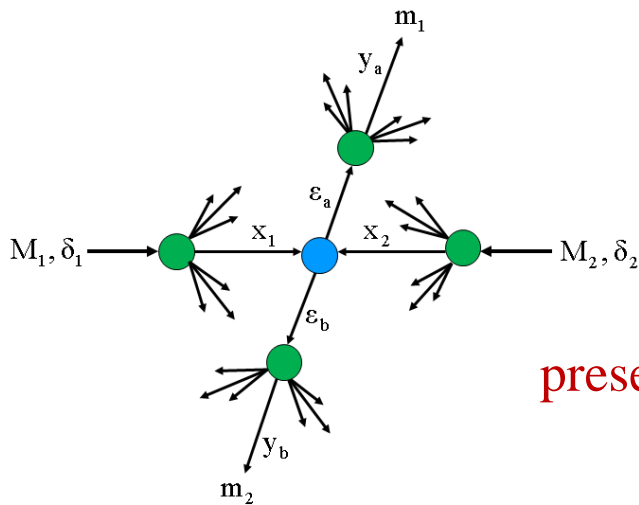
$$(x_1 P_1 + x_2 P_2 - p / y_a)^2 = M_X^2$$

Recoil mass

$$M_X = x_1 M_1 + x_2 M_2 + m_2 / y_b$$



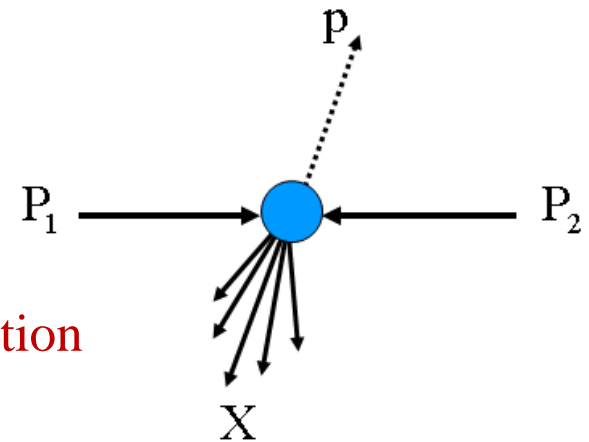
Scaling function $\Psi(z)$



$$\int_0^{\infty} \Psi(z) dz = 1$$

Scale transformation
preserves the normalization condition

$$z \rightarrow \alpha_F z, \quad \Psi \rightarrow \alpha_F^{-1} \Psi$$



$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3} \iff \int E \frac{d^3\sigma}{dp^3} dy d^2p_{\perp} = \sigma_{inel} \cdot N$$

- σ_{in} - inelastic cross section
- N - average multiplicity of the corresponding hadron species
- $dN/d\eta$ - pseudorapidity multiplicity density at angle θ (η)
- $J(z, \eta; p_T^2, y)$ - Jacobian
- $E d^3\sigma/dp^3$ - inclusive cross section

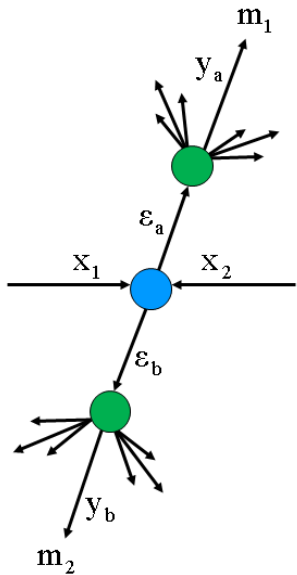
The scaling function $\Psi(z)$ is probability density to produce an inclusive particle with the self-similarity parameter z .

Transverse kinetic energy $\sqrt{s_{\perp}}$

$$s_{\perp}^{1/2} = \underbrace{y_1 (s_{\lambda}^{1/2} - M_1 \lambda_1 - M_2 \lambda_2) - m_1}_{\text{energy consumed for the inclusive particle } m_1} + \underbrace{y_2 (s_{\chi}^{1/2} - M_1 \chi_1 - M_2 \chi_2) - m_2}_{\text{energy consumed for the recoil particle } m_2}$$

energy consumed
for the inclusive particle m_1

energy consumed
for the recoil particle m_2



Fraction decomposition: $x_{1,2} = \lambda_{1,2} + \chi_{1,2}$

$$\lambda_{1,2} = \kappa_{1,2}/y_1 + v_{1,2}/y_2$$

$$\chi_{1,2} = (\mu_{1,2}^2 + \omega_{1,2}^2)^{1/2} \mp \omega_{1,2}$$

$$\omega_{1,2} = \mu_{1,2} U, \quad U = \frac{\alpha - 1}{2\sqrt{\alpha}} \xi, \quad \alpha = \frac{\delta_2}{\delta_1}$$

$$\xi^2 = (\lambda_1 \lambda_2 + \lambda_0) / [(1 - \lambda_1)(1 - \lambda_2)]$$

$$\kappa_{1,2} = \frac{(P_{2,1} p)}{(P_2 P_1)}, \quad v_{1,2} = \frac{M_{2,1} m_2}{(P_2 P_1)}$$

$$\mu_{1,2}^2 = \alpha^{\pm 1} (\lambda_1 \lambda_2 + \lambda_0) \frac{1 - \lambda_{1,2}}{1 - \lambda_{2,1}}$$

$$\lambda_0 = \bar{v}_0 / y_2^2 - v_0 / y_1^2$$

$$\bar{v}_0 = \frac{0.5 m_2^2}{(P_1 P_2)}, \quad v_0 = \frac{0.5 m_1^2}{(P_1 P_2)}$$

$$s_{\lambda} = (\lambda_1 P_1 + \lambda_2 P_2)^2$$

$$s_{\chi} = (\chi_1 P_1 + \chi_2 P_2)^2$$

The scaling function $\Psi(z)$ and self-similarity parameter z are expressed via Lorentz invariants.

Properties of $\Psi(z)$ in pp & $p\bar{p}$ collisions

- Energy independence of $\Psi(z)$ ($s^{1/2} > 20$ GeV)
- Angular independence of $\Psi(z)$ ($\theta_{\text{cms}}=3^0-90^0$)
- Multiplicity independence of $\Psi(z)$ ($dN_{\text{ch}}/d\eta=1.5-26$)
- Power law, $\Psi(z) \sim z^{-\beta}$, at high z ($z > 4$)
- Flavor independence of $\Psi(z)$ ($\pi, K, \phi, \Lambda, \dots, D, J/\psi, B, \Upsilon, \dots, \text{top}$)
- Saturation of $\Psi(z)$ at low z ($z < 0.1$)

These properties reflect self-similarity, locality, and fractality of the hadron interaction at constituent level.

It concerns the structure of the colliding objects, interactions of their constituents, and fragmentation process.

M.T. & I.Zborovsky

Phys.At.Nucl. 70,1294(2007)

Phys.Rev. D75,094008(2007)

Int.J.Mod.Phys. A24,1417(2009)

J. Phys.G: Nucl.Part.Phys. 37,085008(2010)

Int.J.Mod.Phys. A27,1250115(2012)

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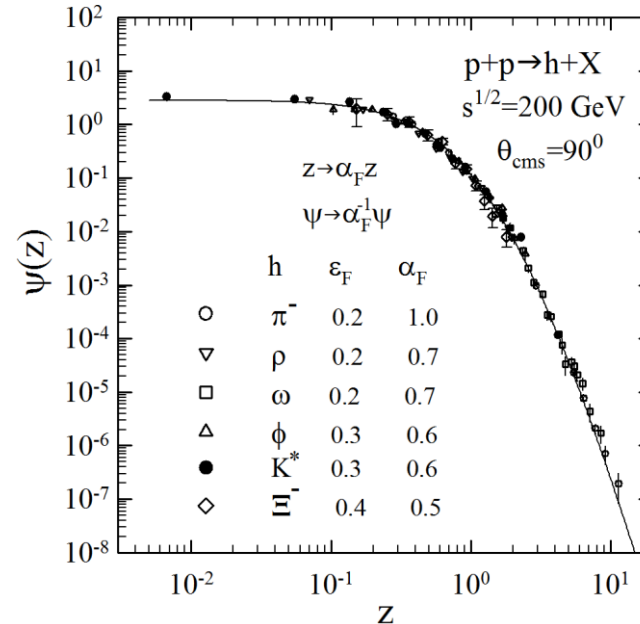
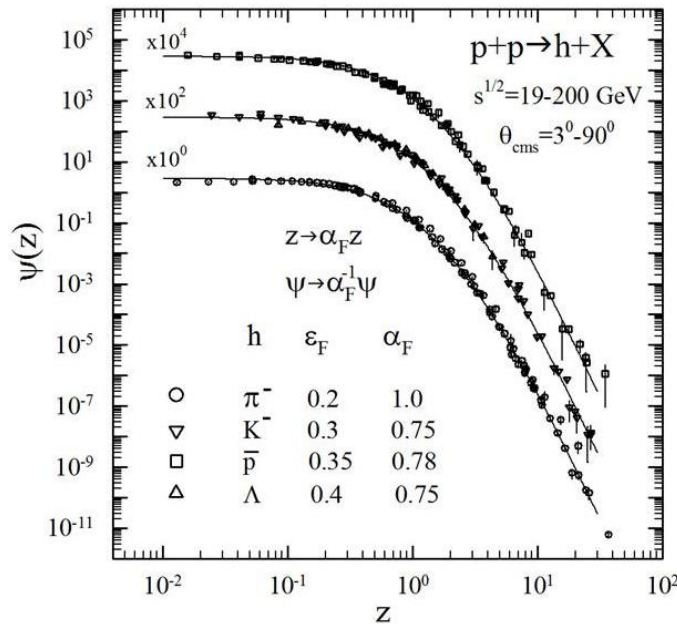
z-Scaling before LHC



Flavor independence of $\Psi(z)$ at RHIC

M.T. & I.Zborovský
 Int.J.Mod.Phys.
 A24,1417(2009)

$\pi^-, \rho, \omega, \phi, K^*, \Lambda, \Xi, J/\psi, D, B, \Upsilon$



STAR:
 PRL 92 (2004) 092301
 PLB 612 (2005) 181
 PRC 71 (2005) 064902
 PRC 75 (2007) 064901

PHENIX:
 PRC 75 (2007) 051902

- Energy independence
- Angular independence
- Flavor independence
- Saturation for $z < 0.01$

- Power law $\Psi(z) \sim z^{-\beta}$ at large z
- ε_F, α_F independent of $p_T, s^{1/2}$

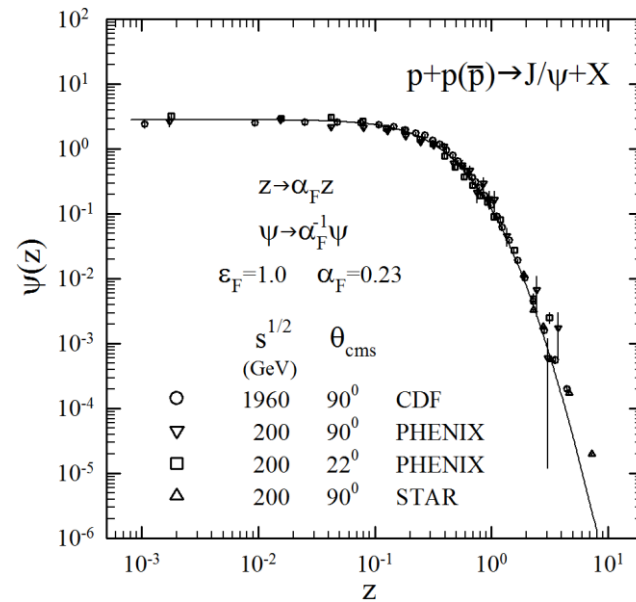
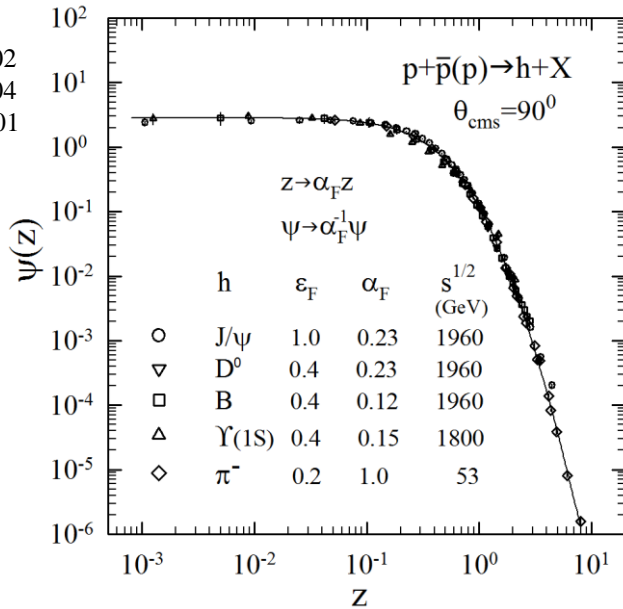
Self-similarity of particle formation with various flavor content.



Flavor independence of $\Psi(z)$ at Tevatron

$\pi^-, \rho, \omega, \phi, K^*, \Lambda, \Xi, J/\psi, D, B, \Upsilon$

CDF:
PRL 88 (2002) 161802
PRL 91 (2003) 241804
PRD 71 (2005) 032001



CDF:
PRD 71 (2005) 032001
PHENIX:
PRL 98 (2007) 232002
STAR:
Z.Tang
J.Phys.G35:104135, 2008

- Energy & angular independence
- Saturation of $\Psi(z)$ for $z < 0.1$
- Flavor independence of $\Psi(z)$
- Extra large $\epsilon_F=1$ for J/ψ



Self-similarity of strangeness production in pp at RHIC

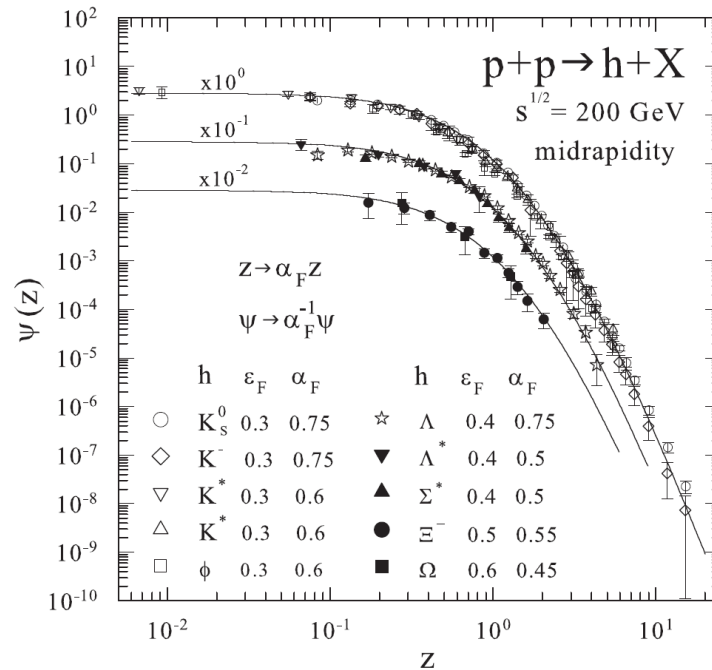
Universality: flavor independence of the scaling function

M.T. & I. Zborovský
Int.J.Mod.Phys.
A24,1417(2009)

$K_S^0, K^-, K^*, \phi, \Lambda, \Xi, \Omega, \Sigma^*, \Lambda^*$

M.T. & I. Zborovský
SQM'15
Dubna, Russia, 2015
HSQCD'16
Gatchina, Russia, 2016

Solid line for π^- meson
is a reference curve
 $\varepsilon_\pi = 0.2, \alpha_\pi = 1$



STAR:
PRL 92 (2004) 092301
PRL 97 (2006) 132301
PLB 612 (2005) 181
PRC 71 (2005) 064902
PRC 75 (2007) 064901
PRL 108 (2012) 072302

PHENIX:
PRC 75 (2007) 051902
PRD 83 (2011) 052004
PRC 90 (2014) 054905

- Energy independence
- Angular independence
- Flavor independence
- Saturation for $z < 0.01$
- Power law $\Psi(z) \sim z^{-\beta}$ at large z
- ε_F, α_F independent of $p_T, s^{1/2}$



Self-similarity of K_S^0 production in pp & $p\bar{p}$

$Sp\bar{p}S$, Tevatron, RHIC, LHC

CERN: UA5

PLB 199 (1987) 311
NPB 258 (1985) 505

CERN: UA1

PLB 366 (1996) 441

FNAL: CDF Coll.

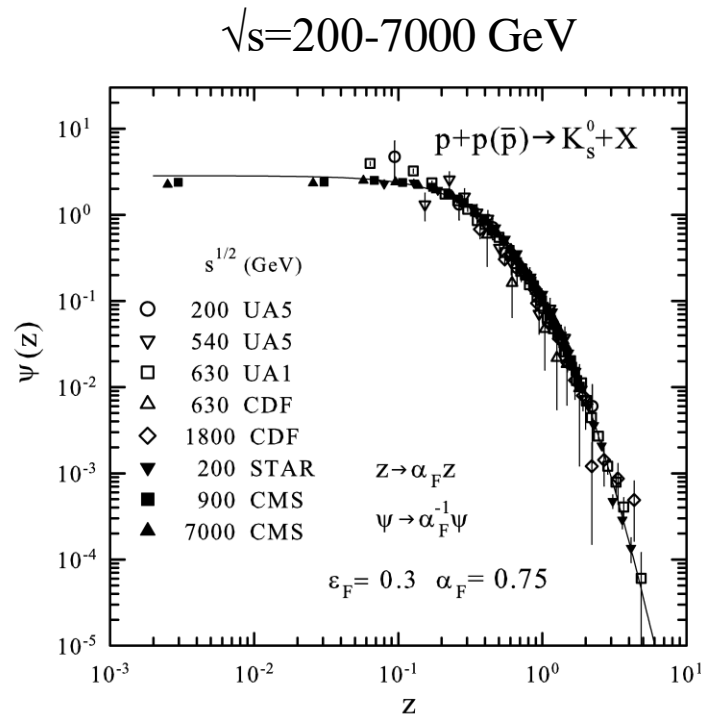
PRD 40 (1989) 3791

RHIC: STAR Coll.

PRC 75 (2007) 064901

LHC: CMS Coll.

J. High Energy Phys.05 (2011) 064



M.T. & I.Zborovský
ISMD'11
Miyajima Island,
Japan, 2011

Solid line for π^- meson
is a reference curve
 $\epsilon_\pi = 0.2, \quad \alpha_\pi = 1$

- Energy independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.01$
- Shape of $\Psi(z)$ is the same in $p\bar{p}$ and pp



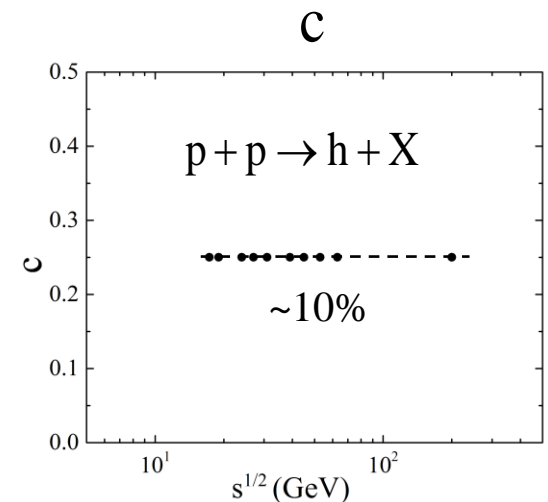
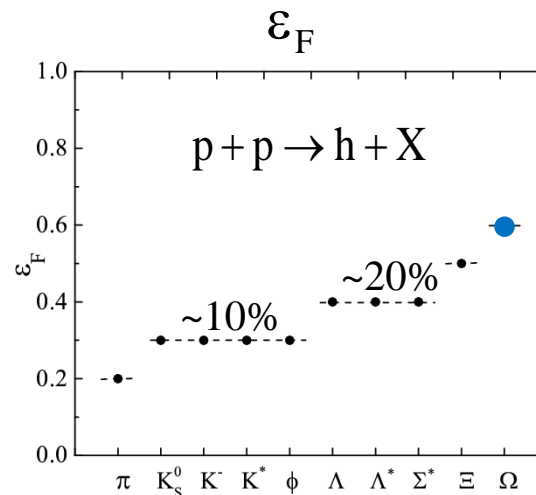
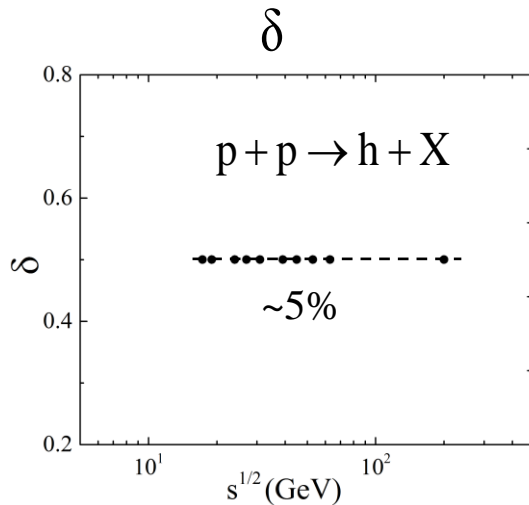
Model parameters: δ , ϵ_F , c

Parameters δ , ϵ_F , c are found from the scaling behavior of Ψ as a function of self-similarity variable z

Proton fractal dimension

Fragmentation dimension

“Specific heat”



- δ , ϵ_F , c are independent of \sqrt{s} , p_T
- ϵ_F depends on flavor

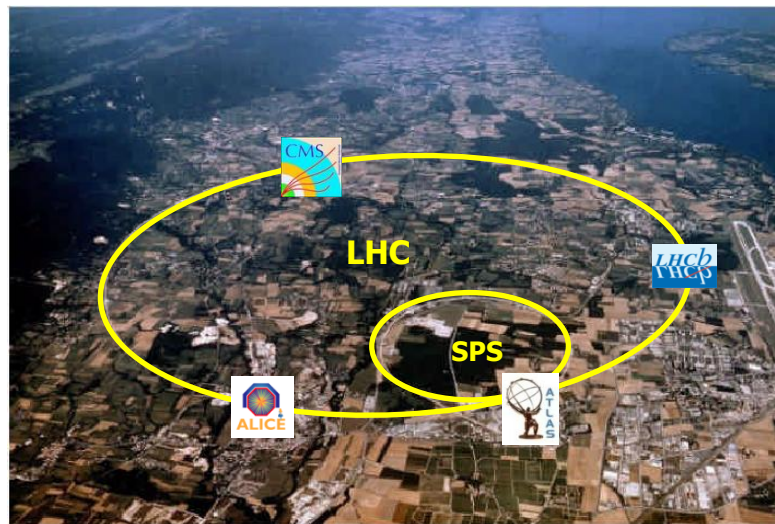
A discontinuity and strong correlation of the model parameters could give indication on new physics in pp collisions:
Search for phase transition, critical point with strange probes.



What about **self-similarity** and **flavor independence**
of $\Psi(z)$ for **top quark** production
in **pp** collisions at **LHC** ?



CERN



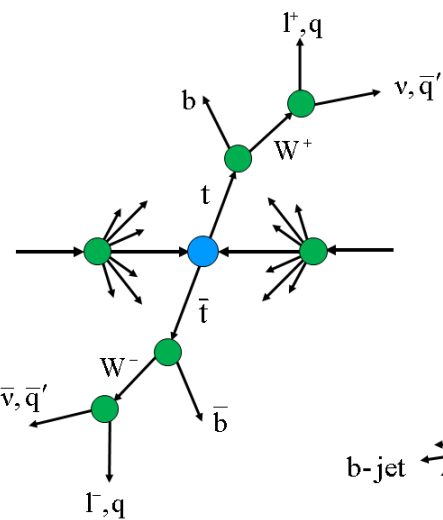
Top quark production and decay

Top-quark discovery

1995

CDF Collab. F.Abe et al.
Phys. Rev. Lett. 74 (1995)2626.
DØ Collab. S.Abachi et al.
Phys. Rev. Lett. 74(1995)2632.

$$m_t \approx 170 \text{ GeV}$$



Gluon fusion

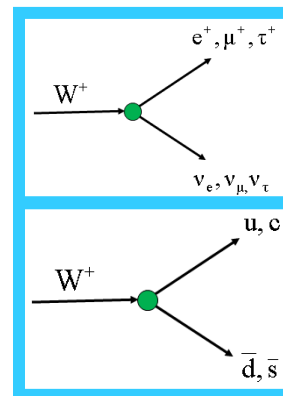
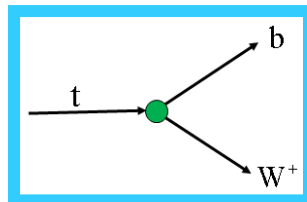


LHC	13 TeV	~ 90%
LHC	7,8 TeV	~ 85%
Tevatron	1.96 TeV	~ 15%

Quark-antiquark annihilation

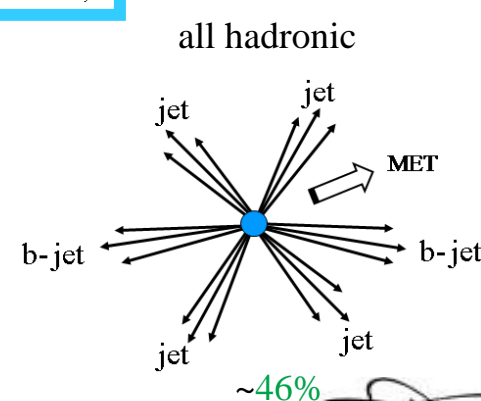
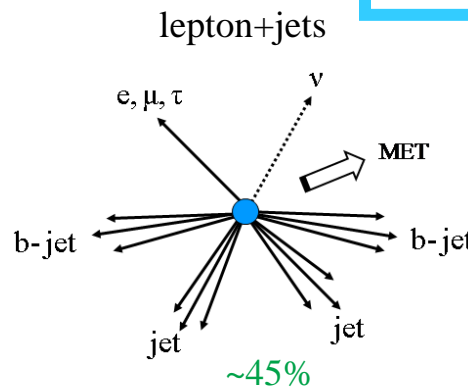
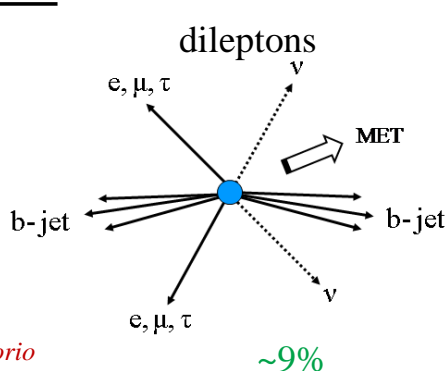


~10%
~15%
~85%



W decay modes

leptons
jets

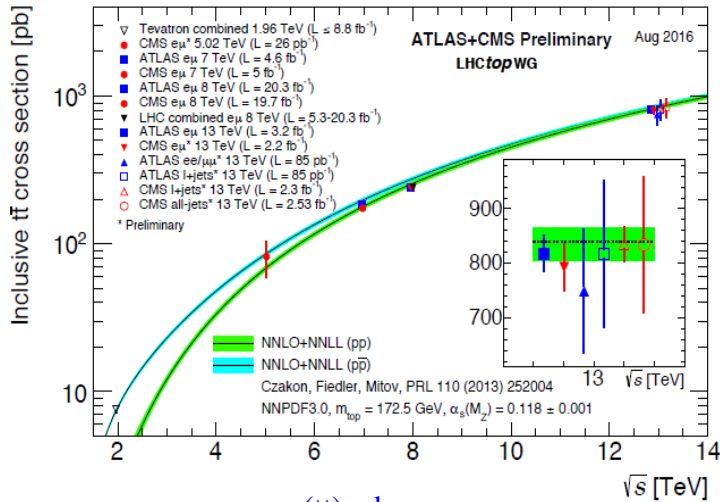


Alberto Orso Maria Iorio
(for the ATLAS, CMS, and LHCb collaborations)
DIS2016, Hamburg, Germany



Top quark properties: mass, charge, spin, width, lifetime, ...

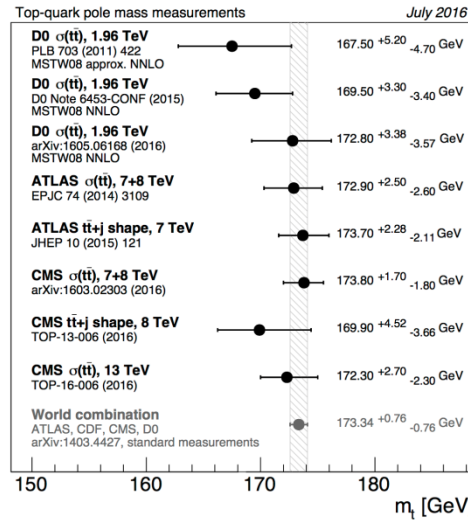
cross section



$\sigma(tt)$, pb

CMS	13 TeV	$793 \pm 8 \pm 38$	(2.2 fb^{-1})
ATLAS	13 TeV	$803 \pm 7 \pm 27$	(3.2 fb^{-1})
CMS	8 TeV	$244.9 \pm 1.4 \pm 6.3$	(19.7 fb^{-1})
ATLAS	8 TeV	$242.4 \pm 1.7 \pm 5.5$	(20.2 fb^{-1})
LHCb	8 TeV	$289 \pm 43 \pm 40$	(2.0 fb^{-1})
CMS	7 TeV	$173.6 \pm 2.1 \pm 4.5$	(5.0 fb^{-1})
ATLAS	7 TeV	$182.9 \pm 3.1 \pm 4.2$	(4.6 fb^{-1})
LHCb	7 TeV	$239 \pm 53 \pm 33$	(1.0 fb^{-1})
CMS	5 TeV	$82 \pm 20 \pm 5$	(26 pb^{-1})

mass



m_t , GeV/c^2

CDF+DØ+CMS+ATLAS
 $173.34 \pm 0.27 \pm 0.71 \text{ GeV}/c^2$
 arXiv:1403.4427

Top quark is a complementary probe to search for new physics:

$t \rightarrow Wb, V_{tb}, V_{ts}, V_{td}, \text{FCNC}: t \rightarrow Zc(u), t \rightarrow (Z, q, g)\gamma,$
 tagged jets, $t\bar{t}, t\bar{b}$ resonances, $A_C, A_{\text{FB}}, A_{\text{CP}},$
 $t\bar{t}$ spin correlations, polarization, ...

electric charge $+2/3e$
 color triplet
 spin $1/2$
 topness $+1$
 full width $2.00 \pm 0.47 \text{ GeV}$
 lifetime $\sim 3.29 \cdot 10^{-25} \text{ s}$
 decay ($\text{Br} \approx 100\%$) $W \rightarrow bt$

3 generations of quarks

u	$I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$ Mass $m = 1.5$ to 4.5 MeV $ ^2 $ Charge = $+\frac{2}{3} e$ $I_z = +\frac{1}{2}$ $m_u/m_d = 0.2$ to 0.7
d	$I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$ Mass $m = 5$ to 8.5 MeV $ ^2 $ Charge = $-\frac{1}{3} e$ $I_z = -\frac{1}{2}$ $m_s/m_d = 17$ to 22 $\bar{m} = (m_u + m_d)/2 = 2.5$ to 5.5 MeV
s	$I(J^P) = 0(\frac{1}{2}^+)$ Mass $m = 80$ to 155 MeV $ ^2 $ Charge = $-\frac{1}{3} e$ Strangeness = -1 $(m_s - (m_u + m_d)/2)/(m_d - m_u) = 30$ to 50
c	$I(J^P) = 0(\frac{1}{2}^+)$ Mass $m = 1.0$ to 1.4 GeV Charge = $+\frac{2}{3} e$ Charm = $+1$
b	$I(J^P) = 0(\frac{1}{2}^+)$ Mass $m = 4.0$ to 4.5 GeV Charge = $-\frac{1}{3} e$ Bottom = -1
t	$I(J^P) = 0(\frac{1}{2}^+)$ Charge = $+\frac{2}{3} e$ Top = $+1$ Mass $m = 174.3 \pm 5.1 \text{ GeV}$ (direct observation of top events) Mass $m = 178.1^{+10.4}_{-8.3} \text{ GeV}$ (Standard Model electroweak fit)

Jay Howarth
 (for ATLAS Collab.)
 ICHEP2016, Chicago, USA

Michelangelo L. Mangano
 ICHEP2016, Chicago, USA

Georgios Daskalakis
 (for CMS Collab.)
 ICNFP2016, Crete, Greece

Alberto Orso Maria Iorio
 (for the ATLAS, CMS, and LHCb Collab.)
 DIS2016, Hamburg, Germany

Antonio Limosani
 (for ATLAS Collab.)
 ICHEP2016, Chicago, USA

J. Fernandez
 (for ATLAS, CDF, CMS, DØ Collab.)
 LHCP16, Lund, Sweden



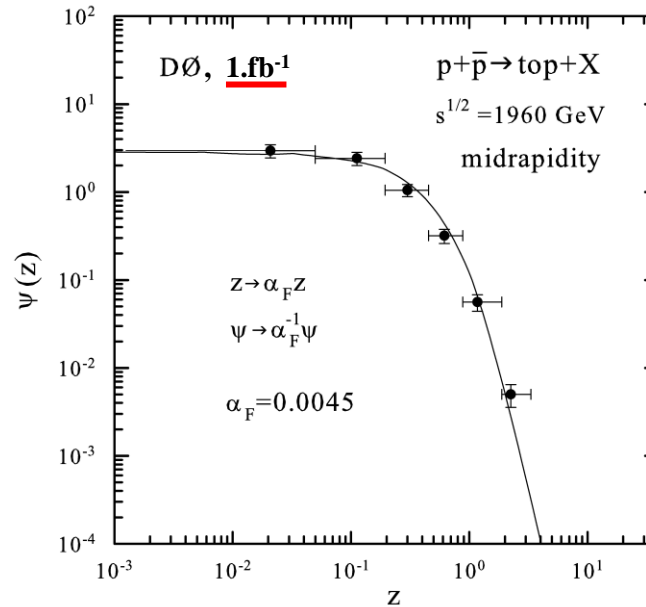
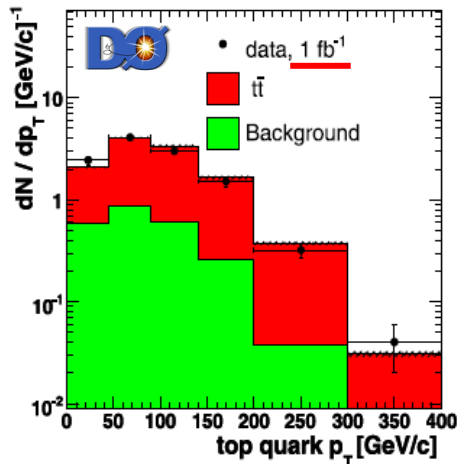
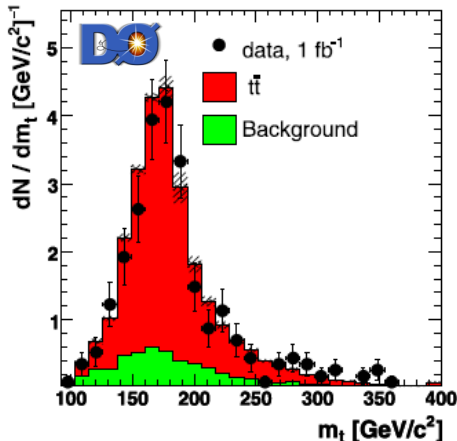
Top flavor & z-Scaling

$p\bar{p}$ & pp @ 1.96,7,8 TeV
low integral luminosity



Self-similarity of top quark production at Tevatron

DØ Collaboration V.M. Abazov et al.
Phys.Lett. B 693 (2010) 515.



M.T. & I.Zborovský
JINR E2-2012-12
J.Mod.Phys. 3(2012)815

- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for or $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\varepsilon_{\text{top}} = 0$
- “Specific heat” $c = 0.25$

Very small energy loss in the elementary $\bar{t}t$ production process.

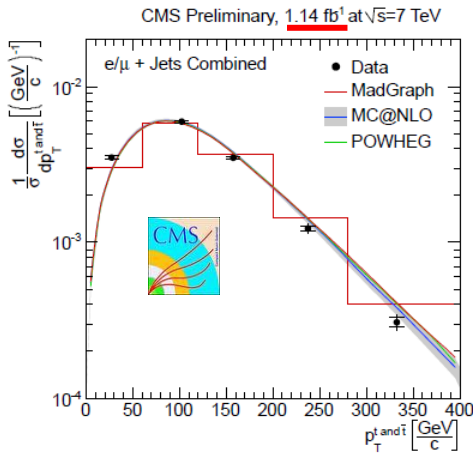
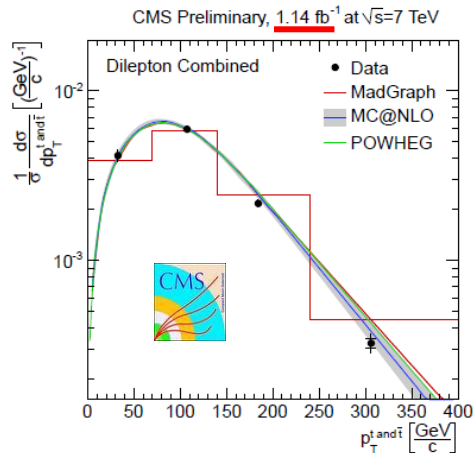
- Measurements of p_T and m_T distributions
- Probing large momentum $20 < p_T < 400 \text{ GeV}/c$
- NLO, NNLO, MC@NLO, $m_t = 170 \text{ GeV}$

DØ data confirm self-similarity of top quark production in $p\bar{p}$.

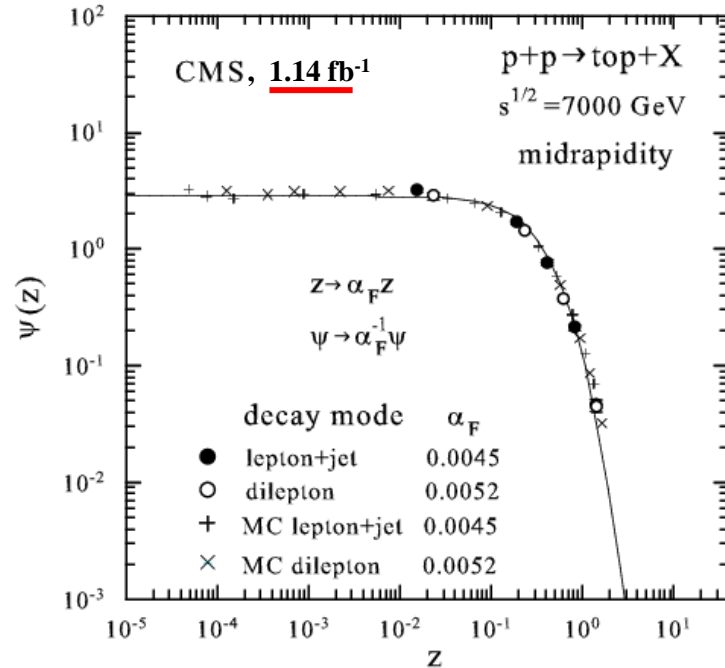


Self-similarity of top quark production at LHC

Differential production cross sections
as a function of the transverse momentum
of the top quarks p_T



CMS Collaboration,
CMS-PAS-TOP-11-013 (2011)



M.T. & I.Zborovský
ISMD'12
Kielce, Poland, 2012

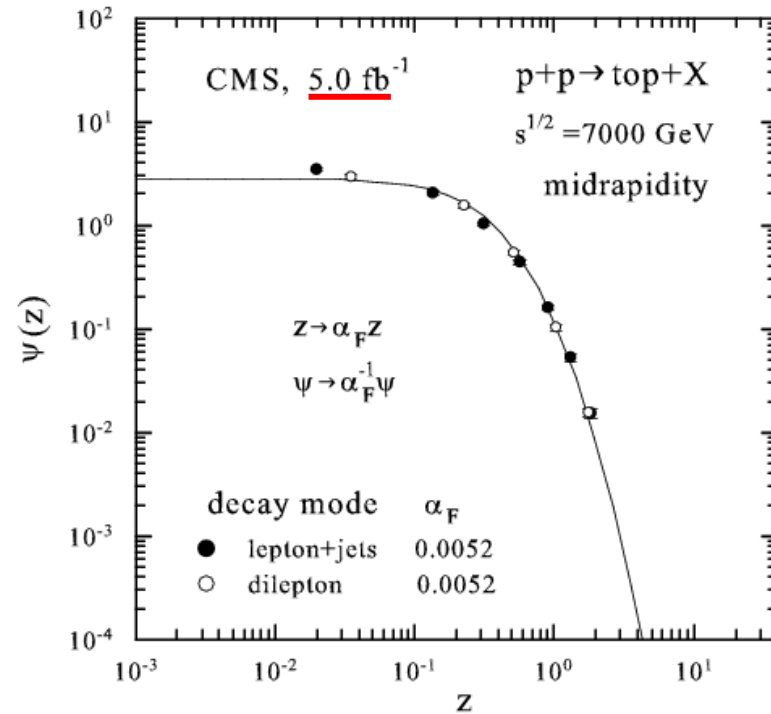
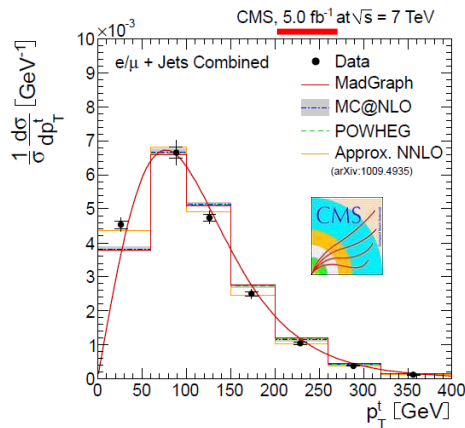
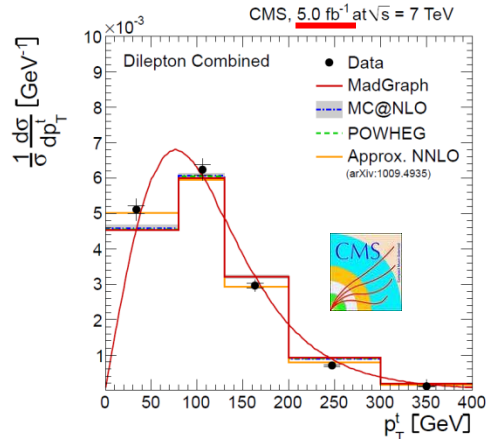
- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\varepsilon_{\text{top}} = 0$
- “Specific heat” $c = 0.25$

CMS data confirm self-similarity
of top quark production in pp



Self-similarity of top quark production at LHC

Differential production cross sections
as a function of the transverse momentum
of the top quarks p_T



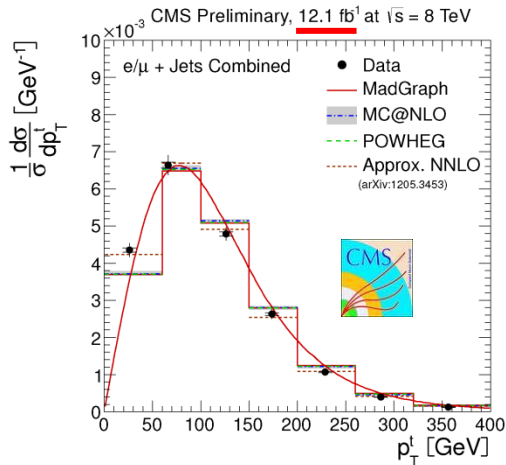
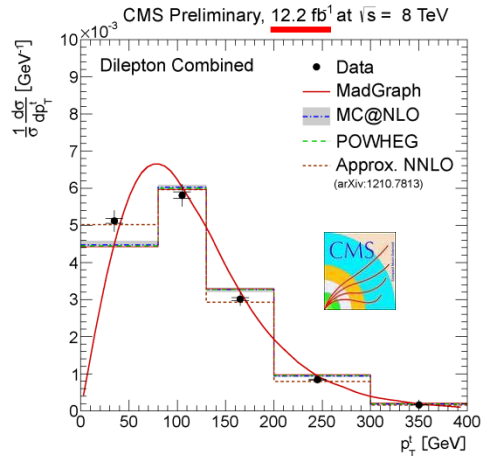
- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\varepsilon_{top} = 0$
- “Specific heat” $c = 0.25$

CMS data confirm self-similarity
of top quark production in pp

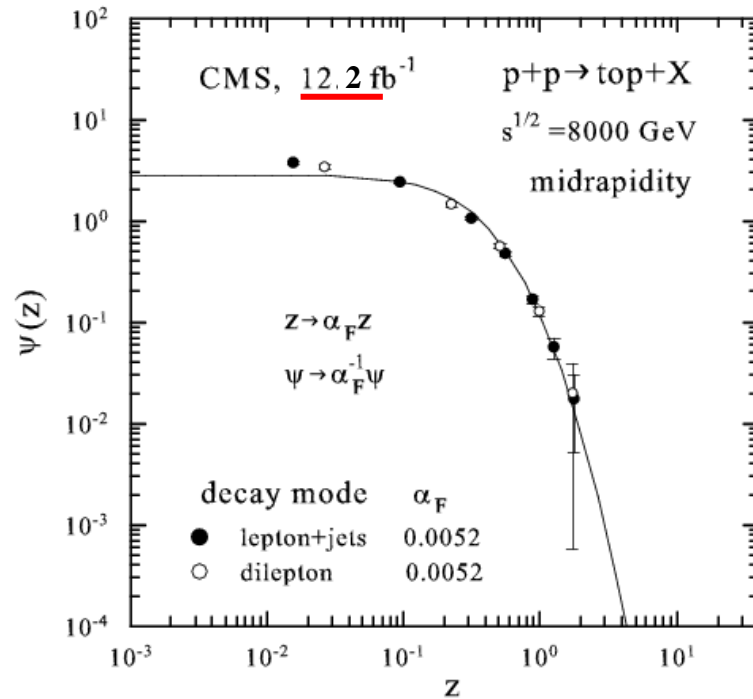
CMS Collaboration,
CMS-PAS-TOP-11-013
Eur.Phys.J.C73(2913)2339

Self-similarity of top quark production at LHC

Differential production cross sections
as a function of the transverse momentum
of the top quarks p_T



CMS Collaboration,
CMS PAS TOP-12-027
CMS PAS TOP-12-028



- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\epsilon_{\text{top}} = 0$
- “Specific heat” $c = 0.25$

CMS data confirm self-similarity
of top quark production in pp

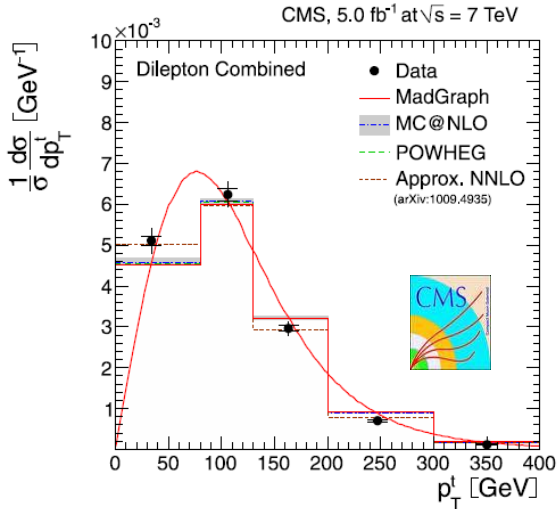
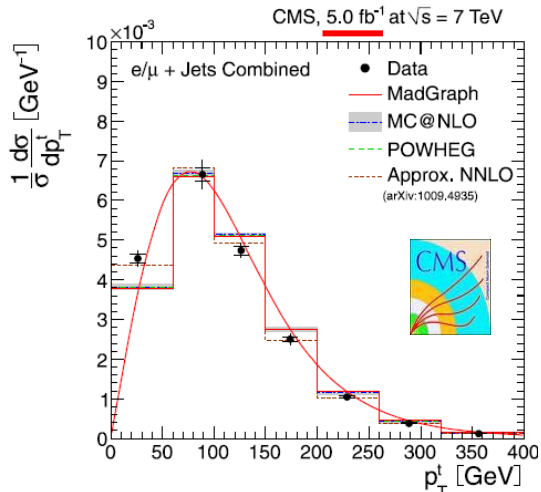


Top flavor & z-Scaling

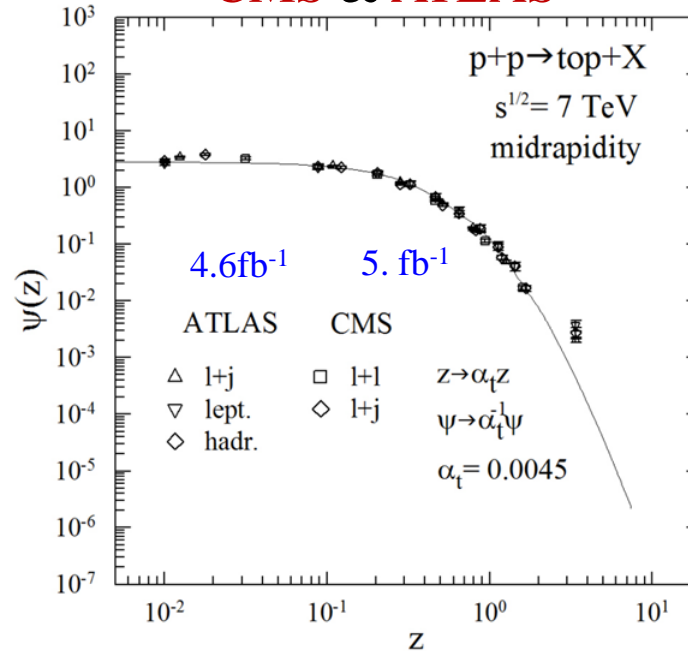
$p\bar{p}$ & pp @ 1.96, 7, 8, 13 TeV
high integral luminosity



Self-similarity of top quark production at LHC @ 7 TeV



CMS & ATLAS



ATLAS
Phys. Rev.
D90 (2014) 072004
JHEP 06 (2015)100

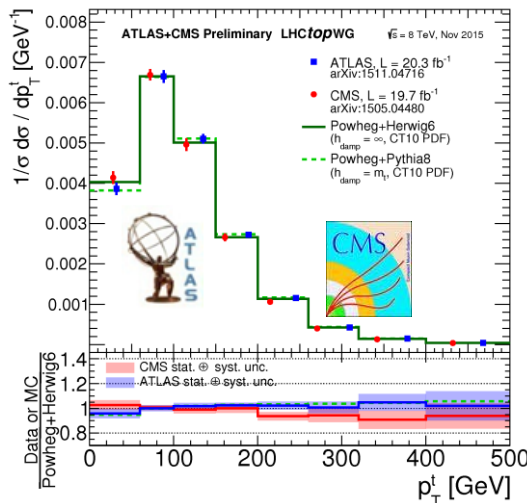
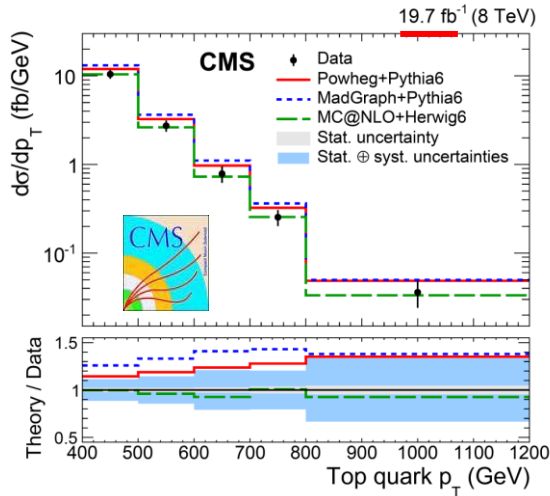
CMS
EPJC 73(2013)2339

- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for or $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\varepsilon_{\text{top}} = 0$
- “Specific heat” $c = 0.25$

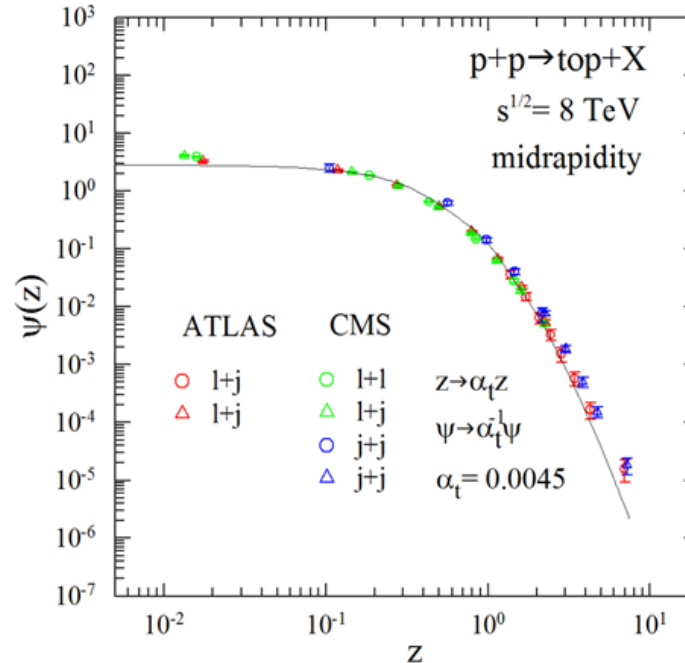
CMS & ATLAS data
confirm self-similarity
of top quark production in pp

Self-similarity of top quark production at LHC @ 8 TeV

Differential production cross sections as a function of the transverse momentum of the top quarks p_T



CMS & ATLAS



- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\epsilon_{top} = 0$
- “Specific heat” $c = 0.25$

CMS & ATLAS data confirm self-similarity of top quark production in pp

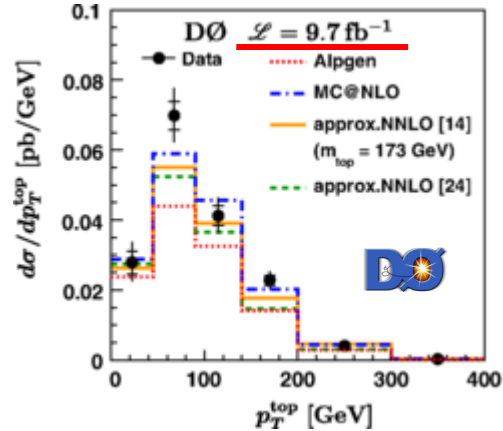
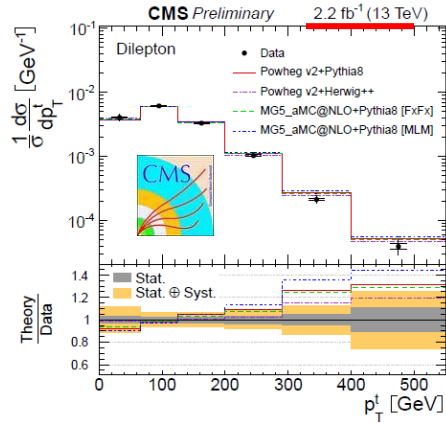
ATLAS
Phys.Rev.D93(2016)032009
arXiv:1511.04716

CMS
EPJC 75(2015)542
EPJC76(2016)128
arXiv:1505.04480
arXiv:1605.00116

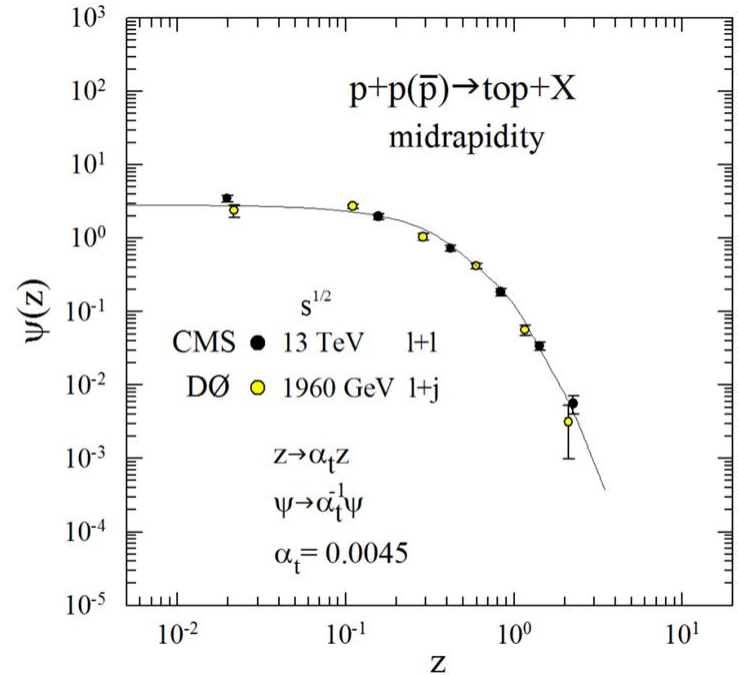
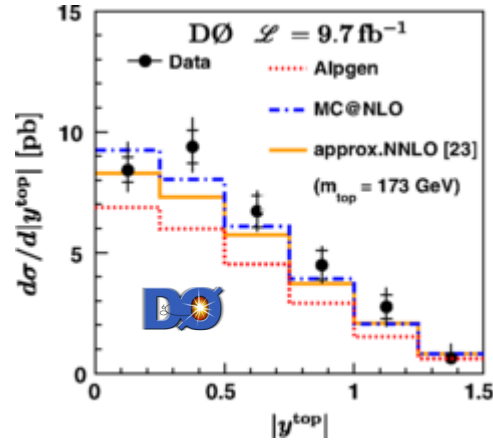
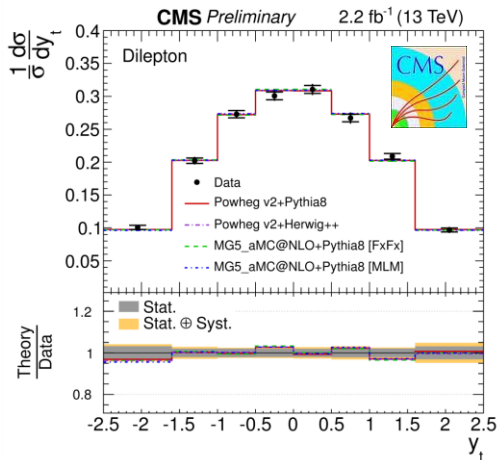


Self-similarity of top quark production at LHC @ 13 TeV

Differential production cross sections
as a function of the transverse momentum of the top quarks p_T



Differential production cross sections
as a function of the rapidity of the top quarks y_t



- Energy independence of $\Psi(z)$
- Flavor independence of $\Psi(z)$
- Saturation of $\Psi(z)$ for $z < 0.1$
- Fractal dimensions $\delta = 0.5$, $\varepsilon_{\text{top}} = 0$
- “Specific heat” $c = 0.25$

CMS-PAS TOP-16-011
DØ PRD 90 (2014) 092006

CMS & DØ data confirm self-similarity
of top quark production in pp & $p\bar{p}$

Self-similarity of top quark production in pp

Self-similarity parameter

$$Z = Z_0 \Omega^{-1}$$

$$Z_0 = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N}$$

Solid line for π^- meson
is a reference curve
 $\varepsilon_{\pi} = 0.2, \quad \alpha_{\pi} = 1$

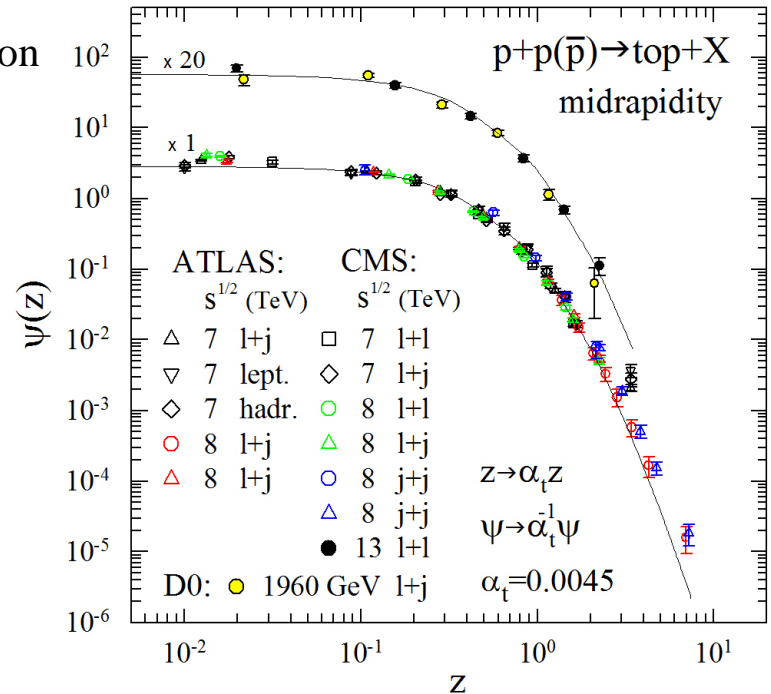
$$\Omega = (1-x_1)^{\delta} (1-x_2)^{\delta} (1-y_a)^{\varepsilon_F} (1-y_b)^{\varepsilon_F}$$

- $dN_{ch}/d\eta|_0$ - multiplicity density
- c - “specific heat” of bulk matter
- δ - proton fractal dimension
- ε_F - fragmentation fractal dimension

Scaling function

$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3}$$

“Collapse” of data points onto a single curve

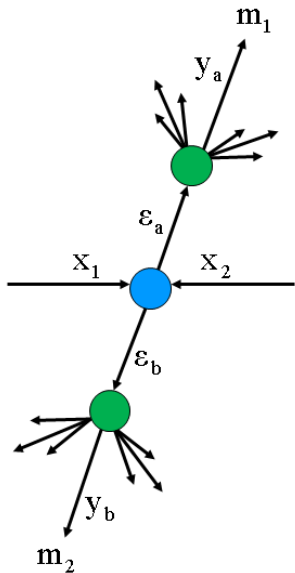


- Energy independence of $\Psi(z)$
- Centrality independence of $\Psi(z)$
- Power law at high z
- Saturation at low z

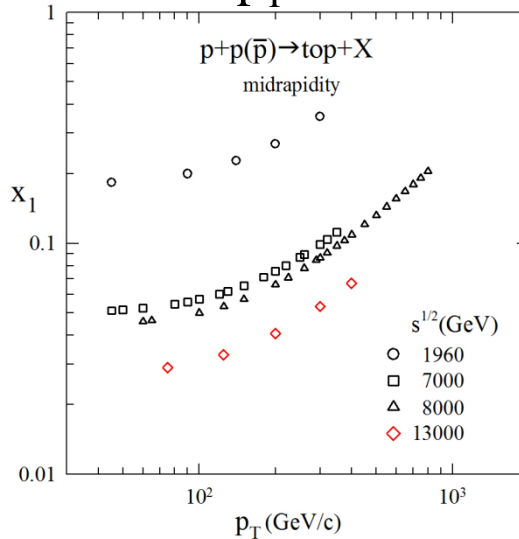
Universality: the same shape of Ψ both for top and π^- (solid line)



Top production at a constituent level



Momentum fractions
vs. p_T & \sqrt{s}



Top quark:

$$y_{\text{top}} \approx 1,$$

$$\epsilon_{\text{top}} \approx 0,$$

$$M_X \approx m_{\text{top}}$$

$$z = z_0 \Omega^{-1}$$

$$\Omega = (1-x_1)^\delta (1-x_2)^\delta (1-y_a)^{\epsilon_F} (1-y_b)^{\epsilon_F}$$

$$M_X = x_1 M_1 + x_2 M_2 + m_{\text{top}} / y_{\text{top}}$$

Negligible energy loss \rightarrow high sensitivity at high x_1 to

- structure of colliding objects (dimensions δ_1, δ_2)
- constituent interactions (“specific heat” c)
- transition of point-like massless top to massive top ($m_{\text{top}} \approx m_{\text{Au}}$)

Verification of universality of $\Psi(z)$ shape over a wide z -range.

Extraction of ϵ_{top} \rightarrow estimation of energy loss.



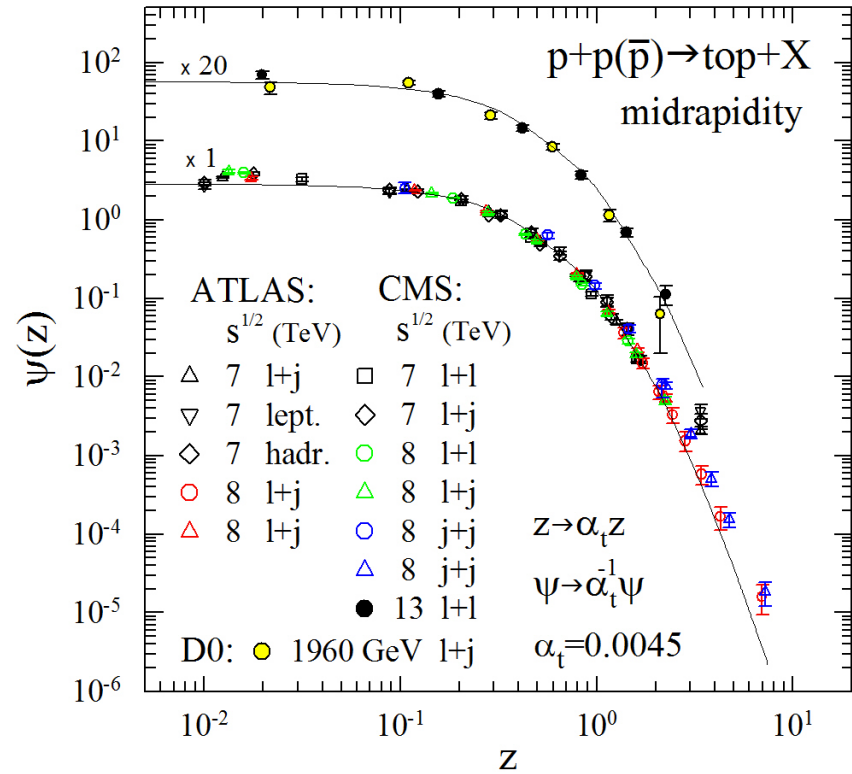
Self-similarity of top quark production at LHC @ Tevatron



$s^{1/2}$ (GeV)

- 1960 PRD90(2014)092006
- △ 7000 PRD90(2014)072004
- ▽ 7000 JHEP06(2015)100
- ◇ 7000 JHEP06(2015)100
- 7000 EPJC73(2013)2339
- ◇ 7000 EPJC73(2013)2339
- 8000 PRD93(2016)032009
- △ 8000 arXiv:1511.04716
- 8000 EPJC75(2015)542
- △ 8000 EPJC75(2015)542
- 8000 EPJC76(2016)128
- △ 8000 arXiv:1605.00116
- ◆ 13000 CMS TOP 16-011

“Collapse” of data points onto a single curve



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- “Specific heat” $c = 0.25$

LHC & Tevatron data
confirm self-similarity
of top quark production in pp & p \bar{p}

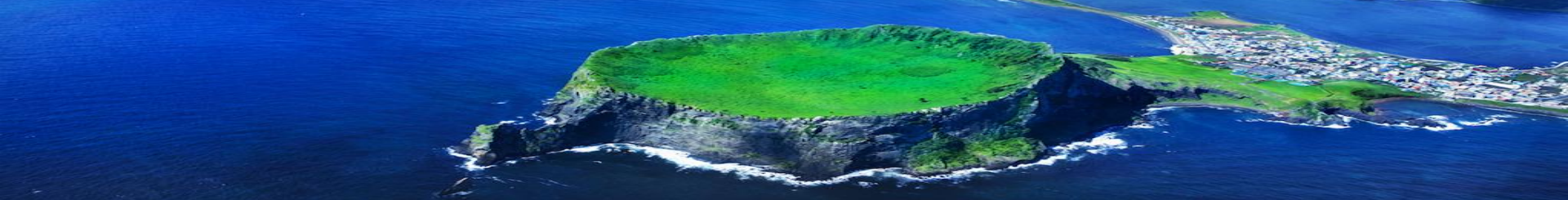


Conclusions

- Results of analysis of new **LHC** data on inclusive transverse momentum spectra of **top quarks** produced in **pp** collisions at $\sqrt{s}=7, 8$ and 13 TeV in **z-scaling** approach were presented.
- New confirmations of **z-scaling** at **LHC** (energy and flavor independence, saturation of $\Psi(z)$) were demonstrated.
- **DØ** data on top transverse momentum spectra in $p\bar{p}$ collisions are in agreement with **CMS** and **ATLAS** data in pp collisions.
- **z-Scaling** of hadron production at high energies manifests **self-similarity, locality** and **fractality** of hadron interactions at a constituent level.

New **TeV-energy** region is available to search for, study and understand new physics phenomena at **LHC**.





ISMD2016

Thank You for Your Attention !

XLVI INTERNATIONAL SYMPOSIUM ON MULTIPARTICLE DYNAMICS
 SEOGWIPO KAL HOTEL, JEJU ISLAND, SOUTH KOREA
 AUGUST 29 - SEPTEMBER 2, 2016

> SESSIONS

- MULTI-PARTICLE CORRELATIONS AND FLUCTUATIONS: FROM SMALL TO LARGE SYSTEMS
- HADRONIC FINAL STATE IN HIGH- p_T INTERACTIONS
- FORWARD PHYSICS AND DIFFRACTION
- PERTURBATIVE AND NON-PERTURBATIVE FEATURES OF QCD
- COLLECTIVITY IN HIGH-ENERGY COLLISIONS: JETS, FLOWS AND OTHERS
- PROTON STRUCTURE, SMALL AND LARGE- x PHYSICS
- COSMIC RAY AND ASTROPARTICLE PHYSICS

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ISMD'16, August 29-September 2, 2016, Jeju Island, South Korea



Back-up slides



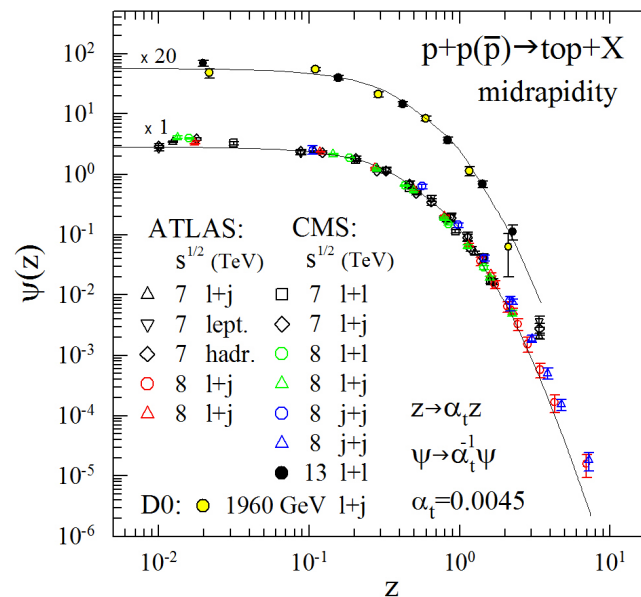
Top-Quark p_T -Spectra at LHC and Flavor Independence of z -Scaling

M. Tokarev (*JINR, Dubna*) & I. Zborovský (*NPI, Řež*)

Self-similarity of top production at **LHC & Tevatron**



- $s^{1/2}$ (GeV)
- 1960 PRD90(2014)092006
 - △ 7000 PRD90(2014)072004
 - ▽ 7000 JHEP06(2015)100
 - ◇ 7000 JHEP06(2015)100
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 - △ 8000 EPJC75(2015)542
 - 8000 EPJC76(2016)128
 - △ 8000 arXiv:1605.00116
 - ◆ 13000 CMS TOP 16-011



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